A circumbinary protoplanetary disc in a polar configuration

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Nearly all young stars are initially surrounded by ‘protoplanetary’ discs of gas and dust, and in the case of single stars at least 30% of these discs go on to form planets. The process of protoplanetary disc formation can result in initial misalignments, where the disc orbital plane is different to the stellar equator in single star systems, or to the binary orbital plane in systems with two stars. A quirk of the dynamics means that initially misaligned ‘circumbinary’ discs – those that surround two stars – are predicted to evolve to one of two possible stable configurations, one where the disc and binary orbital planes are coplanar, and one where they are perpendicular (a ‘polar’ configuration). Prior work has found coplanar circumbinary discs, but no polar examples were known until now. Here we report the first discovery of a protoplanetary circumbinary disc in the polar configuration, supporting the predictions that such discs should exist. The disc shows some characteristics that are similar to discs around single stars, and that are attributed to dust growth. Thus, the first stages of planet formation appear able to proceed in polar circumbinary discs.
The process of star and disc formation is not guaranteed to yield a simple coplanar circumstellar disc, as might be surmised from the coplanar nature of the Solar system. Simulations suggest that once a protoplanetary disc has initially formed around a star or stars, further accretion of material with different angular momenta can result in discs with multiple orbital planes, or discs whose orbital planes are different to the binary stars they orbit\(^2\). IRS 43 appears to be a very young system with a misaligned circumbinary disc\(^6\), evidence that the initial conditions suggested by simulations do indeed occur.

Theory suggests that circumbinary discs should then evolve to one of two possible configurations, a quirk dictated by the orbital dynamics around two stars. For small initial misalignments the angular momentum vector of circumbinary orbits \(L_c\) precesses about the binary angular momentum vector \(L_b\) (a ‘coplanar’ family of orbits), but for larger misalignments \(L_c\) precesses about a vector in the binary’s pericentre direction \(\varpi_b\) (a ‘polar’ family)\(^7\). Because the discs that orbit young stars are gas-rich and hence dissipative, an initially misaligned circumbinary disc will generally evolve to an end state that belongs to one of these two families\(^3,4,8–11\). The expected timescale for this reorientation is generally shorter than the typical \(\sim 3\) million-year disc lifetime\(^12\), meaning that young gas-rich circumbinary discs are most likely to be observed to be in one of the two possible orientations, rather than at an intermediate orientation. While the circumbinary debris disc 99 Herculis is thought to have a polar configuration\(^13\), this disc is four times larger than Neptune’s orbit, and with an age similar to the Solar system does not provide evidence that young gas-rich polar circumbinary discs exist.
Here, we report that the circumbinary disc in the young HD 98800 system is strongly misaligned with the binary orbital plane. We infer that the disc is in the polar configuration by simulating the disc dynamics. We further show that despite this misalignment, the disc shows physical properties similar to discs seen around young single stars.

The HD 98800 system is a well known hierarchical quadruple star system 44.9 parsecs from Earth\textsuperscript{14}, and a member of the \textasciitilde10 Myr-old TW Hydrae Association\textsuperscript{15,16}. It consists of two pairs of binaries (called ‘A’ and ‘B’, or equally ‘AaAb’ and ‘BaBb’) with semi-major axes of about 1 astronomical unit (au), which themselves orbit each other with a semi-major axis of 54 au. The binary BaBb is well characterized\textsuperscript{17}, with an eccentricity of $0.785 \pm 0.005$, ascending node of $289 \pm 1^\circ$ anti-clockwise from North, and inclination of $67 \pm 3^\circ$. Using the new data presented here we derive a new orbit for AB (see Methods), which has an eccentricity of $0.52 \pm 0.01$ and a period of $246 \pm 5$ years, with an ascending node of $4.7 \pm 0.2^\circ$ and inclination of $88.4 \pm 2^\circ$. These orbits as projected on the sky plane are shown in Figure[1] The AaAb orbit is less certain, but the details do not affect our conclusions.

The Northern pair known as HD 98800BaBb has been known to host a bright circumbinary disc since discovery in the 1980s\textsuperscript{18}. The disc is thought to be influenced by the stellar system\textsuperscript{19}, with the inner edge of the disc truncated by the inner binary BaBb, and the outer edge externally truncated by A\textsuperscript{20,21}. The orientation of the disc was initially thought to be coplanar with the inner binary\textsuperscript{20}, but higher resolution observations suggest a different orientation\textsuperscript{21} (see Methods for a comparison with our results). Whether the disc harbours a significant mass of gas has been
unclear, meaning that it has been interpreted as both a gas-rich ‘protoplanetary’ disc\textsuperscript{[21,22]}, and a gas-poor ‘debris’ disc\textsuperscript{[23]}. Detection of oxygen towards the system\textsuperscript{[24]} and molecular hydrogen emission towards B\textsuperscript{[25]}, suggests that this pair is accreting from a gas-rich disc, favouring the former interpretation.

To ascertain the disc orientation, size, structure, and evolutionary status we observed the HD 98800 system with the Atacama Large Millimeter/sub-millimeter Array (ALMA, see Methods). Data were taken at 230GHz (1.3 mm), to image dust continuum emission and the carbon monoxide (CO) J=2-1 rotational transition, and both are strongly detected (Figures 1 and 2). By modelling these data as a disc that lies between inner and outer radii with a power-law surface brightness prescription, we find that the inner edges of the dust and CO are at $2.5 \pm 0.02$ and $1.6 \pm 0.3$ au respectively, while the outer edges are at $4.6 \pm 0.01$ and $6.4 \pm 0.5$ au (see Methods). These models show that the disc is largely axisymmetric, though a small asymmetry in the dust distribution at the inner edge may be a sign of interaction with the binary. The dust and CO components are consistent with having the same orientation; the disc has a position angle of $16 \pm 1^\circ$ (measured anti-clockwise from North) and is inclined by either 26 or $154^\circ \pm 1^\circ$ from the sky plane. While the Doppler shifts seen in CO show that the North side of the disc is rotating towards us (Fig. 2), thus constraining the ascending node to be North of the star, the inclination remains
Figure 1: ALMA 1.3 millimetre continuum image of the HD 98800 dust disc, showing a narrow dust ring 3.5 au in radius that is 2 au wide. White semi-transparent lines show the orbits of the inner binary (BaBb) and the path of the outer binary (AaAb) with respect to BaBb, with dots at the star locations at the time of the ALMA observation. The resolution of these ‘uniformly-weighted’ images (32 × 25 milli-arcseconds, or 1.4 × 1.1au) is given by the ellipse in the lower left corner. The left panel shows the entire system, and the right panel is zoomed in on BaBb.
Figure 2: Intensity-weighted CO velocity (colours) and dust (contours) images. The gas velocity structure is consistent with that expected if the CO disc has the same orientation as the dust. The CO is only shown where it is detected at a signal-to-noise ratio greater than three, and the contours are shown at 20 times the noise level in the continuum image, giving an indication of the location and extent of the dust ring. The resolution of these ‘naturally-weighted’ images (61 $\times$ 54 milli-arcseconds, or 2.7 $\times$ 2.4 au) is given by the ellipse in the lower left corner.
ambiguous because the disc could be rotating either clockwise or anti-clockwise as projected on the sky. That is, these observations do not distinguish whether the East or West side of the disc is closer to Earth.

Of the two possible disc orientations, the $154\degree$ case is only four degrees away from the polar configuration (i.e. is perpendicular to both the BaBb orbital plane and the BaBb pericentre direction), while the $26\degree$ case is inclined $48\degree$ from the BaBb binary plane (which we refer to as the ‘moderately’ misaligned case). The uncertainty on these relative angles is about $4\degree$, so the polar orientation is consistent with being perfectly polar. Given the small chance that a randomly chosen orientation should appear to be in the polar configuration, which is expected based on the dynamics and models discussed above, this configuration is by far the most likely interpretation. That is, the theoretical models provide a prior that leads us to favour the polar configuration, and a sketch is shown in Figure 3.

To further test this hypothesis, we simulated the response of the disc to perturbations from the stellar orbits using both gas-free ‘$n$-body’, and fluid-based smoothed particle hydrodynamics, simulations (see Methods). The main conclusion from the $n$-body simulations is that test particles placed on circular orbits at the observed 2.5-4.6 au radial location of the dust are generally ejected within less than a million years, regardless of the disc orientation. Independent of the disc orientation we therefore conclude that the dust observed with ALMA is embedded within a more massive
Figure 3: Three-dimensional sketch of the polar configuration of the BaBb binary (grey ellipses) and surrounding disc (torus). The axes are indicated by the three labelled arrows. The two triangular planes show the plane of the sky (grey) and of the disc (red), which intersect at an angle of 16° from South (i.e. the disc position angle). The angle between these planes is the disc inclination of 154°. Grey lines show the angular momentum vector of the disc $L_c$ (dotted), and the binary pericentre direction $\omega_b$ (solid), both of which point towards away from Earth. These vectors are aligned within 4°, meaning that for this orientation the disc plane is almost perfectly perpendicular to both the binary orbital plane and the pericentre direction.
gas disc, which acts to stabilize the disc against both interior and exterior stellar perturbations. Our estimates of the gas and dust mass in the disc are consistent with this picture, but do not confirm it because they have large systematic uncertainties (see Methods). The $n$-body dynamics, in concert with the detection of CO, oxygen, and hydrogen gas, therefore suggest that HD 988000BaBb almost certainly harbours a long-lived gas-rich protoplanetary disc.

Our fluid based simulations find that torques from the inner binary re-orient a gas disc in the moderately misaligned configuration to the polar configuration in several hundred years. In contrast, the polar configuration is stable and remains in the observed state for at least 500 BaBb orbits (430 years). While the timescale for this evolution depends on the specific assumptions made for the simulations (e.g. the disc scale height and viscosity), and may be longer than found by our simulations, theory suggests that discs will typically become aligned within a few million years. The re-orientation time is therefore expected to be shorter than the system age of about 10 Myr, and we conclude that the most probable interpretation is that the disc is in the polar configuration.

While we cannot currently detect planets within the HD 98800 disc (the high optical depth and small angular scale hamper imaging, and radial velocity precision is limited for young binaries), our data do show evidence of dust growth. Specifically, our models find that the gas is more radially extended than the bulk of the dust (see also Fig. 2). While the derived edge locations reflect the sensitivity of the observations to some degree, these models account for all of the CO surface brightness, and for 99% of the dust. The dust surface brightness is a factor of a hundred lower at 5.5au compared to 3.5au, which is much larger than the factor of two expected if the dust
emission scaled with the brightness of the gas emission over this distance. Similar differences in
gas and dust radial extent are seen for disks around single stars, and is thought to be caused by in-
ward radial drift of dust particles that have grown beyond microns in size, and/or the in-situ growth
of dust to sizes large enough that their mm-wave emission is fainter at larger distances. Our
models therefore show probable evidence of the effects of grain growth on radial disc structure,
and therefore the same evidence of the first steps towards planet formation seen in equivalent discs
around single stars.

How did this system form? Simulations suggest that such outcomes may be a natural result
of the chaotic nature of star formation. One possibility is that two initially separate binary systems
became gravitationally bound, and misaligned HD 98800BaBb’s disc in the process (and perhaps
destroyed any disc around A). However, simulations show that formation from molecular cloud
material with a range of angular momenta can result in misaligned discs in isolated systems, and
indeed such systems are observed, so it does not appear that the presence of an exterior com-
panion is a necessary condition for forming misaligned circumbinary discs. The IRS 43 system,
with a circumbinary disc misaligned by about 60°, is a possible example of what systems such as
HD 98800 could look like earlier in their evolution before binary torques re-orient the disc (albeit
on a scale of tens of au, rather than a few au).

We may also ask whether polar circumbinary discs might be common. Assuming discs that
are initially randomly oriented relative to the binary orbital plane and that are not massive enough
to affect the binary orbit, and that binary eccentricities are uniformly distributed up to \( e = 0.8 \),
the fraction of discs that should evolve to a polar configuration is 46% (see Methods). If planet formation can proceed equally efficiently in both coplanar and polar configurations, then circumbinary planets on polar orbits are predicted to be nearly as common as their coplanar brethren (though these fractions may be modified by later dynamical evolution\textsuperscript{29}). The most eccentric binaries are the most likely to have polar disc configurations, so it is not surprising that the known transiting circumbinary planets, which are near to coplanar, are all in systems with $e \leq 0.52$, with 8/9 having $e < 0.2$\textsuperscript{30,31}. Polar discs, and perhaps planets, may be a common outcome of circumbinary disc formation, and provide motivation for systematic searches for both.

**Methods**

**Observations and Data Processing** HD 98800 was observed by ALMA in Band 6 (1.3 mm) in two observing blocks on 2017 November 15 and 19, 49 antennas were used in the first block and 45 in the second. The shortest and longest baselines were 92 m and 11.8 km. The correlator configuration used three broad continuum windows with 2GHz bandwidth, and one centred on the CO J=2-1 line with a spectral resolution of 488kHz (0.73km s\(^{-1}\) velocity resolution). Each block comprised observations of HD 98800, interspersed with observations of phase calibrator J1104-2431. J1127-1857 was used as the bandpass and flux calibrator. The time on-source was 34 minutes for each block. The raw data were calibrated using the observatory pipeline with CASA v5.1.

The data were further processed using one cycle of phase self-calibration (self-cal) to improve the signal to noise ratio (s/n). All spectral windows were combined, and the averaging time
('solint') was chosen to be relatively long (20-40min) to avoid flagging antennas due to low s/n, thereby retaining maximal spatial resolution. The rms variation measured in clean images before self-cal with Briggs weighting (robust=0.5) was 27 and 32 µJy beam\(^{-1}\) for the first and second observations. After self-cal these were 20 and 18 µJy beam\(^{-1}\). Attempts at further self-cal did not improve the s/n.

Following calibration the two observations were concatenated into a single set of visibilities for imaging and modelling. This combination was verified to be reasonable by modelling the continuum of each observation separately (as described below), which found that the sky offsets of the disc were consistent to within 0.0002 arcsec (0.01au). The difference in integrated flux densities was consistent to within 1%. In the final Briggs-weighted clean image the beam size is \(46 \times 42\) mas, the rms is 14 µJy beam\(^{-1}\), and the peak s/n is 280. In a naturally weighted image the beam size is \(64 \times 56\) mas, the rms is 13 µJy beam\(^{-1}\), and the peak s/n is 450. In a uniformly weighted image the beam size is \(32 \times 25\) mas, the rms is 43 µJy beam\(^{-1}\), and the peak s/n is 46.

For continuum modelling a single spectral window from the combined observations was used (the first, centred at 1.311 mm) with the 2GHz bandwidth averaged into four channels. While more data could have been used, the continuum s/n is easily sufficient to obtain stringent modelling constraints with one spectral window. Visibility data were time averaged into 20s chunks, and then exported to a text file and modelled as outlined below. The weights associated with each visibility were divided by a re-weighting factor such that a null model produces a \(\chi^2\) value of 1, based on the expectation that each individual visibility measurement has negligible s/n\(^{32}\). The re-weighting factor was 5.8 (which is decreased to 2.6 if the CASA \texttt{statwt} task is run first).
Figure 4: Velocity-averaged CO (moment 0) map. Contours are shown at 2, 3, 4, 5, 6, and 7$\sigma$, with $\sigma = 3.9$ mJy beam$^{-1}$. While the peaks to the NW and SW of the centre appear relatively high, subtraction of a smooth model finds that these peaks are not significant (see lower panel of Figure 5).

For gas modelling the window centred on the CO J=2-1 line was used. The continuum was subtracted using the CASA $\text{uvcontsub}$ task, the two observations merged using the $\text{mstransform}$ task, and 40 channels near the CO line extracted to a series of text files containing the visibilities at each frequency (or equivalently, velocity). A re-weighting factor was again used, which was within a few percent of one. A naturally-weighted clean CO cube has a beam size of $61 \times 54$ mas, an rms of 0.8 mJy beam$^{-1}$ in each 0.73 km s$^{-1}$ channel, and typical peak s/n of 4 to 6 depending on the channel. The intensity-weighted CO velocity (moment 1) map is show in Figure 2, and
the velocity-integrated CO (moment 0) map is shown in Figure 4. Channel maps are shown in the upper panel of Figure 6 where the data have been further averaged to show only 20 channels.

HD 98800 has been observed at millimetre wavelengths many times in the past with single-dish telescopes. These show a considerable degree of scatter, with ref[33] measuring $30.7 \pm 8.2$ mJy and $54.4 \pm 3.61$ mJy at 1.3mm with the CSO and IRAM respectively. Our modelling below yields a total disc flux of $47.4 \pm 0.4$ mJy. Including an absolute calibration uncertainty of 10% yields a final flux measurement of $47 \pm 5$ mJy. Our value is not significantly below the previous single dish measurements, so it is unlikely that we have resolved out significant flux.

The phase centre of the observations is not perfectly centred on either AaAb, BaBb, nor the system photocentre, no doubt caused by some uncertainty in the actual position of the system components and their relative motions as derived by Hipparcos[14]. As another output of the modelling, assuming that the BaBb barycentre is at the centre of the disc, at the time of the observation (2017.874) we find that BaBb is centred at $\alpha = 11\ 22\ 05.17437$, $\delta = -24\ 46\ 39.5043$ ($170.52155986^\circ, \ -24.77764009^\circ$). The positional uncertainty from the modelling is $\pm 0.0001$ arcsec, but the true uncertainty is limited by ALMA’s pointing accuracy, which the Technical Handbook suggests is about 0.03 arcsec.

Visibility Modelling Modelling of the continuum and CO data was done in the visibility plane using an optically thin line of sight integration code. While the dust is likely optically thick, the use of a radiative transfer code would make little difference here because the disc is close to
face-on, and we are therefore simply modelling the surface brightness of the disc as a function of radius. A function specifies the three-dimensional disc density in spherical polar coordinates, which is mapped into a 3d cartesian volume using two or three rotations (the position angle $\Omega$, the inclination $i$, and the argument of pericentre $\omega$ where necessary). Two axes of this cube represent the sky plane and the third the line of sight, and the final continuum image of a given model is created by summing the cube along the line of sight axis. Velocity cubes of the model are created by first computing the radial velocity at each location in the cube. Layers in the velocity cube are again the sum along the line of sight axis, but only including pixels from the cube that are within the velocity range for a given layer.

The range of models that are consistent with the data are found using the Markov-Chain Monte-Carlo (MCMC) package emcee. The log likelihood $-\chi^2/2$ of each model is computed given the visibility data using GALARIO. GALARIO also computes the pixel size and image extent necessary for sufficient $u,v$ resolution when the images are transformed into visibilities, which are 4.6 milli arcseconds per pixel and 2048 pixels.

The strongest signal in the continuum image in Figure 1 is a narrow ring of dust emission, so we model this ring to derive constraints on structure and reveal any lower-level emission. For both continuum and CO we use a simple power-law density model, where the dust or gas lies between two limiting radii $r_{in}$ and $r_{out}$ and where the volume density is a power law function of radius $r^{\alpha}$. The density is specified in a given pixel in the cube, and the vertical scale height is a fixed fraction of the radial distance, so the surface density is $\propto r^{\alpha+1}$. The vertical density structure is Gaussian with the scale height fixed to $0.05r$ for all models, as for a nearly face-on
disc this parameter is poorly constrained. For the continuum model we found that the fit was
significantly improved if the disc inner edge has a small eccentricity $e_{in}$, which was implemented
by varying $r_{in}$ as a function of azimuth. Further parameters are the sky offsets $x_0$ and $y_0$, the disc
position angle East of North $\Omega$ and inclination $i$, and the argument of pericentre $\omega$. The images
are scaled by the total flux $F$ (in the 2d image for continuum, or the 3d cube for CO). There are
therefore eight parameters for the continuum model ($x_0, y_0, \Omega, \omega, i, F, r_{in}, r_{out}, \alpha$, and $e_{in}$). The
density is multiplied by an emission function that mimics the Rayleigh-Jeans tail of a blackbody
(i.e. $\propto 1/\sqrt{r}$). The radial dependence of this function is largely arbitrary as it is degenerate with
$\alpha$, and while it is a reasonable approximation for the dust seen in the continuum, the temperature
dependence for CO may be different. For the CO model the eccentric inner edge parameters $\omega$ and
$e_{in}$ are not necessary as the s/n is much lower, but an additional parameter, the systemic velocity of
HD 98800 BaBb, $v_{sys}$, is needed. We assume the CO orbits a single point mass with the combined
mass of HD 98800BaBb of $1.28 M_{\odot}$.  

While it is likely that the CO and dust are optically thick we found that our models were
sufficient to reproduce the data. We tried modelling the data with a simple optical depth prescrip-
tion where the observed surface brightness in the model sky images was attenuated by a further
free parameter $\tau_{SB}$ via $1 - e^{-SB/\tau_{SB}}$ (i.e. $\tau_{SB}$ is the surface brightness at which the emission be-
comes optically thick), but we found that these models were consistent with $\tau_{SB} = 0$ (and the other
parameters unchanged) and therefore that this additional complication is not necessary to obtain
constraints on the disc extent and spatial orientation.
Figure 5: Residuals after subtracting the best fitting continuum model. The upper panel shows the image with natural weights with solid contours at ±2 and 4σ (with σ = 20 µJy beam⁻¹), and dashed contours at 20σ from the original image. As in other images the stellar orbits are also shown. The lower panel is the same as the upper panel, but for uniform weights, and with σ = 60 µJy beam⁻¹. Here the uncertainties are higher than quoted in the text because the continuum modelling was only applied to one spectral window.
Continuum modelling results: The best fitting continuum model was found using 64 ‘walkers’ (parallel MCMC chains) run for 1000 steps (having discarded a prior ‘burn-in’ run of 1000 steps). The best-fit parameters derived from the posterior distributions are given in Table 1. The y offset $y_0$ is relatively large because the observation phase centre is offset from BaBb as described above. The main parameters of interest here are the disc orientation $\Omega$ and $i$, and the dust extent from $r_{in}$ to $r_{out}$, which are discussed in the main text.

The flux density from the ring of 46 mJy can be converted to a dust mass, if the emission is assumed to be optically thin. Using equation 5 of ref[36] (which assumes an opacity of 1.7 cm$^2$ g$^{-1}$) and assuming a dust temperature of 160K derived from photometry over a range of wavelengths[37], the result is $0.33 M_\oplus$. Whether the dust ring is actually optically thick, and therefore whether the dust mass is underestimated, is uncertain; the flux expected from a ring of uniform surface brightness extending from 2.5 to 4.5au at a constant temperature of 160K is 130 mJy. This estimate does not mean the dust is optically thin however, as the surface density profile is found to be decreasing with radius. The bulk of the dust emission may therefore be concentrated in an optically thick region that is narrower than the best-fit 2au width, an issue that can be resolved with higher spatial resolution observations.

Initial attempts to model the continuum with axisymmetric models left asymmetric residuals suggestive of an offset near the inner disc edge, which motivated the use of an eccentric inner disc edge. While this parameterisation may not be representative of the true structure, our finding
Table 1: **Best-fit parameters and 1σ uncertainties for the continuum model.** The best-fit value is the median, and the uncertainty the average of the 68% confidence intervals, both derived from the MCMC posterior distributions. The flux uncertainty includes a 10% calibration uncertainty, which dominates the uncertainty.

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that the best-fit $e_{in}$ is significantly greater than zero shows that the disc is not axisymmetric, and that this asymmetry lies near the inner disc edge. The position angle of the pericentre is given by the parameter $\omega$; as it is measured from the ascending node the best-fit value of $-73^\circ$ means that the disc is closest to the binary towards the North-West (i.e. a position angle of approximately $-72 + 16 = -56^\circ$). While it is tempting to make comparisons with the simulations in Figure 9, these show gas density and the observed asymmetry is in the dust. Nevertheless, it is likely that the preference for a non-zero inner edge eccentricity results from perturbations from the inner binary, and the structure may be characterized in more detail with higher resolution continuum imaging, and deeper and/or lower spatial resolution line imaging.

Residual images are shown in Figure 5, which shows that our model reproduces nearly all of the observed continuum structure. The peak s/n in the original naturally weighted continuum image for the same spectral window is 300, meaning that the residuals are at most only 1% of the peak. Some emission remains beyond the bright ring at 2-4$\sigma$, suggestive of low-level dust emission that might be recovered more strongly in lower resolution images. Some residual emission is also seen interior to the ring, which might arise from dust entrained in gas that is flowing towards and accreting onto the inner binary, and be related to our finding that the inner disc edge is asymmetric. Accreting material may provide an explanation for the facts that HD 98800 was reported to be photometrically variable by Hipparcos, and that HD 98800B suffers significantly more dust extinction than $A_j^{17}$, $A_j^{19}$, $A_j^{38}$, $A_j^{39}$. 
Figure 6: CO channel maps and residuals. The upper panel shows the original cube with natural weights, where each sub-panel is labelled with the velocity on which the bin is centred (in km s$^{-1}$) and the star is marked by the white ‘+’ symbol. The lower panel is the same as the upper panel, but the best-fitting model has been subtracted. Contours are shown at -2, 2, 4, and 6$\sigma$, where $\sigma = 0.67$ mJy beam$^{-1}$ and the beam size is $0.06 \times 0.05''$. 
Table 2: **Best-fit parameters and 1σ uncertainties for the CO model.** The best-fit value is the median, and the uncertainty the average of the 68% confidence intervals, both derived from the MCMC posterior distributions. The CO flux uncertainty includes a 10% calibration uncertainty (which is similar to the precision).

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<td>$r_{out}$</td>
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<td>0.009</td>
<td>arcsec</td>
</tr>
<tr>
<td>$\alpha$</td>
<td>-1.8</td>
<td>0.4</td>
<td>–</td>
</tr>
<tr>
<td>$v_{sys}$</td>
<td>5.1</td>
<td>0.1</td>
<td>km s$^{-1}$</td>
</tr>
</tbody>
</table>
CO modelling results: Channel maps near the systemic velocity of HD 98800BaBb are shown in the upper panel of Figure 6. The best fitting CO velocity model was found using 64 walkers run for 1000 steps, where 1000 prior steps were discarded as a burn-in. The best-fit parameters derived from the posterior distributions are given in Table 2. The residuals after subtraction of the best-fitting model are shown in the lower panel of Figure 6. The CO disc orientation is consistent with the continuum model results shown in Table 2, but the CO disc covers a greater radial extent, from 1.6 to 6.4au compared to 2.5 to 4.6au.

The peak level of channel emission in Figure 6 is approximately 5 mJy beam$^{-1}$, which we find is consistent with that expected from optically thick CO at an excitation temperature of 70K. A lower excitation temperature would yield a lower flux than observed, while a higher excitation temperature would yield a higher flux, or could originate from optically thin CO.

We can estimate a minimum CO mass by assuming that the CO emission is marginally optically thick ($\tau = 1$) with an excitation temperature of 70K (i.e. this mass estimate only applies if $\tau \gtrsim 1$). The best-fit total CO flux of 0.31 Jy km s$^{-1}$ is then equivalent to a mass of $2.8 \times 10^{-5} M_{\oplus}$. If we assume that the disc is primordial and has a standard $^{12}$CO ratio of $10^4$, then the total gas mass is roughly $0.28 M_{\oplus}$, similar to the dust mass.

In terms of the dust to gas mass ratio, the empirical evidence for which dominates remains highly uncertain because i) even if both are optically thick, the dust optical depth could be much greater than the CO optical depth and thus the dust mass greater than the gas mass (or vice versa), ii) the CO excitation temperature may be higher than our 70K estimate, in which case the gas
would be optically thin and the mass lower than our minimal estimate, and iii) the ratio of molecular hydrogen to CO could be different to our assumed value, in which case the total gas mass could be higher or lower than our estimate, even if the CO mass is correct. **While it might be expected that the gas in the HD 98800 disc is depleted because the system is relatively old, the results of our $n$-body simulations below suggest that the dust dynamics are dominated by the gas, and therefore that the gas/dust ratio is not significantly below unity. However, the possibility of inward radial dust drift suggests the gas/dust ratio may be lower than expected from the interstellar medium at the location of the dust ring.** Further observations that target other $^{12}$CO transitions, and optically thinner lines such as $^{13}$CO and C$^{18}$O, are needed to provide further information on the disc optical depth and gas temperature. **As noted above, higher spatial resolution continuum observations are also needed to understand the dust optical depth.** Such work is well motivated, as the simple ring-like nature of the disc may make it an ideal object for studying dust-gas interaction.

**Comparison with VLA** Ribas et al. (ref[21]) imaged the HD 98800B disc with the Karl G. Jansky Vary Large Array (VLA), and derived constraints on the continuum disc size and orientation (they did not detect CO). They report a disc inclination of 40-45° at a position angle of 0-10°, but do not quote formal confidence intervals, and do not discuss how this orientation compares to the binary orbital planes. We modelled the VLA image using the model described above (though with $\alpha$ fixed in the range -1 to 0, as the s/n is much lower), and find a disc extent consistent with that derived from ALMA, and an inclination of $35 \pm 7^\circ$ and position angle $9 \pm 10^\circ$, also consistent with our results.
Orbits Ref\cite{40} find that the systemic velocity of AaAb (12.75 km s\(^{-1}\)) was more positive than BaBb (5.73 km s\(^{-1}\)) in the early 1990s, when A and B were near maximum elongation. Thus, at that time BaBb was moving towards Earth relative to the system centre of mass. The ascending node of the AB orbit (measured East of North) as reported in previous literature is therefore incorrect and should be near 4.2°, not 184.2° \cite{40,41}. Thus, as indicated in the figures, AaAb will go behind the disc in 2026. AaAb being a binary, time-series photometry may reveal further details about the disc structure and AaAb orbit in a manner similar to KH 15D \cite{42,43}.

Using the current best-fit visual orbit for AB \cite{41}, the radial velocity of BaBb should be higher at the epoch of our ALMA observations (2017.874) than in the last few decades, because it is now closer to AaAb and moving more slowly towards Earth. However, the velocity of 5.1 km s\(^{-1}\) at epoch 2017.874 is lower than 5.73 km s\(^{-1}\) at 1991.96 found for BaBb by ref \cite{40}. That is, relative to the system centre of mass BaBb is moving towards Earth more rapidly now than it was in the 1990s. A possible reason is that the orbit is more eccentric than the best-fit visual orbit suggests.

To derive an updated orbit, we obtained previous observations of the AB separation and position angle from the Washington Double Star catalogue (WDS) \cite{44}. The system does not appear in Gaia DR2, presumably because of the multiple nature of the system. These data extend back to the early 1900s, and all observations before 2009 have no uncertainties. Based on the scatter from fitting results, we estimated pre-1950 observations to have position angle uncertainties of 2°, 1950-2009 observations to have uncertainties of 1°, and all pre-2009 separations to have uncertainties of 0.1”. Post-2009 position angle uncertainties were assumed to be 0.5°, the estimated systematic uncertainty \cite{41}, and separation uncertainties were used as given. Two further observations are the
Table 3: **Best-fit parameters and $1\sigma$ uncertainties for the AB orbit.** The best-fit value is the median, and the uncertainty the average of the 68% confidence intervals, both derived from the MCMC posterior distributions.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
<th>Uncertainty</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
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<td>arcsec</td>
</tr>
<tr>
<td>e</td>
<td>0.517</td>
<td>0.007</td>
<td>–</td>
</tr>
<tr>
<td>i</td>
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<td>0.1</td>
<td>degrees</td>
</tr>
<tr>
<td>$\omega$</td>
<td>64</td>
<td>2</td>
<td>degrees</td>
</tr>
<tr>
<td>$\Omega$</td>
<td>4.6</td>
<td>0.2</td>
<td>degrees</td>
</tr>
<tr>
<td>T</td>
<td>2023.0</td>
<td>0.5</td>
<td>years</td>
</tr>
</tbody>
</table>

7.02 ± 0.2 km s$^{-1}$ difference between the radial velocity of A and B at epoch 1991.96, and the -0.61 km s$^{-1}$ difference between the 1991.96 and 2017.874 velocities for B, which assumes that the radial velocity of B is the same as the systemic velocity $v_{sys}$ derived from the CO modelling.

To fit an orbit to these data we compute the position angles, separations, and 1991.96 and 2017.874 radial velocities, from which we derive a $\chi^2$. As with the visibility modelling described above we use the python `emcee` package to find the best-fitting orbits, and the results are shown in Figure [7 and Table 3](#). The fitted parameters are the semi-major axis $a$, the eccentricity $e$, the inclination $i$, the argument of pericentre $\omega$, the ascending node $\Omega$ (measured anti-clockwise from
Figure 7: Posterior distributions for the AB orbit, showing that some parameters are degenerate (e.g. $T$ and $\omega$). Contoured sub-panels show the distribution of points from the MCMC chains, where high-density regions are indicated by the greyscale and contours, and lower density regions by dots representing individual steps in the chains. Histogram sub-panels show the posterior distributions, with median and 68% confidence intervals marked by dashed lines, with titles quantifying those ranges. The mass of B has been omitted from this plot, as it was set by a prior (see text).
North), the time of pericentre passage $T$, and the mass of A $M_A$. The mass of A is estimated as $1.3 \pm 0.15 M_\odot$ and is included as a parameter in the fitting with a prior reflecting this uncertainty. We assumed a mass of $1.28 M_\odot$ for B, which is well constrained.

Introduction of the additional radial velocity constraint changes the orbital parameters compared to the most recent published orbit, which is similar to the most recent orbit derived by A. Tokovinin (and which has been updated with the correct ascending node). The main difference relative to these previous orbits are an increased orbital period (251 vs. 206 years) and eccentricity (0.52 vs. 0.43), and that uncertainties can now be assigned to each parameter; currently the AB orbit is graded ‘5’ in the 6th Orbit Catalog, meaning that the orbital elements ‘may not even be approximately correct’ (however the proximity to our updated solution suggests that in hindsight a higher grade could have been assigned). There remain small systematic offsets in the residual separations and position angles, so it is possible that the orbit will change somewhat with further monitoring. We use our best-fit values for the AB orbit in the $n$-body simulations below.

**Simulations $n$-body:** We simulated the system as gas-free using the REBOUND code, to test where particles could orbit in the absence of stabilising forces that would arise if the gas mass is comparable to or greater than the dust mass. While ref provide stability maps for a wide range of circumbinary configurations, here the effect of the outer binary is also important, so system-specific simulations are necessary. We modelled the inner binary BaBb using the best-fit

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1See [http://www.ctio.noao.edu/~atokovin/stars](http://www.ctio.noao.edu/~atokovin/stars)
Figure 8: Particle lifetimes for the moderately inclined (left panel) and polar (right panel) disc orientations, shown as a function of semi-major axis and inclination to the sky plane for the best-fit disc orientation. Each pixel shows the lifetime of a single particle with a random initial true anomaly, meaning that no particles in the moderately inclined disc survive for 1Myr. Particles in the polar configuration do survive for up to 1Myr, but only at semi-major axes just outside 4 au and between 5-7au.
parameters from ref[17], the outer binary AaAb as a single object, the AB orbit as derived above, and all other particles as massless. The disc appears largely circular based on the continuum modelling, so we initialized particles on circular orbits in one of the two possible disc orientations at a range of true anomalies, and ran simulations for 1Myr. We used the ‘whfast’ integrator[49] with a time step of 1/20th of the BaBb orbital period. Particles with distances more than 2000 au from the system centre of mass are removed and their removal time recorded; while the integration method does not allow collisions nor compute close encounters accurately, these events soon lead to particle ejection anyway.

The results are shown in Figure 8, and show that in the gas-free case test particles do not survive for 1Myr in the moderately inclined disc configuration. Particles in the polar configuration do survive for up to 1Myr, but only at semi-major axes between 5 and 7 au and a very narrow band near 4au, and neither region is consistent with the extent seen in the continuum with ALMA. In both configurations particles beyond 7 au are typically removed in 5000 years; comparing this time to the 250 year period of the AB binary suggests that short-term interactions are the cause (i.e. the removal time is tens of AB orbits, not hundreds or thousands which would suggest long-term secular effects), and therefore that 7 au is the approximate outer disc truncation radius imposed by A.

These results therefore indicate that gas-free dynamics do not apply to the dust observed between 2.5 to 4.6 au around HD 98800BaBb, and that the dust is almost certainly strongly influenced and stabilized by gas. The disc is therefore probably gas-rich (i.e. the gas mass is greater than the dust mass), and given the detection of hydrogen gas emission[25], likely still in the primordial
protoplanetary disc phase.

Smoothed Particle Hydrodynamics: We used Phantom [50] to simulate the response of the two possible disc configurations to perturbations from the inner binary, assuming a gas-rich protoplanetary disc. The simulations were run for 500 orbits of the inner binary (430 years.) We did not include the outer binary, as the disc was found to change orientation on a shorter timescale (∼100 years) than the period of the outer binary (∼250 years). This timescale difference of course does not mean that A has no effect on the disc around B, since test particles in the polar configuration are truncated at around 7 au, which is near the outer extent of the detected CO.

For the disc, the simulations used the same SPH parameters as ref [3] and 300,000 particles. While we cannot be sure that these specific parameters apply to HD 98800’s disc, theory suggests that real discs are likely to become aligned before they disperse [18, 10]. While the absolute timescales derived from our simulations may be inaccurate, as the disc scale height and viscosity could be different, the evolution is likely to be similar.

The results of simulations of the two configurations are shown in Figure [9], where the left set of panels shows the moderately misaligned case, and the right panels the polar case (the images were created using splash [51]. In each pair of images, the left subpanels show the disc density projected onto the sky plane, and the right panel a side view. The time evolution (moving down the panels) shows that the polar configuration does not significantly change orientation, while the
Figure 9: SPH simulations of the disc in the moderately misaligned (left panels) and polar (right panels) configurations, where each panel is separated by 100 binary orbits (about 86 years) in time, from top to bottom. The colour scale shows gas column density. In each $5 \times 5$ au panel, the x/y axes correspond to the sky plane in au, and the z to the line of sight (with +ve z towards Earth). The moderately misaligned disc precesses significantly over the duration of the simulation, in particular over the first few hundred orbits, eventually reaching a similar orientation to the disc in the polar configuration.
moderately misaligned case does. In fact, the moderately misaligned disc eventually reaches the polar configuration, though has been significantly perturbed and disrupted in the process. Thus, we conclude that the polar disc configuration is by far the best interpretation of the data, as the lifetime of the disc in the moderately misaligned case is very short relative to the stellar age of ten million years. Because the time taken to re-orient the disc is short relative to the AB orbital period, and the effect of A where the disc is observed is minimal, including A in the simulations would not change this conclusion.

Some spiral structure has been induced in the disc in the polar case; if the HD 98800 disc has similar structure these perturbations may be the cause of the asymmetry that requires the continuum model to have non-zero $e_{in}$.

Population estimate of disc orientations  To gauge whether circumbinary discs in the polar configuration might be common, we make a simple population estimate (see also ref [4], which provides equations that could be used to make a similar estimate). The assumptions are that i) the discs do not have sufficient angular momentum to re-orient the binary (i.e. test-particle dynamics apply), ii) discs initially have uniformly distributed orientations with respect to the binary, iii) the binary eccentricity distribution is uniform between 0 and 0.8 [28]. The most uncertain of these is ii); if circumbinary discs are more often initially coplanar with their binaries the estimated fraction would be lower than we find below.
Figure 10: Model of the fraction of uniformly oriented circumbinary discs that evolve to polar orbits, as a function of eccentricity. Each panel shows contours of the constant of motion $c$ for circumbinary orbits uniformly spaced between $-4e^2$ and 1. Polar orbits lie in the grey regions (dashed contours), and coplanar orbits lie in the white regions (solid contours). Dots show a subsample of 100 random orientations, with coplanar configurations shown by grey dots, and polar configurations by black dots. The title of each sub-panel shows the binary eccentricity and the fraction of polar orbits.
The evolution of a low-mass circumbinary disc can be visualized in the $i \cos \Omega, i \sin \Omega$ plane with plots like those shown in Figure [10] where the constant of motion for a given disc is

$$c = \cos^2 i - e^2 \sin^2 i \left(5 \sin^2 \Omega - 1\right).$$

The dividing line ('separatrix') between orbits that are coplanar (i.e. those that precess about the binary orbital plane) and polar (i.e. those that precess about a plane perpendicular to the binary pericentre direction) is given by $c = e^2$. We assume here that the region of parameter space in which a disc initially starts determines the outcome; dissipation causes the disc plane to relax to coplanar (0,0), or polar (0,±π/2), and discs do not cross the separatrix.

To estimate the fraction of discs on coplanar and polar orbits for a given eccentricity, we populate the $i \cos \Omega, i \sin \Omega$ plane with $N = 10^6$ orbits. Orbits are uniformly distributed by generating two random numbers $u$ and $v$ between 0 and 1 for each orbit, from which we obtain $\Omega = 2\pi u$ and $i = \cos^{-1}(2v - 1)$. We then calculate $c$ for each of the $N$ orbits, and find the fraction that lie on polar trajectories (i.e. the fraction in the grey region in Figure [10]).

We then repeat the calculation at a series of 16 binary eccentricities between 0.0 and 0.8, as shown in Figure [10]. The overall fraction of discs that should evolve to polar configurations given our assumptions is the average value across this range of eccentricities, and found to be 46%. The systems that evolve to polar configurations are heavily weighted towards high eccentricities, as the fraction of parameter space where this happens is much larger. As noted in the main text, the eccentricities of the binaries that host circumbinary planets are typically small, and higher eccentricity binaries are the most promising focus for misaligned circumbinary planet searches.
Data and code availability The ALMA data used in this study are available in the ALMA Science Archive at http://almascience.eso.org/aq/. That is, they will be when the proprietary period lapses.

The post-processing, modelling, and other scripts used in this study are available on github at https://github.com/drgmk That is, they will be made available in a dedicated repository upon publication.


**Author Information** The authors declare that they have no competing interests. Correspondence and requests for materials should be addressed to g.kennedy@warwick.ac.uk.

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Author Contributions GMK conceived the project, analysed the data, carried out the modelling, and wrote the manuscript. LM contributed gas calculations and provided advice on self-calibration. BMY set up and ran the $n$-body simulations. DP provided advice on running the SPH simulations. All co-authors provided input on the manuscript.