

Liquid-phase adsorption: common problems and how we could do better

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Abstract

1 Adsorption plays a vital role in many applications from adsorbents for concentrating valuable
2 compounds or removing pollutants to catalysts. In gas and liquid phases, the adsorption
3 phenomena may look similar and the results are often transferred. But solvents play a role
4 and may change the adsorption behaviour even for strong adsorbates – liquid phase
5 adsorption is different!

6 The review covers kinetics and thermodynamics of adsorption processes and focuses on
7 several areas that receive only minor attention despite being crucial for obtaining reliable
8 results. Such underappreciated areas include the analysis of how to maximise experimental
9 accuracy of adsorption studies and analyse the model parameters and their confidence
10 intervals; the effect of the mathematical representation and model linearization on the
11 results; the possibility of processes other than adsorption during the experiments.

12 The experiments based on disappearance of the adsorbate from the equilibrium solution
13 shall be performed to ensure at least 10% decrease in concentration for reasonable
14 accuracy. Regression analysis and analysis of the confidence intervals of the parameters
15 merit particular attention as well as an independent validation of the model assumptions.
16 Even an excellent data fit may provide results differing by several times from the correct
17 values.

18 Adding to the dispute on dimensions in the adsorption constants in van't Hoof equation, the
19 review adds arguments in favour of using constants in L/mol units. The review concludes
20 with the proposed workflow in the analysis of liquid-phase adsorption data from the data
21 acquisition to data analysis and modelling and offers a Matlab app for Langmuir adsorption
22 data analysis.

23 **Keywords:** adsorption; error; Langmuir; catalysis; Equilibrium constant; adsorption kinetics

24 **1. Introduction**

25 In the United Kingdom as an example, chemicals constitute the 3rd largest manufacturing
26 sector that employs 400,000 people and generates £48.7bn turnover [1]. The chemicals
27 manufacturing relies on catalytic processes, mainly heterogeneous catalysis, judging by the
28 value and scale of the production [2,3]. There is barely a synthesis that does not include a
29 catalytic step – from petroleum cracking into fuels to the synthesis of cancer drug candidates
30 [4–6]. Adsorption extends far beyond catalysis being vital in pollution removal, in
31 concentrating of rare compounds. Aqueous effluents from most industries such as paint,
32 pesticide, petroleum, printing, pharmaceuticals, wood, paper, steel, textile contain chemicals
33 are treated by adsorption processes [7].

34 Adsorption of substrates on the catalyst surface is one of the key reaction steps - the steps
35 critical for the catalyst performance but all too often overlooked. Adsorption energy must fall
36 within a narrow range to provide the highest reaction rate – too strong adsorption hinders
37 reaction creating catalyst surface overly occupied with the substrate, too weak interaction
38 provides low catalyst coverage and low probability of the reaction. This Sabatier principle is
39 one of the key findings in catalysis – the corresponding volcano plots (reaction rate versus
40 adsorption energy) are observed in all the areas of catalysis [8–10]. Complex reaction
41 networks with multiple intermediates and bond formations could be accurately described
42 only in terms of a single desorption process [11]. On the other hand, the adsorption
43 phenomena are sometimes detrimental for catalysis – strong adsorption of by-products is
44 often the cause for catalyst deactivation [12–15]. Hence, understanding of the adsorption
45 processes is vital for the catalyst design.

46 The adsorption process itself, however, is scarcely studied directly in liquid-phase reactions.
47 The insights are often obtained only indirectly using kinetic modelling or DFT computation.
48 Data generated in gas-phase is often transferred into the liquid phase. This approach seems
49 reasonable especially for non-reactive solvents and strong adsorbates. However, such a
50 common sense does not always hold. For example, Pt nanoparticles encapsulated with
51 polymer dendrimers show drastically different behaviour in solvents compared to gas-phase
52 even for carbon monoxide [16]. In gas phase, the particles adsorb carbon monoxide weakly
53 with low capacity; in liquid-phase, both the capacity and adsorption energy increase because
54 the dendrimer polymer swells and opens the catalyst surface [16]. Considering that such a
55 dramatic effect was observed for one of the strongest adsorbates, the validity of a casual
56 transfer of results from gas phase into the liquid phase becomes questionable.

57 The study of liquid-phase adsorption in catalysts differs from conventional adsorbates, and
58 this difference may bring insights into the conventional adsorption. Conventionally, the dyes,

59 heavy metals or environmental pollutants in low concentration are adsorbed over active
60 carbons or natural materials [7,17–20]. By their design and intended application, these
61 adsorbents must have a high adsorption capacity with high adsorption constant. For
62 catalysts, in contrast, the Sabatier principle limits the adsorption constant. Moreover, the
63 supported catalysts with a few percent of the active component have a much lower
64 adsorption capacity. Both the lower constant and capacity make the adsorption studies much
65 more challenging and demanding. Such demands, however, surface many critical aspects of
66 the adsorption studies; therefore, the insights and conclusions derived will be of value for all
67 aspects of the liquid phase adsorption.

68 Understanding the adsorption processes with direct studies in liquid phase could open ways
69 for a deeper understanding of the reaction mechanisms and development of more selective
70 and efficient catalysts. This review discusses the main adsorption models and potential
71 problems which attract little attention but can have drastic implications on the results
72 obtained.

73 **2. Experiments on liquid-phase adsorption**

74 The adsorption experiments are generally based on the material balance. An adsorbent
75 material is exposed to the adsorbate solution with a known concentration. The adsorbate
76 concentration decreases in the solution ($V_{solution}$) and adsorption (q_e) is calculated as the
77 difference between its introduced ($C_{initial}$) and the remaining concentrations ($C_{equilibrium}$)
78 based on the equation 1. Adsorption is often normalised by the adsorbent mass.

$$79 \quad q_e = V_{solution} (C_{initial} - C_{equilibrium}) \cdot \quad 1$$

80 This approach is widely used in the analysis of dyes or metal ions [17,21–24] as well as for
81 the catalytic applications [25]. Obviously, this material balance approach is simple, however,
82 there are several problems that the reader must be aware of.

83 The first problem with the approach is the possibility of unforeseen interactions. These may
84 include chemical reactions, reactions with the impurities, and the effect of the adsorbent on
85 the medium. For example, the adsorption of Cr(VI) brought in contact with an adsorbent may
86 lead to reduction in addition to adsorption. Species of Cr(VI) may react with the surface to
87 form Cr(III) and be desorbed [26]. As a result of Cr(III) desorption, the Cr(VI) content in the
88 solution decreases. In the case of photometric analysis of Cr(VI) concentration, a strong
89 decrease will be observed that may be wrongly attributed to high adsorption. Hence to avoid
90 such problems, a possibility of such reactions as well as alternative analysis methods shall
91 be considered.

92 The second problem comes from using the concentration difference in equation 1 which may
 93 dramatically increase measurement errors. Equation 2 shows the error in the adsorption
 94 determined with the experimental errors denoted with symbol δ :

$$95 \quad \delta q_e = |q_e| \sqrt{\frac{\delta V^2}{V^2} + \frac{\delta C_{initial}^2 + \delta C_{equilibrium}^2}{(C_{initial} - C_{equilibrium})^2}} \quad 2$$

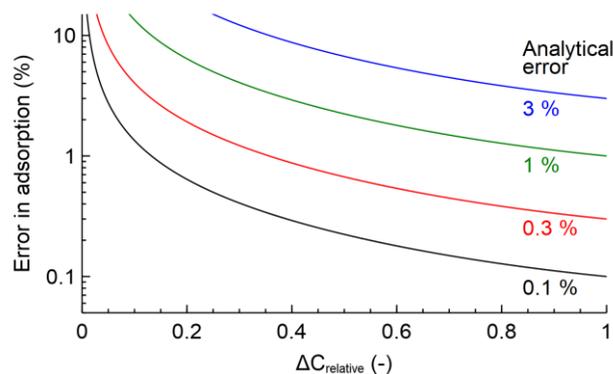
96 The second term under the square root shows that the error in the adsorption increases
 97 when the *relative change* in concentration is small. This conclusion is intuitive – analysis of
 98 small changes against a large background is difficult.

99 The analytical error (in concentration) is often proportional to the determined value (
 100 $\delta C = \xi \cdot C$) when concentration is far from their detection limits [27,28]. Neglecting errors in
 101 volume measurement, the relative error in adsorption may be simplified as shown in
 102 equation 3:

$$103 \quad \frac{\delta q_e}{|q_e|} = \xi \frac{\sqrt{C_{initial}^2 + C_{equilibrium}^2}}{|C_{initial} - C_{equilibrium}|} = \xi \sqrt{1 + \frac{2}{\Delta C_{relative}} + \frac{2}{\Delta C_{relative}^2}}, \quad 3$$

104 where $\Delta C_{relative} = \frac{C_{initial} - C_{equilibrium}}{C_{initial}}$.

105 Fig. 1 shows that the error in the adsorption analysis is affected by the *relative* decrease in
 106 concentration. If the relative change in concentration is small (<0.05), the error in adsorption
 107 dramatically increases rendering results unreliable. A relative change in concentration,
 108 however, depends on both the intrinsic adsorption properties and on the amounts and
 109 concentrations used.



110
 111 Fig. 1. The relative adsorption error as a function of analytical error and the relative change
 112 in adsorbate concentration; the analysis is based on the material balance approach
 113 (equation 1).

114 The error analysis shows that there is a limit on the concentration range that could result in
115 accurate experimental results on adsorption. Moreover, excellent analytical reproducibility is
116 important being a limiting factor in adsorption accuracy.

117 Considering limitations in the material balance approach, an alternative method of directly
118 analysing the amount of material adsorbed seems particularly promising. Such a method
119 means detecting the adsorbed material directly on the adsorbent. In case of gas phase, such
120 studies are somewhat easy considering an absence of solvent and the possibility for direct
121 spectroscopic and even gravimetric analyses. Examples include titration of acid sites of
122 zeolite materials with nitrogen bases and observing a decrease in acidic groups in the
123 spectra or appearance of new bands [29,30]. These methods, however, are fraught with their
124 own issues and uncertainties [31]. (Spectroscopic studies require knowledge of molar
125 absorption coefficients which may change with coverage). Another way of studying the
126 amount adsorbed may be desorption experiments performed, for example, carrying out
127 solvent exchange [32] or temperature-programmed desorption [33].

128 The material balance experiments may over-estimate adsorption because of unforeseen
129 reactions between the adsorbate and the material; the desorption experiments under-
130 estimate in case of dissociative or strong adsorption. Therefore, all studies require attention
131 and care. Independent data validation such as a combination of both adsorption and
132 desorption or a combination of spectroscopy with gravimetry is a good way to minimise the
133 uncertainty [34].

134 3. Adsorption isotherms and data analysis

135 Once the adsorption data are obtained over a range of equilibrium concentrations, these are
136 conventionally presented and analysed in terms of adsorption isotherms. There are many
137 models that vary in physical meaning, the number of parameters and the accuracy of the
138 description. Here, several widely used adsorption isotherm models are presented and more
139 details could be found in reviews by Tran et al. or Rangabhashiyam et al. [17,26].

140 The Langmuir model is omnipresent because of simplicity and obvious physical meaning of
141 the parameters. Equation 4 shows the relationship between the adsorption at equilibrium
142 concentration $C_{equilibrium}$, adsorption constant K_L , and maximum adsorption capacity of q_{max} :

$$143 \quad q_e = q_{max} \frac{K_L C_{equilibrium}}{1 + K_L C_{equilibrium}} . \quad 4$$

144 The Langmuir model assumes that the adsorbent surface is uniform – it contains a fixed
145 number of sites that demonstrate identical adsorption energy, the adsorbant molecules could
146 adsorb reversibly only over unoccupied sites, and do not interact with each other.

147 Another widely used Freundlich isotherm is shown in equation 5:

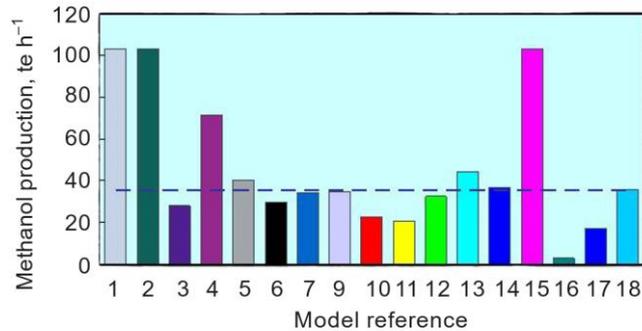
$$148 \quad q_e = K_F C_{equilibrium}^n \quad 5$$

149 where K_F is the adsorption constant and n is the empirical parameter. This model is
150 empirical; it often correctly describes adsorption over non-uniform surfaces but not the
151 saturation behaviour.

152 In performing a regression analysis of the experimental data, there are two potentially
153 conflicting aims: (i) to describe the system behaviour, or (ii) to gain mechanistic insights. The
154 mechanistic aim, obviously, requires rigour in the data analysis and independent validation
155 of the model assumptions. The descriptive aim seems deceptively simple. But the
156 descriptive models are often extrapolated beyond the studied range of parameters. In this
157 case, a careful analysis of the model and the data obtained becomes vital.

158 Correlation does not mean causation – people with umbrellas, although strongly correlating,
159 do not cause rain. A computationally accurate description of a particular isotherm (good fit)
160 does not show that the model is correct [31]. The model assumptions might not be fulfilled
161 resulting in unexpected behaviour beyond the studied range. Even if the model is correct,
162 the parameters obtained may be inaccurate resulting in unreliable extrapolations. Stitt at al.
163 [35] writes: “Just because the results are in colour, it doesn’t mean they are right” and
164 provides ample examples of totally inaccurate yet computationally valid model descriptions.

165 A minor mistake in the model may lead to dramatic changes in the extrapolated results [35].
166 The example in Fig. 2 shows the results of kinetic modelling of the same data with various
167 models. All of these models showed an excellent fit with the R^2 values above 95%, most
168 above 99%. The dashed line shows the “correct” data possible because the fitted data were
169 artificially generated from a known kinetic model. Despite an excellent fit in all the models,
170 the results are dramatically different - as much as 350% different!



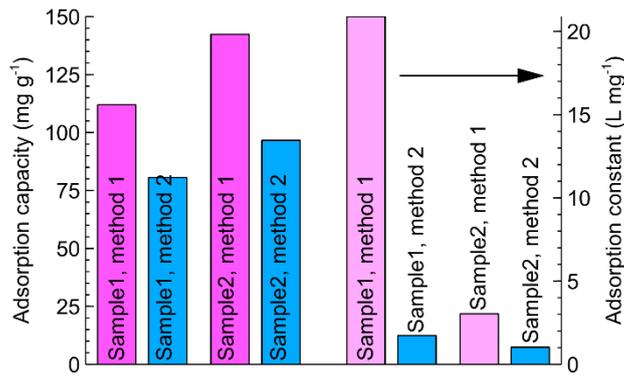
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172 Fig. 2. The discrepancy in various kinetic models of the artificially generated kinetic data
 173 (dashed line). Reprinted from ref. [35] which is based on the data obtained from ref. [36].

174

175 To avoid such poor results as in Fig. 2, the model must be validated by varying other
 176 parameters such as temperature/pressure dependence. In the case of gas-phase
 177 adsorption, Malek and Farooq [24] studied several models and compared the temperature
 178 behaviour and accuracy in describing the competitive adsorption. But the first step in
 179 assessing the model is to perform curve fitting and ensure that the parameters are well
 180 defined.

181 The confidence intervals are most often estimated using black-box computational packages
 182 that provide totally misleading data especially for non-linear models such as Langmuir
 183 isotherm. A conventionally used linearization approach, on the other hand, introduces
 184 additional errors and affects error estimates by imposing co-variation between parameters.
 185 Bolster and Hornberger [37] discuss that Langmuir linearization may lead even to
 186 computationally inaccurate results. A dramatic example is presented by Hamdaoui [38] who
 187 applied two Langmuir linearization methods to the experimental data and obtained
 188 dramatically different parameters. The differences between the Langmuir parameters
 189 obtained with 2 models ranged between -85% to +27%, while the goodness of fit was above
 190 98.5% in both cases. Goodness of fit is not sufficient!



191

192 Fig. 3. Parameters of a Langmuir isotherm fitted with two linearization methods for two
 193 samples. The figure is based on the data by Hamdaoui [38].

194 Supplementary SI2 takes adsorption parameters from ref. [39], generates sets of model
 195 datapoints with an introduced normally-distributed error and performs regression analysis
 196 using various methods. Not surprisingly, the results show that the non-linear Langmuir
 197 approach with proper error weighing (discussed below) provide results closest to the correct
 198 adsorption parameters. Disregarding error weights creates almost twice larger deviations
 199 from the correct values, while linearization methods often produce unreliable data.

200 **Proper curve fitting.** The regression analysis has to be done properly as the example in
 201 Fig. 3 demonstrates. The first step is to avoid linearization and use non-linear model
 202 equation combined with the estimated experimental analytical errors. That may sound
 203 difficult but proper regression is simple – it minimises the objective function (weighed
 204 residual) as shown in equation 6:

$$205 \quad f_{objective} = \sum_i \omega_i (q_{experiment,i} - q(C_i))^2, \quad 6$$

206 where $q_{experiment,i}$ are experimental adsorption datapoints, $q(C_i)$ the model values, and ω_i
 207 are the statistical weights of the i -th point. It is the weighing factor that makes a difference.

208 The weighting factors are calculated from the expected analytical uncertainties using
 209 equation 7, where σ_i is the uncertainty (standard deviation) in the analysis of datapoint i ,
 210 and ξ_i is the relative experimental error (typically 0.5 – 2 % = 0.005 – 0.02). A more general
 211 case of errors both in X and Y axes is shown in Supplementary SI1.

$$212 \quad \omega_i = 1/\sigma_i^2 = 1/(\xi_i q_{experiment,i}(C_i))^2 \quad 7$$

213 Considering that in most cases, the *relative* experimental errors are constant (except when
 214 close to the detection limit) [27,28], the objective function could be simplified as in equation 8

215 :

$$f'_{objective} = \sum_i \left(1 - \frac{q(C_i)}{q_{experiment,i}}\right)^2 .$$

8

217 Performing regression in most of the software packages (Origin, Excel) would result in the
 218 implicit assumption of constant *absolute* errors (rather than relative ones). As a result, high
 219 concentrations (with the corresponding high absolute errors) will be disproportionately well
 220 fitted and low concentrations may be, in effect, neglected. This approach of constant
 221 absolute errors combined with non-linear model may lead to worse results compared to
 222 unpredictable linearized approaches. The most reliable approach, however, is to use non-
 223 linear model with the objective function in equation 8. Supplementary SI2 elaborates on the
 224 inaccuracy of linearization models.

225 **Confidence intervals.** Once a proper curve fitting is performed, the next step is to study the
 226 confidence intervals. Likely the simplest and the most reliable way to perform such an
 227 analysis is to use the Monte-Carlo method described by Alper and Gelb [40] – the method
 228 that automatically accounts for co-variation in the model parameters. Many software
 229 packages generate some estimations on the confidence intervals but these may be grossly
 230 inaccurate [40].

231 The idea of the Monte-Carlo method is to generate a number (100-1000) of mock fitting data
 232 (experimental data plus random noise with the experimental standard deviation). These
 233 mock data are fitted and generate a set of model parameters. The statistics of the
 234 parameters obtained show the confidence intervals.

235 Broad confidence intervals show that the values cannot be relied upon and the model likely
 236 contains too many parameters. The widely used adsorption models contain only two
 237 parameters, but there are many models with as much as 5 parameters [24,26,41]. A larger
 238 number of parameters improves goodness of fit but makes all the parameters far less
 239 defined.

240 **4. Analysing thermodynamic parameters**

241 Any spontaneous process occurs because the system moves toward the minimum of the
 242 Gibbs's free energy, ΔG°_{ads} in equation 9. Considering that the adsorbate molecules move
 243 from the 3-dimensional freedom of the solution onto a 2-dimensional catalyst surface, the
 244 adsorption entropy (ΔS°_{ads}) often decreases. In this case, the adsorption enthalpy (ΔH°_{ads})
 245 must be negative for the adsorption to take place.

$$246 \Delta G^{\circ}_{ads} = \Delta H^{\circ}_{ads} - T \Delta S^{\circ}_{ads} .$$

9

247 The thermodynamic parameters of the adsorption are often obtained from the relation
 248 between the adsorption constant ($K_{equilibrium}$ in $L mol^{-1}$) and the Gibbs free adsorption energy
 249 (van't Hoff equation) 10. Here R is the universal gas constant and T is the adsorption
 250 temperature. The adsorption constant here could be either Langmuir or Freundlich constants
 251 in case of diluted solutions. More details on the ways to obtain the constant suitable for this
 252 equation are provided in reviews [42,43].

$$253 \quad \Delta G_{ads}^o = -RT \ln K_{equilibrium} \quad 10$$

254 **The problem of the dimensioned constant.** The Gibbs standard energy has dimensions of
 255 $J mol^{-1}$, the same as these of RT . Hence, the logarithm and the constant is dimensionless.

256 There is a controversy in how to resolve the misalignment of dimensions – $K_{equilibrium}$ must be
 257 dimensionless but the measured constant has the inverse units of concentration. There is a
 258 flurry of recent papers on the topic which argue on how to reconcile this problem of
 259 dimensions. First of all, both sides agree that the units of measured adsorption constant
 260 must be recalculated into $L mol^{-1}$, rather than keeping more exotic units such as $mg g^{-1}$.
 261 Such a simple matter is sometimes overlooked rendering results incorrect [26,42,44].

262 There is a hot disagreement, however, on the ways how to convert the dimensioned into the
 263 dimensionless constant. The problem comes from the value of the equilibrium adsorption
 264 constant shown in equation 11:

$$265 \quad K_{experimental} = \frac{\alpha_{A_adsorbed}}{\alpha_{A_in_solution} \alpha_{adsorbent}}. \quad 11$$

266 Here $K_{experimental}$ is the adsorption constant and α are the activities of the corresponding
 267 species: adsorbed compound A, compound A remaining in the solution at equilibrium, and
 268 the adsorbent itself. The equation could be simplified considering activity coefficients 1
 269 (which is valid for non-ionic and diluted ionic solutions [42,45]) and considering the Langmuir
 270 model the equilibrium coverage of θ . The resulting equation 12 shows the origin of the
 271 dispute – the constant determined experimentally has units of inverse concentration.

$$272 \quad K_{experimental} = \frac{\theta}{C_{A_in_solution} (1-\theta)}. \quad 12$$

273 Both sides of the dispute agree that the problem shall be resolved by multiplying the
 274 experimental constant (in $L mol^{-1}$) by a certain coefficient (in $mol L^{-1}$) that renders the product
 275 dimensionless. The value of the coefficient is disputed.

276 On one side, Milonjić [46] and Tran et al. [26,45] suggests multiplication by 55.5 mol L⁻¹. This
277 constant is a concentration of water in the solution. Zhou and Zhou [45] provide a detailed
278 proposition explaining that the constant of 55 mol L⁻¹ comes from considering adsorption
279 competition between the adsorbate and the solvent.

280 On the opposite side, Liu [47], Ghosal and Gupta [42] provide reasons that the constants
281 shall be multiplied by 1 mol L⁻¹. The reasoning comes from the description of thermodynamic
282 constants in terms of activities, not concentrations. The activity of component A is shown in
283 equation 13:

$$284 \quad \alpha_A = \gamma_A \frac{C_A}{C_{ref}}, \quad 13$$

285 where γ_A is the activity coefficient, C_A is the concentration of the adsorbed specie in mol
286 L⁻¹, and C_{ref} is the concentration of the reference state equal to 1 mol L⁻¹ [42].

287 The reader is advised to read papers from both sides of the argument (in particular papers
288 by Ghosal and Gupta [42], and Zhou and Zhou [45]) to form a coherent picture. In the
289 current review the author, however, offers additional reasoning that may clarify the dispute.
290 There are two points that both lead to the same conclusion on resolving the dispute.

291 The first point is that the same problem of dimensioned adsorption constants shown in
292 equation 12 equally applies to gas phase, but there is no disagreement there. The gas-
293 phase adsorbate concentrations may be presented in the units of in mol L⁻¹, or even mol
294 mol⁻¹ (molar fraction of adsorbate in gas phase). More conventionally, however, pressure is
295 used as a measure of adsorbate activity rendering the corresponding experimental constant
296 in bar⁻¹. This difference between the gas and liquid phases, however, shows that rendering
297 the *concentration itself* dimensionless (using mole fraction) makes little sense. In liquid
298 phase, multiplication of the constant by 55.5 mol L⁻¹ renders, in effect, concentrations
299 dimensionless molar fractions. The reason is that using mole fractions does not explain the
300 increasing adsorption at a higher pressure. If we double pressure, we expect higher
301 adsorption. If we consider molar fraction (that is 1 regardless of pressure) we would struggle
302 explaining the difference in adsorption. Hence, the experimentally determined adsorption
303 constant must be dimensioned in gas and liquid phases.

304 The second point comes from the analysis of how the problem of dimensioned constants
305 could affect the resulting Gibbs energy assuming for the argument's sake the possibility of
306 logarithmic Joule as a physical unit. Equation 14 explicitly states the constant \mathcal{J} required to
307 make the experimental constant dimensionless:

308
$$\Delta G_{ads}^{\circ} = -RT \ln (\mathcal{G} K_{experimental}) = -RT \ln \mathcal{G} - RT \ln K_{experimental} .$$
 14

309 Considering the arithmetic of logarithms, equation 14 shows that such constant \mathcal{G} simply
310 provides an offset to the determined Gibbs energy of $-RT \ln \mathcal{G}$. The corresponding offset
311 affects the absolute value of the Gibbs energy we observe. Considering equation 9, this
312 offset translates to an offset in the value of the adsorption enthalpy but does not affect the
313 adsorption entropy which depends on the slope in the G vs T plot.

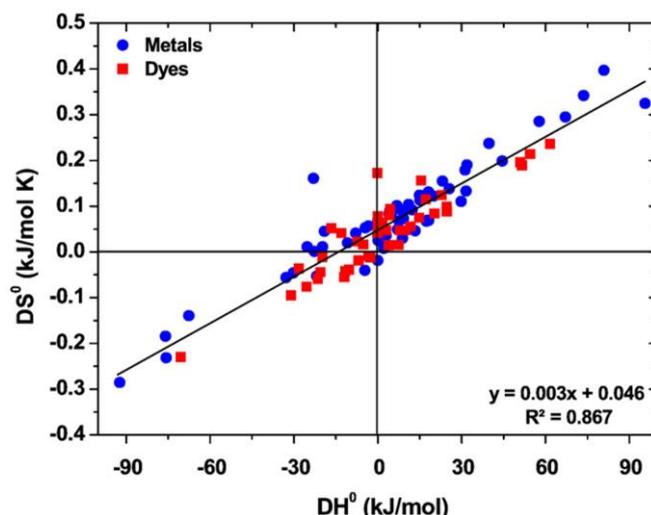
314 This consideration implies that the absolute value of the Gibbs energy, as well as enthalpy,
315 cannot be determined, while that of entropy could be. Such a trivial statement,
316 unsurprisingly, agrees with thermodynamics – the existence of absolute values of entropy
317 and only relative values of enthalpy. For simplicity, enthalpy is often referred to certain
318 reference states as elements stable under normal temperature and pressure.

319 The standard conditions for gases, defined by IUPAC, are the temperature of 0 °C and a
320 pressure of 1 bar. Hence, all gas-phase adsorption constants are calculated in terms of bar⁻¹
321 with the (often implied) “dimensionalisation” constant \mathcal{G} of 1 bar [48]. In liquid phase, the
322 standard IUPAC state is for a solute at a concentration of 1 mol dm⁻³ rendering the required
323 “dimensionalisation” constant \mathcal{G} of 1 dm³ mol⁻¹ [48]. Therefore, the correct way of calculating
324 the thermodynamic parameters from the liquid-phase adsorption data is shown in equation
325 15:

326
$$\Delta G_{ads}^{\circ} = -RT \ln (K_{experimental} [in L mol^{-1} for diluted solutions]).$$
 15

327 **Analysis of adsorption thermodynamics.** If the Gibbs adsorption energy obtained is
328 negative, the adsorption is often said to occur “spontaneously” [26,41,42,44,46]. However,
329 the “spontaneous” does not mean “occur”. A small but negative value of the Gibbs free
330 energy shows that the equilibrium constant is below 1 (equation 10). This note may be of
331 little practical value for the design of pollutant adsorbents that must strongly adsorb to be
332 useful. For the catalytic applications, however, both too high and too low adsorption
333 constants are obstacles for the reaction. An “optimal” adsorption constant (that provides the
334 highest reaction rate) might be below 1, the Gibbs adsorption energy may conceivably be
335 positive.

336 Having the Gibbs adsorption energy determined, the adsorption enthalpy and entropy may
337 be obtained using equation 9 by studying adsorption at various temperatures. Such a
338 derivation, albeit trivial, raises an interesting question of correlation between the parameters
339 derived. Anastopoulos and Kyzas in their review [44] show a strong correlation between the
340 thermodynamic parameters obtained in the literature (Fig. 4) and call for alternative and
341 independent ways to validate the parameters.



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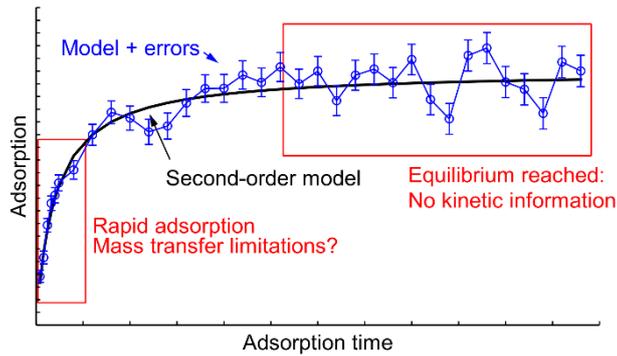
343 Fig. 4. Correlation between the adsorption entropy and enthalpy observed for the dyes and
 344 metal ions over various materials. The picture is reprinted from review [44].

345 The observed values of adsorption entropies and enthalpies can fall into 4 major groups
 346 depending on if they are positive or negative. Fig. 4 shows that the more prevalent are cases
 347 with exothermic adsorption with a negative adsorption enthalpy; and endothermic reactions
 348 with the increasing entropy. However, all the cases are realised in the literature [41]

349 5. Adsorption kinetics

350 The adsorption kinetics are often studied using similar approaches as thermodynamics; the
 351 only difference is the analysis in the adsorbate concentration change over time. The data
 352 obtained are fitted to a model. Similarly to thermodynamics, fitting shall benefit from using
 353 non-linearized equation to account for changing *absolute* experimental errors (and often
 354 constant *relative* experimental errors). (Equation 8 provides the way to calculate fitting
 355 residuals in such a case). The uncertainty intervals of the model parameters obtained shall
 356 be checked using Monte-Carlo.

357 A particular consideration for kinetics is the required analysis duration. Fig. 5 shows
 358 computer-generated adsorption data based on pseudo-second order kinetics with the
 359 analytical uncertainty of 3% (Supplementary SI3). Once the equilibrium is reached, the
 360 concentration does not change and the data points characterise the adsorption
 361 thermodynamics, not kinetics. Hence, taking too many of these points into regression may
 362 introduce unnecessary errors into the parameters determined; in the best case, these points
 363 are valueless.



364

365 Fig. 5. Computer-generated data for pseudo-second order adsorption model with an
 366 experimental error at 3% (standard deviation) analytical uncertainty. The initial region may
 367 be limited by mass transfer; the equilibrium region contains no kinetic information.

368 While analysing adsorption kinetics, similar to reaction kinetics, one needs to study if the
 369 external mass transfer is not the rate-limiting factor. Otherwise, the data will reflect the rate
 370 of stirring rather than intrinsic adsorption. A simple way to check for external mass transfer is
 371 to perform experiments at various stirring rates and observe rates of adsorption constant
 372 above a certain stirring rate. However, many small reactors show minor changes in the
 373 Reynolds number in a broad stirring rate and may provide misleading results [49]; too high
 374 rotation rate, however, may decrease mass transfer [50]. Hence, a comparison of smaller
 375 and larger stirrers, possibly impellers, may be carried out for the test [51].

376 Internal mass transfer – the diffusion of the adsorbate molecules into the pores may often be
 377 a rate-limiting factor. In this case, the researcher may either look for the intrinsic rates of
 378 adsorption that requires studies with smaller adsorbent particles or using wall coatings
 379 [14,52,53]. Often, however, it is more practically important to characterise the apparent rates
 380 – in effect, internal mass transfer because such data characterises the behaviour of the
 381 adsorbents in many practical applications. The examples include adsorption of metal ions
 382 and dyes over chitosan (lobster shell waste) [21] and similar agricultural waste materials that
 383 have low porosity [32,54].

384 There are 3 most widely models used for describing the adsorption kinetics: pseudo first or
 385 second order, and internal diffusion. A wider range of adsorption models and equations are
 386 discussed by Qiu et al. [54].

387 Pseudo first or second order models treat adsorption in terms of a corresponding order
 388 chemical reaction with rate equations shown in equations 16 and 17:

389
$$\frac{dq(t)}{dt} = k_1(q_{equilibrium} - q(t)); q(t) = q_{equilibrium}(1 - \exp(-k_1t)),$$
 16

$$390 \quad \frac{dq(t)}{dt} = k_2(q_{equilibrium} - q(t))^2; q(t) = \frac{q_{equilibrium}^2 k_2 t}{q_{equilibrium} k_2 t + 1}, \quad 17$$

391 where k are apparent adsorption rate constants, $q(t)$ is the adsorption at the moment of t
 392 and $q_{equilibrium}$ is the equilibrium adsorption. These equations are often linearized, which as
 393 discussed above, may introduce unpredictable errors into the parameters obtained by
 394 regression (Fig. 3).

395 The other commonly used model considers intra-particle diffusion as the rate-limiting step.
 396 The adsorbent is considered homogeneous spheres with the mass transfer determined by
 397 equation 18 [54,55]:

$$398 \quad \frac{\partial q(t,r)}{\partial t} = \frac{D_s}{r^2} \frac{\partial}{\partial r} \left(r^2 \frac{\partial q(t,r)}{\partial r} \right), \quad 18$$

399 where q is the adsorption at the moment t and radial position in the particle r , D_s is the
 400 intra-particle diffusion coefficient. This equation could be solved and simplified to obtain
 401 equation 19:

$$402 \quad q(t) = q_{equilibrium} \cdot 6 \sqrt{\frac{D_s}{\pi R^2}} \sqrt{t}, \quad 19$$

403 where $q_{equilibrium}$ is the equilibrium adsorption and R is the particle radius. Such an
 404 approximation is valid for $q(t) / q_{equilibrium} < 0.3$ [54,55].

405 **6. Conclusions**

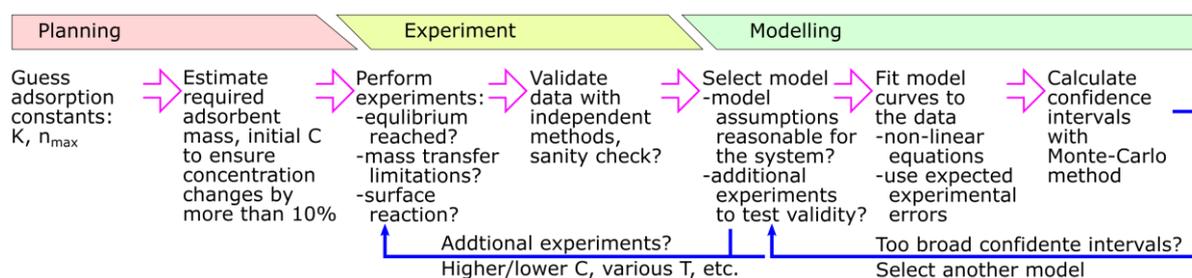
406 The review discusses experimental approaches, modelling to obtain thermodynamic, and
 407 kinetic parameters of adsorption. The suggested workflow is schematically presented in Fig.
 408 6.

409 The planning steps involve assuming or estimating the adsorption constant; calculating the
 410 adsorbent mass and adsorbate concentrations to ensure that the measured adsorption could
 411 provide the desired accuracy. Reasonable accuracy is expected if the initial concentration
 412 changes by at least 10% relative to the initial concentration; otherwise the experimental
 413 errors would make results unusable (Fig. 1).

414 The experiment steps involve adsorption measurements and assessing the data with
 415 alternative methods to exclude the possibility of false readings caused by side-phenomena
 416 other than adsorption. An always advisable sanity check may involve comparing the

417 adsorption data with the known properties of the material such as overall surface area or
418 adsorption site stoichiometry.

419 The modelling steps include selecting the adsorption model, curve fitting of the experimental
420 data using the original non-linear equations, and considering experimental errors. The fitting
421 objective function may be the one shown in equation 8 – the function that assumes constant
422 relative errors in adsorption and no errors in the X axis values. Confidence intervals of the
423 model parameters shall be calculated for mathematical sanity of the model using the Monte-
424 Carlo approach [40]. Linearized models provide less predictable and often outright
425 inaccurate results as shown in Supplementary SI2. Such calculations may be performed
426 using the Matlab code for the Langmuir model; a standalone executable freely available at
427 ref. [56].



428

429 Fig. 6. Proposed workflow for adsorption experiments and analysis.

430 These steps allow obtaining mathematically reasonable results and assess the goodness of
431 fit for the model selected. However, a good fit of the model and narrow confidence intervals
432 do not validate the underlying model assumptions. If the modelling aims to probe into the
433 adsorption mechanisms, the model assumptions must be checked independently. If the
434 model aims only for a description of the experimental data, particular attention shall be given
435 on the range of studied conditions, extrapolation beyond the conditions would likely produce
436 unreliable data.

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