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Abstract—Due to the agile maneuverability, unmanned aerial vehicles (UAVs) have shown great promise for on-demand communications. In practice, UAV-aided aerial base stations are not separate. Instead, they rely on existing satellites/terrestrial systems for spectrum sharing and efficient backhaul. In this case, how to coordinate satellites, UAVs and terrestrial systems is still an open issue. In this paper, we deploy UAVs for coverage enhancement of a hybrid satellite-terrestrial maritime communication network. Using a typical composite channel model including both large-scale and small-scale fading, the UAV trajectory and in-flight transmit power are jointly optimized, subject to constraints on UAV kinematics, tolerable interference, backhaul, and the total energy of the UAV for communications. Different from existing studies, only the location-dependent large-scale channel state information (CSI) is assumed available, because it is difficult to obtain the small-scale CSI before takeoff in practice and the ship positions can be obtained via the dedicated maritime Automatic Identification System. The optimization problem is non-convex. We solve it by using problem decomposition, successive convex optimization and bisection searching tools. Simulation results demonstrate that the UAV fits well with existing satellite and terrestrial systems, using the proposed optimization framework.

Index Terms—Hybrid satellite-terrestrial network, maritime communications, power allocation, trajectory, unmanned aerial vehicle (UAV).

I. INTRODUCTION

Currently, the increase of activities on the ocean has promoted great demand for wireless communications [1]–[3]. To satisfy the increasing requirements, hybrid satellite-terrestrial networks have emerged, in which satellites and terrestrial systems are integrated for maritime coverage enhancement [4]–[6]. Basically, the satellites, deployed in the Geostationary Earth Orbit or Low Earth Orbits, can provide a wide-area coverage [7]. However, their transmission rate is usually limited due to long transmission distance and restricted onboard payloads. High-throughput satellites have thus attracted great attentions [8]. Yet, it is still quite challenging to realize the global broadband coverage using the state-of-the-art satellite technologies at a practically affordable cost. As an alternative, terrestrial base stations (TBSs) can be deployed along the coast to offer high-rate communication services. However, their coverage range is usually limited.

Different from satellites and TBSs, unmanned aerial vehicles (UAVs) have shown considerable promise for agile communications [9], [10]. UAVs can enable aerial base stations with largely increased line of sight (LOS) transmission range. Moreover, UAVs can adaptively change their spatial locations according to the communication demands. While most existing studies on UAVs focused on the terrestrial scenario, we explore the potential gain of UAVs for maritime coverage enhancement in this paper. Particularly, we focus on the coordination issue between UAVs and existing maritime satellites/terrestrial systems. Related works can be summarized into three categories according to their system models, which are discussed as follows.

1) UAVs only: Most previous works focused on the UAV-only system model, while ignoring satellites and TBSs. For rotary-wing UAVs, the optimal placement of UAVs has been widely investigated, leading to many insightful observations [11]–[18]. In [12] and [13], the optimal altitude was analyzed in terms of area spectral efficiency and outage probability, respectively. In [14], the transmit power and the bandwidth were jointly optimized for achieving maximum throughput. In [15] and [16], the deployment of multiple UAVs was comprehensively investigated to ensure the coverage with a minimum number of UAVs. In addition, the authors of [16] have also skillfully addressed the problem of the latency-minimal 3D cell association among UAVs.

For fixed-wing UAVs, the trajectory design is an important issue, which is closely related to the UAV’s kinematic parameters [19]–[24]. Considering the UAV’s maximum velocity, the trajectory of the UAV was optimized for achieving maximum throughput and minimum UAV periodic flight duration in [19]–[21]. Furthermore, considering the UAV’s maximum acceleration, the trajectory optimization for the UAV was investigated for energy efficiency in [22], [23]. These works [11]–[24] mainly considered static users. For mobile users, the ergodic achievable rate was maximized by dynamically adjusting the UAV heading [25]–[27]. Intuitively in the maritime scenario, the UAV trajectory should adaptively cater to the mobility of ships, providing an accompanying
broadband coverage, which however remains elusive.

2) Coexistence of UAVs and TBSs: In addition to UAV-only models, the coexistence of UAVs and TBSs was investigated in [28]–[33]. The TBS can be used as a hub to connect rotary-wing UAVs to the network [28]. In this case, the access link and the backhaul link should be jointly optimized to maximize the sum rate. In [29], the UAV-based multi-hop backhaul network was formulated to adapt to the dynamics of the network. In [30], solar powered UAVs were investigated and the network’s energy consumption was minimized by determining whether UAVs were needed and the number of UAVs to be used. Outage probability is also an important issue for the coexistence of UAVs and TBSs [31]–[33]. In [33], the throughput was maximized subject to the maximum outage probability constraint. For the maritime scenario, the TBS is the primary choice for UAV backhaul due to their high-speed transmission rate.

3) Coexistence of UAVs and Satellites: More recently, the integration of UAVs and satellites has been investigated in [34]–[39]. Particularly, the authors of [36] investigated the integration of satellite and UAV communications for heterogeneous flying vehicles. In addition, the long transmission delay is quite challenging for satellites. Thus, the impact of UAV altitude on the average delay was analyzed to coordinate UAVs and satellites in [37]. A multi-UAV assisted network was formulated in [38], where the coverage probability and the ergodic achievable rate were analyzed for post-disaster areas. The airborne mobile wireless networks were considered in [39], where an efficient power allocation scheme was proposed to support the diverse real-time services.

Despite of the aforementioned works, there remain open problems in the integration of UAVs into hybrid satellite-terrestrial maritime communication networks. Firstly, to solve the spectrum scarcity problem, it is valuable to explore the potential of spectrum sharing among satellites, UAVs and terrestrial networks. Till now, spectrum sharing between satellites and terrestrial networks has been studied [43]–[45]. For more complicated spectrum sharing among satellites, UAVs and terrestrial networks, it is crucial to obtain the channel state information (CSI) for interference mitigation. Both the large transmission delay via satellites and the mobility of UAVs and ships render this challenging. This problem has never been investigated in existing studies. Secondly, the real-time UAV planning has been widely studied, for which the UAV was deployed to cover the entire area or for maximum coverage [11], [14], [16], [38]. During the transmission, the position, the heading angle or resources for the UAV were dynamically optimized to improve the quality of service [7], [8], [16], [18], [25]–[28]. However, the UAV cannot land on the sea surface and replenish energy on the sea surface. Instead, the UAV has to wait on the coast. According to the communication demand, the UAV journeys between the position on the coast and that on the ocean for covering the mobile user. In this case, the UAV’s positions on the ocean should be designed before the UAV takes off. Specially, the distance between the position on the coast and that on the ocean is large, which leads to a long flight time. To avoid this issue, the pre-deployment of the UAV should be investigated, for which a whole trajectory of the UAV is planned for coverage enhancement according to the mobility of the user before the UAV takes off and then the UAV is pre-deployed with the designed trajectory. However, the limited capacity of wireless backhaul affects the real-time transmission and the energy for communications at UAVs is also limited due to battery life. These constraints should be considered in the optimization of UAV trajectory. Besides, different from most previous works which use the free space path loss model to simplify analysis, it is more practical to consider both large-scale and small-scale fading [46], [47]. However, it is difficult to acquire the random small-scale fading before takeoff [48]. Thus, we propose a new method that only uses the large-scale CSI in UAV trajectory design.

Motivated by the above observations, we investigate a hybrid satellite-UAV-terrestrial maritime communication network where UAVs are integrated for coverage enhancement. Considering the severe environment on the ocean, we consider the fixed-wing UAV, which has longer duration of flight and stronger anti-wind capability than the rotary-wing UAV. A typical composite channel model including both large-scale and small-scale fading is used. We obtain the ship positions from the dedicated maritime Automatic Identification System. Accordingly, different from the terrestrial scenario, we assume that only the large-scale CSI is available before the UAV takes off. The main contributions are summarized as follows.

1) In our work, UAVs share the spectrum with satellites and utilize TBSs or satellites as wireless backhaul. In [43]–[45], the spectrum sharing was investigated only considering satellites and TBSs. We further integrate UAVs into this system and focus on the new challenges of achieving the CSI for interference mitigation.

2) Because the large-scale CSI is location dependent, we can obtain it using historical or pre-measured data on the ocean. We optimize the whole trajectory and transmit power during the fight, subject to the UAV’s kinematical constraints, the backhaul constraints, tolerable interference constraints and the communication energy. In [11]–[39], the trajectory design and resource allocation were investigated using perfect CSI at all scales. We consider the issue caused by pre-deploying UAVs above the sea surface and solve the issue using the large-scale CSI.

3) The optimization problem is non-convex. We decompose the problem and solve it by using successive convex optimization and bisection searching tools. Simulation results demonstrate that the UAV fits well with existing satellite and terrestrial systems. Besides, a significant performance gain can be achieved via joint optimization of the UAV trajectory and transmit power by using only the large-scale CSI.

The rest of this paper is organized as follows. In Section II, the system model is introduced. The problem for the UAV-aided coverage enhancement is formulated and solved in Section III. In Section IV, simulation results are presented. Section V concludes the paper.

Throughout this paper, vectors and scalars are denoted by boldface letters and normal letters, respectively. | · | indicates
TABLE I
MAIN NOTATIONS.

<table>
<thead>
<tr>
<th>Notation</th>
<th>Meaning</th>
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<tbody>
<tr>
<td>U, F, Ξ</td>
<td>Set of UAVs, TBSs and satellites connected to UAVs, respectively</td>
</tr>
<tr>
<td>Ψ</td>
<td>Set of users served by UAVs</td>
</tr>
<tr>
<td>Sv</td>
<td>Set of satellites sharing the same frequency with the u-th UAV</td>
</tr>
<tr>
<td>Ch</td>
<td>Transmit power of the u-th UAV</td>
</tr>
<tr>
<td>γt</td>
<td>Ergodic achievable rate between the u-th UAV and its user in Ψ at time t</td>
</tr>
<tr>
<td>εt, u</td>
<td>Ergodic achievable rate between the u-th UAV and the γ-th TBS at time t</td>
</tr>
<tr>
<td>ρu,v,t</td>
<td>Ergodic achievable rate between the ε-th satellite in Ξ and the u-th UAV at time t</td>
</tr>
<tr>
<td>L  thượng</td>
<td>Channel and path loss between the u-th UAV and its user in Ψ at time t, respectively</td>
</tr>
<tr>
<td>L  thượng</td>
<td>Channel and path loss between the u-th UAV and the α-th user in Oα at time t, respectively</td>
</tr>
<tr>
<td>L  thượng</td>
<td>Channel and path loss between the γ-th TBS and the u-th UAV at time t, respectively</td>
</tr>
<tr>
<td>L  thượng</td>
<td>Channel and path loss between the ε-th satellite in Ξ and the u-th UAV at time t, respectively</td>
</tr>
<tr>
<td>L  thượng</td>
<td>Channel and path loss between the ε-th satellite in Ξ and the u-th UAV at time t, respectively</td>
</tr>
<tr>
<td>P  thượng</td>
<td>Transmit power of the u-th UAV and the γ-th TBS at time t, respectively</td>
</tr>
<tr>
<td>P  thượng</td>
<td>Transmit power of the s-th satellite in Sv and the ε-th satellite in Ξ at time t, respectively</td>
</tr>
<tr>
<td>Gθ, GΩ</td>
<td>Antenna gain of users served by UAVs and users served by satellites, respectively</td>
</tr>
<tr>
<td>GΩ, GΨ, GΞ</td>
<td>Antenna gain of UAVs, TBSs, and satellites, respectively</td>
</tr>
<tr>
<td>ξΩ, ξΞ</td>
<td>Path-loss exponent for the UAV-to-ground link and the satellite-to-ground link, respectively</td>
</tr>
<tr>
<td>AΩ, AΞ</td>
<td>Path loss at dΘ for the UAV-to-ground link and the satellite-to-ground link, respectively</td>
</tr>
<tr>
<td>cψ,v,t</td>
<td>Position vector of the u-th UAV and the γ-th TBS at time t, respectively</td>
</tr>
<tr>
<td>cψ,v,t</td>
<td>Position vector of the u-th user in Ψ and the α-th user in Oα at time t, respectively</td>
</tr>
<tr>
<td>Ψ</td>
<td>Velocity vector of users in Ψ at time t</td>
</tr>
<tr>
<td>vmax, vmin</td>
<td>Maximum velocity, minimum velocity</td>
</tr>
<tr>
<td>cmax, cmin</td>
<td>Maximum height, minimum height</td>
</tr>
<tr>
<td>Ω</td>
<td>Maximum acceleration</td>
</tr>
<tr>
<td>P  thượng</td>
<td>Maximum transmit power of UAVs</td>
</tr>
<tr>
<td>τ0</td>
<td>Travel time during which a UAV serves a mobile user</td>
</tr>
<tr>
<td>E0</td>
<td>Allowable communication energy</td>
</tr>
<tr>
<td>I0</td>
<td>Interference temperature limitation</td>
</tr>
<tr>
<td>K</td>
<td>Rician factor</td>
</tr>
<tr>
<td>h</td>
<td>Rician fading</td>
</tr>
</tbody>
</table>

the absolute value of a scalar or the cardinality of a set. Transpose operator is indicated with $[\cdot]^T$. l_p-norm means $\|x\|_p = \left( \sum_{i=1}^{n} |x_i|^p \right)^{1/p}$. $CN(0, \sigma^2)$ represents the complex Gaussian distribution with zero mean and $\sigma^2$ variance. $\hat{x}_t$ and $\ddot{x}_t$ denote the first-order and second-order derivatives of $x_t$ with respect to $t$. $E[\cdot]$ denotes the expectation operator. Main notations are summarized in Table I.

II. SYSTEM MODEL

We consider a practical hybrid maritime network consisting of mobile users (ships), UAVs, TBSs and satellites, as shown in Fig. 1. The TBSs are deployed along the coast to provide communication services for users in the area of coastal waters. The broadband coverage area of TBSs is usually limited due to large non-line-of-sight pathloss. Out of the coverage area of TBSs, the maritime satellites provide communication links. For the ships equipped with expensive high-gain antennas, the broadband service can be guaranteed. Whereas for the low-end ships without high-gain antennas, it is still difficult to enjoy a broadband service even within the coverage area of satellites. To fill up this gap, we utilize UAVs to provide broadband services in an on-demand manner. More specifically, if a mobile user needs a high-rate communication service (e.g., a video conference) from $t_s$ to $t_e$, the communication request will be sent from the mobile user to its nearest TBS and then transmitted to the central processor. The central processor selects one idle UAV and prepares the idle UAV to serve the mobile user. After the idle UAV is sent, the mobile user will be associated to the idle UAV at time $t_s$. The UAV will fly along the optimized trajectory to serve the user from time $t_s$ to time $t_e$. After finishing the high-rate communication service, the mobile user will be associated to its nearest TBS at time $t_e$ and the UAV will go back to the coast.

In this paper, the spectrum is shared between UAVs and satellites. Thus, there may be interference between the UAV-to-user link and the satellite-to-user link. Because the antenna gain of users served by UAVs is lower than that of users served by satellites, the interference on users served by UAVs from satellites can be ignored. Besides, interference management and user association among UAVs are important for improving the quality of service, which have been comprehensively investigated in [40]–[42]. Due to the space limitation, we
simplify the system model to concentrate on spectrum sharing between UAVs and satellites. We assume that, from \(t_1\) to \(t_2\), a user is connected to one UAV and the UAV only serves one user. Moreover, only a few users are served by UAVs and thus UAVs are sparsely distributed on the immense ocean. To avoid the interference between UAVs, orthogonal resources, e.g., different subcarriers or different time slots, have been used before UAVs take off. Then, to mitigate the leakage interference on users served by satellites, we jointly adjust the trajectory and the transmit power of UAVs.

To serve the mobile users on the ocean, UAVs need the wireless backhaul. Both TBSs and satellites can be used. As shown in [36], when UAVs are close to the mainland, the air-to-ground backhaul is able to provide enough capacity. In this case, TBSs nearest to UAVs can be utilized to connect UAVs to the central processor. Otherwise, satellites are used instead. Note that UAVs have limited energy. Generally, UAVs fly close to the coast and are mainly served by TBSs. In this paper, we focus on the TBS-assisted backhaul but also study the satellite-assisted backhaul.

We assume that autonomous UAVs are employed as aerial base stations and both UAVs and users served by UAVs are equipped with a single antenna. Let \(U\) and \(\Psi\) denote the set of UAVs and the set of users served by UAVs, respectively. In this paper, each UAV only serves one user and thus \(|U| = |\Psi|\). Let \(T_0\) be the travel time from \(t_1\) to \(t_2\) during which the \(u\)-th UAV serves its user. At time \(t\), the signal transmitted from the \(u\)-th UAV is denoted as \(b_{u,t}^U\) and the received signal of the user served by the \(u\)-th UAV can be expressed as

\[
q_{u,t}^\Psi = P_{u,t}^U G_U h_{u,u,t}^\Psi b_{u,t}^U + e_{u,u,t}^\Psi
\]

where \(0 \leq t \leq T_0\), \(P_{u,t}^U\) denotes the transmit power of the \(u\)-th UAV, \(G_U\) denotes the antenna gain of UAVs, \(G_\Psi\) denotes the antenna gain of users served by UAVs, \(h_{u,u,t}^\Psi\) denotes the channel between the \(u\)-th UAV and its user, and \(e_{u,u,t}^\Psi\) denotes the White Gaussian noise.

We assume that UAVs are high enough to enable LOS transmission. A typical composite channel containing both large-scale and small-scale fading is employed. The channel between the \(u\)-th UAV and its user at time \(t\) can be represented as

\[
\tilde{h}_{u,u,t}^U,\Psi = \left( \frac{L_{u,u,t}^U}{d_{u,u,t}^{U,\Psi}} \right)^{-1/2} h_{u,u,t}^U,\Psi
\]

where \(L_{u,u,t}^U\) denotes the path loss and \(h_{u,u,t}^U,\Psi\) denotes Rician fading during the information transmission. Let \(d_{u,u,t}^{U,\Psi}\) denote the distance between the \(u\)-th UAV and its user at time \(t\). We assume the earth surface to be smooth and flat. Then, the path loss model can be expressed as

\[
L_{u,u,t}^{U,\Psi} (\text{dB}) = A_U + 10 \zeta_U \log d_{u,u,t}^{U,\Psi} + X_{u,u,t}^{U,\Psi}
\]

where \(d_0\) denotes the reference distance, \(A_U\) denotes the path loss at \(d_0\), \(\zeta_U\) denotes the path-loss exponent, and \(X_{u,u,t}^{U,\Psi}\) is a zero-mean Gaussian random variable with standard deviation \(\sigma_X\) [50]–[52]. Rician fading can be represented as

\[
h_{u,u,t}^{U,\Psi} = \sqrt{\frac{K_U}{1 + K_U}} + \sqrt{\frac{1}{1 + K_U}} g_{u,u,t}^{U,\Psi}
\]

where \(g_{u,u,t}^{U,\Psi} \sim \mathcal{C}(0, 1)\) and \(K_U\) indicates the Rician factor that corresponds to the ratio between the LOS power and the scattering power [53]–[56]. On the ocean, ships normally travel along the fixed shipping routes and then the historical or

\[1\] If the distances are shorter than a few tens of kilometers, it is often permissible to neglect earth curvature and assume the earth surface to be smooth and flat [49].
pre-measured data can be derived. We can use the derived data to obtain the relationship between the location and the large-scale CSI. By using this relationship, the corresponding large-scale CSI per location can be obtained. Thus, we assume that path loss $L_{\text{path}}$, and Rician factor $K_U$ are available, whereas $g_{u,t}^{\text{U}}, g_{r,t}^{\text{R}}$ is unknown. The ergodic achievable rate $R_{u,t}^{\text{U},\Psi}$ between the $u$-th UA V and its user at time $t$ can be derived as

$$R_{u,t}^{\text{U},\Psi} = \mathbb{E} \left\{ \log_2 \left( 1 + \frac{P_u^{\text{U}} G_u G_\Psi \left| h_{u,t}^{\text{U},\Psi} \right|^2}{\sigma^2} \right) \right\}$$

(5)

where $\sigma^2$ denotes noise power. The expectation is taken over the small-scale fading.

By substituting (2) and (3) into (1), the received signal of the user served by the $u$-th UA V can be rewritten as

$$d_{u,t}^{\text{U}} = P_{u,t}^{\text{U}} W_{u,t}^{\text{U},\Psi} \left( \sigma_i^{\text{U},\Psi} \right)^{-\alpha_i^{\text{U}}/2} h_{u,t}^{\text{U},\Psi} b_{u,t}^{\text{U}} + e_{u,t},$$

(6)

where $W_{u,t}^{\text{U},\Psi} = G_u G_\Psi d_0^{\text{U}/2} 10^{-\frac{L_{\text{path}}^{\text{U},\Psi}}{10}}$ is known, $P_{u,t}^{\text{U}}$ and $d_{u,t}^{\text{U},\Psi}$ need to be determined. Considering the user mobility, our aim is to maintain certain achievable rate to avoid severe performance degradation during the travel time. Before the $u$-th UA V is deployed, the trajectory and the transmit power of the $u$-th UA V are optimized to maximize the minimum ergodic rate during the whole travel time $T_0$. After the $u$-th UA V is sent out, the $u$-th UA V serves the mobile user according to the optimized trajectory and transmit power.

III. UAV-AIDED COVERAGE ENHANCEMENT

In this section, we formulate the optimization problem of the UAV trajectory and in-flight transmit power and provide an iterative algorithm to solve the optimization problem.

A. Problem Formulation

The set of TBSs is denoted as $\Gamma$. We assume that the $\gamma$-th TBS receives the high-rate communication request from a mobile user and then starts to send the $u$-th UA V. During the travel time $T_0$ of the $u$-th UA V, the $\gamma$-th TBS is nearest to the mobile user among TBSs and provides wireless backhaul for the $u$-th UA V. We consider a three-dimensional Cartesian coordinate system, in which the $\gamma$-th TBS is located at $\mathbf{e}_\gamma^T = (0, 0, z_\gamma)$. The positions of the $\gamma$-th TBS and its user at time $t$ are respectively denoted as $\mathbf{e}_\gamma^{\text{U},t} = [x_{\gamma,t}^{\text{U}}, y_{\gamma,t}^{\text{U}}, z_{\gamma,t}^{\text{U}}]^T$ and $\mathbf{e}_t^{\text{U},t} = [x_{u,t}^{\text{U}}, y_{u,t}^{\text{U}}, z_{u,t}^{\text{U}}]^T$. We discretize the travel time $T_0$ into $T$ time slots with a step size $\Delta t$. We adjust the trajectory and the transmit power of the $u$-th UA V per time slot. We assume that UAVs and users on the ocean move under the law of uniformly accelerated rectilinear motion during $\Delta t$. Moreover, $\Delta t$ is small enough so that an exact trajectory of UAVs can be obtained and the large-scale channel is assumed to remain the same during $\Delta t$.

The set of satellites sharing the same frequency with the $u$-th UA V are denoted as $S_u$. The set of users served by satellites and interfered by the $u$-th UA V is denoted as $O_u$. To simplify the analysis, we assume that satellites and their users are equipped with a single antenna. Without loss of generality, we assume that one user served by a satellite is interfered by the $u$-th UA V per time slot. Let the $\theta$-th user in $O_u$ be served by the $s$-th satellite in $S_u$ at time $t$. The ergodic achievable rate for the $\theta$-th user in $O_u$ at time $t$ can be denoted as

$$R_{s,o,t}^{\text{U},\Psi} = \mathbb{E} \left\{ \log_2 \left( 1 + \frac{P_s^{\text{S}} G_S G_O \left| h_{s,o,t}^{\text{S},\Psi} \right|^2}{\sigma^2} \right) \right\}$$

(7)

where $P_s^{\text{S}}$ denotes the transmit power of the $s$-th satellite, $G_S$ denotes the antenna gain of satellites, and $G_O$ denotes the antenna gain of users served by satellites. $h_{s,o,t}^{\text{S},\Psi}$ denotes the channel between the $u$-th UA V and the $\theta$-th user in $O_u$ which can be written as equations as equations in (2), (3) and (4). $h_{s,o,t}^{\text{S},\Psi}$ denotes the channel between the $s$-th satellite in $S_u$ and the $\theta$-th user in $O_u$, which can be expressed as

$$h_{s,o,t}^{\text{S},\Psi} = \left( L_{s,o,t}^{\text{S},\Psi} \right)^{-1/2} \tilde{h}_{s,o,t}^{\text{S},\Psi}$$

(8)

where $L_{s,o,t}^{\text{S},\Psi}$ denotes the path loss and $\tilde{h}_{s,o,t}^{\text{S},\Psi}$ denotes Rician fading during the information transmission. Let $d_{s,o,t}^{\text{S},\Psi}$ denote the distance between the $s$-th satellite in $S_u$ and the $\theta$-th user in $O_u$. Then, the path loss model can be expressed as

$$L_{s,o,t}^{\text{S},\Psi} = A_S + 10 \varsigma_S \log \left( \frac{d_{s,o,t}^{\text{S},\Psi}}{d_0} \right) + X_{s,o,t}^{\text{S},\Psi}$$

(9)

where $d_0$ denotes the reference distance, $A_S$ denotes the path loss at $d_0$, $\varsigma_S$ denotes the path-loss exponent, and $X_{s,o,t}^{\text{S},\Psi}$ is a zero-mean Gaussian random variable with standard deviation $\sigma_{X_S}$. Rician fading can be represented as

$$\tilde{h}_{s,o,t}^{\text{S},\Psi} = \sqrt{ \frac{K_S}{1 + K_S} } + \sqrt{ \frac{1}{1 + K_S} } g_{s,o,t}^{\text{S},\Psi}$$

(10)

where $g_{s,o,t}^{\text{S},\Psi} \in CN(0,1)$ and $K_S$ indicates the Rician factor. The expectation is taken over the small-scale fading. To avoid the interference shown in (7), an interference temperature limitation $I_0$ is applied to give

$$\mathbb{E} \left\{ P_{u,t}^{\text{U}} G_u G_\Psi \left| h_{u,o,t}^{\text{U},\Psi} \right|^2 \right\} \leq I_0, o \in O_u.$$  

(11)

On the ocean, the UAV has to be connected to the central processor. Either the TBS-to-UAV link or the satellite-to-UAV link can be considered for the wireless backhaul. Due to the wireless backhaul, the ergodic achievable rate of the access side of the $u$-th UA V $R_{\text{U},\Psi}^{\text{U},\Psi}$ cannot exceed that of the backhaul side of the $u$-th UA V. Thus, we have

$$R_{\text{U},\Psi}^{\text{U},\Psi} \leq R_{\text{U},\Psi}$$

(12)

Orthogonal resources, e.g., different subcarriers or different time slots, have been used to avoid the interference between UAVs. When the $\gamma$-th TBS provides the wireless backhaul for the $u$-th UA V, we have $R_{\text{U},\Psi} = R_{\text{U},\Psi}^{\text{U},\Psi}$, which can be expressed as

$$R_{\text{U},\Psi}^{\text{U},\Psi} = \mathbb{E} \left\{ \log_2 \left( 1 + \frac{P_{\gamma,t}^{\text{U}} G_{\gamma,t} G_\Psi \left| h_{\gamma,t}^{\text{U},\Psi} \right|^2}{\sigma^2} \right) \right\}$$

(13)
where $G_U$ denotes the antenna gain of TBSs and $h_{γ,u,t}^{Γ,U}$ denotes the channel between the $γ$-th TBS and the $u$-th UAV, which can be written as

$$h_{γ,u,t}^{Γ,U} = \left( \frac{d_{γ,u,t}^{Γ,U}}{d_γ^{Γ,U}} \right)^2 \frac{A_{U,U}^{Γ,U} h_{γ,u,t}^{Γ,U}}{d_γ^{Γ,U}} \left( \sqrt{K_{U} + \sqrt{1 + K_{U}} g_{γ,u,t}^{Γ,U}} \right)$$

where $d_{γ,u,t}^{Γ,U}$ denotes the distance between the $γ$-th TBS and the $u$-th UAV, $X_{γ,u,t}^{Γ,U}$ is a zero-mean Gaussian random variable with standard deviation $\sigma_{X_{γ,u,t}}$, and $g_{γ,u,t}^{Γ,U} \in CN(0, 1)$. Let $Ξ$ be the set of satellites serving UAVs. When the $u$-th UAV is connected to the $ξ$-th satellite in $Ξ$, we have $R_{bh} = R_{ξ,u,t}^{Ξ,U}$, which can be expressed as

$$R_{ξ,u,t}^{Ξ,U} = \mathbb{E} \left\{ \log_2 \left( 1 + \frac{P_{ξ,u,t}^{Ξ,U} G_{U} G_{Ψ} \left( h_{ξ,u,t}^{Ξ,U} \right)^2}{\sigma^2} \right) \right\}$$

where $P_{ξ,u,t}^{Ξ,U} = P_{ξ,u,t}^{Ξ,U}$ denotes the transmit power of the $ξ$-th satellite in $Ξ$ at time $t$ and $h_{ξ,u,t}^{Ξ,U}$ denotes the channel between the $ξ$-th satellite and the $u$-th UAV, which can be written as

$$h_{ξ,u,t}^{Ξ,U} = \left( \frac{d_{ξ,u,t}^{Ξ,U}}{d_{ξ,u,t}} \right)^2 \frac{A_{U,U}^{Ξ,U} h_{ξ,u,t}^{Ξ,U}}{d_{ξ,u,t}} \left( \sqrt{K_{ξ} + \sqrt{1 + K_{ξ}} g_{ξ,u,t}^{Ξ,U}} \right)$$

where $d_{ξ,u,t}^{Ξ,U}$ denotes the distance between the $ξ$-th satellite and the $u$-th UAV, $X_{ξ,u,t}^{Ξ,U}$ is a zero-mean Gaussian random variable with standard deviation $\sigma_{X_{ξ,u,t}}$, and $g_{ξ,u,t}^{Ξ,U} \in CN(0, 1)$.

The definition of the velocity and the acceleration of the fixed-wing UAV can be expressed as

$$v_{U,t} = c_{U,t}, \quad a_{U,t} = -c_{U,t}.$$ (17) (18)

The fixed-wing UAV has intrinsic maximum velocity $v_{max}$ and maximum acceleration $a_{max}$. Besides, it has the minimum velocity $v_{min}$ (or the stall velocity) to remain aloft. Because of these bounds to the amplitude of the velocity and the acceleration, we have

$$\|v_{U,t}\|_2 \geq v_{min}, \quad \|v_{U,t}\|_2 \leq v_{max}, \quad \|a_{U,t}\|_2 \leq a_{max}.$$ (19) (20) (21)

Besides, considering the bounds of the height of the $u$-th UAV, we have

$$z_{min} \leq z_{U,t} \leq z_{max}.$$ (22)

The lower bound in (22) is used to guarantee that the UAV is high enough to enable LOS transmission. The upper bound in (22) is set to indicate the maximum height that the UAV can reach according to the air traffic control.

We focus on the dynamic coverage performance of the user during $T$ time slots. As the energy consumption for communications is limited, we have

$$\sum_{t=1}^{T} P_{u,t}^{U} \Delta t \leq E_0$$ (23)

where $E_0$ denotes the allowable energy consumption during $T$. Considering the maximum transmit power $P_{u,t}^{U \text{ max}}$, we have

$$0 \leq P_{u,t}^{U} \leq P_{u,t}^{U \text{ max}}.$$ (24)

The working time of the UAV is mainly determined by the fuel for flying and the battery for the communication. We assume that the fuel of the fixed-wing UAV is large enough for the trip during the travel time $T$. If the residual energy is not enough to provide services after $T$, multi-UAV scheduling can be employed.

According to the above analysis, the optimization problem can be formulated as

$$\max_{p_{u,t}^{U}, c_{u,t}, a_{u,t}} \min_{t} R_{u,t}^{U}$$

subject to (11), (12), (17), (18), (19), (20), (21), (22), (23), (24)

where the minimum ergodic achievable rate during $T$ time slots is maximized, by optimizing UAV’s transmit power, three-dimensional coordinates, velocities and accelerations during $T$ time slots.

B. An Iterative Solution

The optimization problem in (25) is difficult because the expectation is taken over the Rician fading in (5), (11) and (12). Because the path loss $L_{u,t}^{Ψ}$ is available and $g_{u,t}^{Ψ} \in CN(0, 1)$, the average SNR can be expressed as

$$E \left\{ P_{u,t}^{U} G_{U} G_{Ψ} \left( L_{u,t}^{Ψ} \right) \right\} = \frac{P_{u,t}^{U} G_{U} G_{Ψ} \left( L_{u,t}^{Ψ} \right)}{\sigma^2}.$$ (26)

Let $\eta_{u,t} = P_{u,t}^{U} G_{U} G_{Ψ} \left( L_{u,t}^{Ψ} \right)$ and $\eta_{u,t}$ is analyzed and the result is demonstrated in the following theorem.

**Theorem 1:** The ergodic achievable rate $R_{u,t}^{U}$ is strictly concave and monotonically increasing with respect to the average SNR $\eta_{u,t}$.

**Proof:** See Appendix A. \hfill \blacksquare

According to the monotonicity of the objective function, we equivalently simplify (25) as

$$\max_{p_{u,t}^{U}, c_{u,t}, a_{u,t}} \min_{t} \frac{P_{u,t}^{U} G_{U} G_{Ψ} \left( L_{u,t}^{Ψ} \right)}{\sigma^2}.$$ (27)

Similarly, we assume that $K_{U} = K_{ξ}$. Then, the constraint (12) can be equivalently simplified as

$$\max_{p_{u,t}^{U}, c_{u,t}, a_{u,t}} \min_{t} \frac{P_{u,t}^{U} G_{U} G_{Ψ} \left( L_{u,t}^{Ψ} \right)}{\sigma^2} \leq P_{bh,t} G_{bh} G_{U} \left( L_{bh,t} \right) \leq P_{bh,t} G_{bh} G_{U} \left( L_{bh,t} \right)$$ (28)

where $p_{bh,t} = \left\{ p_{γ,t}^{Γ}, p_{ξ,t}^{Ξ} \right\}$, $L_{bh,t} = \left\{ L_{γ,t}^{U}, L_{ξ,t}^{Ξ} \right\}$, $G_{bh} = \left\{ G_{Γ}, G_{ξ} \right\}$, $L_{γ,t}^{U}$ denotes the path loss between the $γ$-th TBS and the $u$-th UAV, and $L_{ξ,t}^{Ξ}$ denotes the path loss between the $ξ$-th satellite in $Ξ$ and the $u$-th UAV.
To deal with the derivatives in (17) and (18), by using the first-order and second-order Taylor approximations, the constraints in (17) and (18) can be expressed as
\[
v_{u,t+1}^U \approx v_{u,t}^U + a_{u,t}^U \Delta t,
\]
\[
c_{u,t+1}^U \approx c_{u,t}^U + v_{u,t}^U \Delta t + \frac{1}{2} a_{u,t}^U \Delta t^2.
\]
Let
\[
\Delta v_{u,t}^U = v_{u,t+1}^U - (v_{u,t}^U + a_{u,t}^U \Delta t),
\]
\[
\Delta c_{u,t}^U = c_{u,t+1}^U - \left( c_{u,t}^U + v_{u,t}^U \Delta t + \frac{1}{2} a_{u,t}^U \Delta t^2 \right).
\]
We also let \( \Delta v_{w,t}^U \) and \( \Delta c_{w,t}^U \) denote the \( w \)-th element in \( \Delta v_{u,t}^U \) and \( \Delta c_{u,t}^U \), where \( w \in \{1, 2, 3\} \). We have
\[
\|\Delta v_{w,t}^U\| \leq \Delta v_0,
\]
\[
\|\Delta c_{w,t}^U\| \leq \Delta c_0
\]
where thresholds \( \Delta v_0 \) and \( \Delta c_0 \) are set to be small values. According to \( g_{u,o,t}^U \in \mathbb{C}N(0, 1) \), we have
\[
\mathbb{E} \left[ p_{u,t}^U g_{u_o,t}\right] = p_{u,t}^U g_{u_o,t} \left( L_{u_o,t}\right)^{-1}
\]
where \( L_{u_o,t}^U \) denotes the path loss between the \( u \)-th UAV and the \( o \)-th user in \( O_u \). Then, the constraint in (11) can be rewritten as
\[
p_{u,t}^U g_{u_o,t} \left( L_{u_o,t}^U\right)^{-1} \leq I_0.
\]
To solve the max-min problem, let
\[
Q = \min_{p_{u,t}^U} \left( L_{u_o,t}^U\right)^{-1} \sigma^{-2}
\]
Based on the above analysis, the problem in (25) can be approximated as
\[
\max_{p_{u,t}^U, c_{u,t}^U, v_{u,t}^U, a_{u,t}^U, Q} \quad Q \quad \text{(38a)}
\]
subject to
\[
(19), (20), (21), (22), (23),
(24), (25), (33), (34), (36),
\]
\[
\left. Q \right| L_{u_o,t}^U \leq \frac{p_{u,t}^U g_{u_o,t} \left( L_{u_o,t}^U\right)^{-1}}{\sigma^{-2}}
\]
(38b).
Let \( c_{u,t}^O \) denote the position vector of the \( o \)-th user interfered by the \( u \)-th UAV and \( c_{u,t}^\xi \) denote the position vector of the \( \xi \)-th satellite in \( \Xi \). According to (3), we rewrite constraints (28), (36) and (38b) with \( c_{u,t} \) as
\[
B_{u,t}^{w} p_{bh,t} \|c_{u,t}^U - c_{u,t}^w\| \geq B_{u,t}^{w} p_{bh,t} \|c_{u,t}^U - c_{bh,t}\| \|s_{bh}\|,
\]
\[
I_0 \|c_{u,t}^U - c_{u,t}^o\| \geq B_{u,t}^{o} p_{bh,t}^U,
\]
\[
Q \|c_{u,t}^U - c_{u,t}^w\| \leq B_{u,t}^{w} p_{bh,t}^U
\]
with
\[
B_{u,t}^{w} = G_u G_o \sigma_0^\xi \sigma^{-2} \left( \frac{w}{w-1} \right)^{\alpha_{w-1} X_{u,o,t}^\xi},
\]
\[
B_{u,t}^{o} = G_u G_o \sigma_0^\xi \sigma^{-2} \left( \frac{w}{w-1} \right)^{\alpha_{w-1} X_{u,o,t}^w},
\]
\[
B_{u,t}^{w} = G_u G_o \sigma_0^\xi \|10^{-2} X_{u,o,t}^\xi\|
\]
where \( c_{bh,t}^U \in \{c_{u,t}^U, c_{\xi,t}^U\} \), \( s_{bh} \in \{s_{U}, s_{\xi} \} \), \( A_{bh} \in \{A_{U}, A_{\xi} \} \) and \( X_{bh,t}^U \in \{X_{u,t}^U, X_{\xi,t}^U\} \). The convexity of \( \|c_{u,t}^U - c_{u,t}^w\| \) is closely related to \( c_{u,t} \). To make the analysis easy, based on the monotonicity of power functions, the constraints in (39), (40) and (41) are rewritten as
\[
\left( B_{u,t}^{w} p_{bh,t}^U \right) \|c_{u,t}^U - c_{u,t}^w\| \geq \left( B_{u,t}^{w} p_{bh,t}^U \right) \|c_{u,t}^U - c_{bh,t}\| \|s_{bh}\|,
\]
\[
I_0 \|c_{u,t}^U - c_{u,t}^o\| \geq \left( B_{u,t}^{o} p_{bh,t}^U \right) \|c_{u,t}^U - c_{bh,t}\|.
\]
\[
Q \|c_{u,t}^U - c_{u,t}^w\| \leq \left( B_{u,t}^{w} p_{bh,t}^U \right) \|c_{u,t}^U - c_{bh,t}\|.
\]
One can see that \( \|c_{u,t}^U\|^2 \), \( \|a_{u,t}^U\|^2 \), \( \|c_{u,t}^U - c_{u,t}^w\|^2 \) and \( \|c_{u,t}^U - c_{u,t}^w\|^2 \) are convex functions. The constraints in (20), (21) and (47) indicate the convex sets with respect to \( v_{u,t}^U \), \( a_{u,t}^U \), and \( c_{u,t}^U \). The constraints in (19) and (46) indicate the concave sets with respect to \( v_{u,t}^U \) and \( c_{u,t}^U \).

Then, we determine the convexity of \( A_{bh} \). If the satellite-to-UAV backhaul link is considered, \( c_{bh,t} = c_{\xi,t}, p_{bh,t} = p_{\xi,t}, G_{bh} = G_{\xi}, s_{bh} = s_{\xi}, A_{bh} = A_{\xi} \) and \( X_{bh,t} = X_{\xi,t}^U \). In the inequality (45), because the satellite is far away from the UAV, we assume that the distance between the UAV and the satellite does not change during \( T \) time slots and then \( \|c_{u,t}^U - c_{\xi,t}\| \) is constant. In this case, the constraint in (45) is non-convex with respect to \( c_{u,t}^U \). If the TBS-to-UAV backhaul link is considered, \( c_{bh,t} = c_{\xi,t}, p_{bh,t} = p_{\xi,t}, G_{bh} = G_{\xi}, s_{bh} = s_{\xi}, A_{bh} = A_{\xi} \) and \( X_{bh,t} = X_{\xi,t}^U \). Define the function
\[
f_1 \left( c_{u,t}^U \right) = \left( B_{u,t}^{w} p_{\xi,t}^U \right)^{2/\sigma_0} \|c_{u,t}^U - c_{u,t}^w\|^2 - \left( B_{u,t}^{w} p_{\xi,t}^U \right)^{2/\sigma_0} \|c_{u,t}^U - c_{\xi,t}\|^2.
\]
To determine the convexity of \( f_1 \), we verify the relationship between \( f_1 \left( c_{u,t}^U \right) \) and \( c_{u,t}^U \) by the second-order derivatives. We have the following theorem.

**Theorem 2:** If \( B_{u,t}^{w} p_{\xi,t}^U \leq B_{u,t}^{w} p_{u,t}^U \), \( f_1 \left( c_{u,t}^U \right) \) is a concave function, else if \( B_{u,t}^{w} p_{\xi,t}^U > B_{u,t}^{w} p_{u,t}^U \), \( f_1 \left( c_{u,t}^U \right) \) is a convex function.

**Proof:** The second-order partial derivative of \( f_1 \left( c_{u,t}^U \right) \) with respect to \( c_{u,t}^U \) is
\[
\tilde{f}_1 \left( c_{u,t}^U \right) = 2 \left( B_{u,t}^{w} p_{\xi,t}^U \right)^{2/\sigma_0} - 2 \left( B_{u,t}^{w} p_{u,t}^U \right)^{2/\sigma_0}.
\]
For any given \( B_{u,t}^{w} p_{\xi,t}^U \leq B_{u,t}^{w} p_{u,t}^U \), if \( p_{\xi,t}^U \leq B_{u,t}^{w} p_{u,t}^U \), \( \tilde{f}_1 \left( c_{u,t}^U \right) \) is a concave function, then we have a convex constraint in (45). If \( B_{u,t}^{w} p_{\xi,t}^U > B_{u,t}^{w} p_{u,t}^U \), \( \tilde{f}_1 \left( c_{u,t}^U \right) \) is a convex function, then we have a concave constraint in (45). Based on the above analysis, the problem in (38) is still non-convex due to the non-convex constraints in (19), (45) and (46). To make the problem in (38) more tractable, the Taylor expansion is employed to approximate the convex functions with the linear ones. Then, we obtain the following lemma.
**TABLE II**

**Successive Convex Optimization of Trajectory and Transmit Power.**

**Initialization:**
\[ c_{u,t}^{0}, v_{u,t}^{0}, e = 1.0 \times 10^{-3}, L_0 = 50, Q^0 = 0, \]
\[
\text{FOR } j = 1 \text{ TO } L_0 \\
1) \text{ Solve the problem in (55) for } c_{u,t}^{j-1}, v_{u,t}^{j-1}, \text{ then denote} \]
\[ \text{the optimal solution as } P_{u,t}^{j-1}, c_{u,t}^{j-1}, v_{u,t}^{j-1}, a_{u,t}^{j-1}, Q^j. \]
2) \text{ If } |Q^j - Q^{j-1}|/Q^j < e, \text{ stop.} \\
\]

**END**

**TABLE III**

**Successive Convex Optimization and Decoupling of Trajectory and Transmit Power.**

**Initialization:**
\[ c_{u,t}^{0}, v_{u,t}^{0}, e = 1.0 \times 10^{-3}, L_0 = 50, Q^0 = 0, \]
\[
\text{FOR } l = 1 \text{ TO } L_0 \\
1) \text{ Solve the problem in (56) for } c_{u,t}^{l-1}, v_{u,t}^{l-1}, \text{ then denote} \]
\[ \text{the optimal solution as } P_{u,t}^{l-1}, c_{u,t}^{l-1}, v_{u,t}^{l-1}, a_{u,t}^{l-1}, Q^l. \]
2) \text{ Solve the problem in (57) with } c_{u,t}^{l-1}, v_{u,t}^{l-1}, \text{ and } P_{u,t}^{l-1}, \text{ denote} \]
\[ \text{the optimal solutions as } c_{u,t}^{l-1}, a_{u,t}^{l-1}, Q^l. \]
3) \text{ If } |Q^l - Q^{l-1}|/Q^l < e, \text{ stop.} \\
\]

**END**

\[ L_1 \text{: For any given } v_{u,t}^{l}, c_{u,t}^{l}, \text{ we have} \]
\[ \left\| v_{u,t}^{l} \right\|_2^2 + 2 \left( v_{u,t}^{l} \right)^T \left( v_{u,t}^{l} - c_{u,t}^{l} \right) \geq v_{\text{min}}^2, \]  
\[ (50) \]
\[ f_{u,t}^{l} \left( P_{u,t}^{l} \right) \geq \left( B_{u,t}^{l} \right)^T f_{u,t}^{l} \geq \left\| c_{u,t}^{l} - c_{u,t}^{l} \right\|_2^2, \]  
\[ (51) \]
\[ f_{u,t}^{l} \geq v_{u,t}^{l} \geq v_{u,t}^{l}, \]  
\[ (52) \]

\[ j_{u,t}^{l} = \left\| v_{u,t}^{l} - c_{u,t}^{l} \right\|_2^2 + 2 \left( c_{u,t}^{l} - c_{u,t}^{l} \right)^T \left( c_{u,t}^{l} - c_{u,t}^{l} \right), \]  
\[ (53) \]
\[ j_{u,t}^{l} = \left\| v_{u,t}^{l} - c_{u,t}^{l} \right\|_2^2 + 2 \left( c_{u,t}^{l} - c_{u,t}^{l} \right)^T \left( c_{u,t}^{l} - c_{u,t}^{l} \right). \]  
\[ (54) \]

**Proof:** See Appendix B.

According to Lemma 1, we can iteratively solve the problem by using the successive convex optimization. The details are given in Table II. In the \( l \)-th iteration, by using \( v_{u,t}^{l-1} \) and \( c_{u,t}^{l-1} \) obtained in the \( (l-1) \)-th iteration, the optimization problem can be formulated as

\[ \max_{P_{u,t}^{l-1}, c_{u,t}^{l-1}, v_{u,t}^{l-1}, a_{u,t}^{l-1}, Q^l} \quad Q^l \]  
\[ \text{subject to } (20), (21), (22), (23), (24), (34), \]  
\[ (33), (47), (50), (51), (52). \]

In constraints, the superscript \( l \) is used for \( P_{u,t}^{l-1}, c_{u,t}^{l-1}, v_{u,t}^{l-1}, a_{u,t}^{l-1}, \) and \( Q^l \), respectively. Besides, \( v_{u,t}^{l-1} \) and \( c_{u,t}^{l-1} \) are replaced with \( v_{u,t}^{l-1} \) and \( c_{u,t}^{l-1} \), respectively.

In (55), the variables \( Q^l, P_{u,t}^{l-1}, \) and \( c_{u,t}^{l-1} \) are closely related to each other because of multiplication operations, as shown in Fig. 2. Consequently, \( c_{u,t}^{l-1} \) cannot be obtained together with \( Q^l \) and \( P_{u,t}^{l-1} \). Geometric programming can be employed to transform the multiplication operation into add one, so that \( P_{u,t}^{l-1} \) and \( c_{u,t}^{l-1} \) can be solved together. But it provides a tight bound. Therefore, we decouple the problem in (55) into two subproblems and solve it iteratively, as shown in Table III. First, with given \( c_{u,t}^{l-1} \), we optimize \( E_{u,t}^{l-1} \). Then, with the obtained \( P_{u,t}^{l-1} \) we optimize \( c_{u,t}^{l-1} \). In addition, due to the linear relationship, \( c_{u,t}^{l-1}, v_{u,t}^{l-1} \) and \( a_{u,t}^{l-1} \) are solved together in this paper. Two subproblems are described as follow.

1) **Optimization of transmit power:** By using \( E_{u,t}^{l-1} \) obtained in the \( (l-1) \)-th iteration, we set \( c_{u,t}^{l-1} = c_{u,t}^{l-1} \) and optimize the transmit power \( P_{u,t}^{l-1} \) by solving the following problem

\[ \max_{P_{u,t}^{l-1}, Q^l} \quad Q^l \]  
\[ \text{subject to } (20), (21), (22), (33), (34), \]  
\[ (47), (50), (51), (52). \]

The problem in (56) is a LP, which can be solved with CVX [57].

2) **Optimization of three-dimensional coordinates, velocities and accelerations:** By using the obtained \( P_{u,t}^{l-1}, c_{u,t}^{l-1} \) and \( v_{u,t}^{l-1} \), the problem in (55) can be rewritten as

\[ \max_{c_{u,t}^{l-1}, v_{u,t}^{l-1}, a_{u,t}^{l-1}, Q^l} \quad Q^l \]  
\[ \text{subject to } (20), (21), (22), (33), (34), \]  
\[ (47), (50), (51), (52). \]

Then, we can iteratively solve the problem in (55) by employing successive convex optimization.

Similarly, to solve the problem in (57), the bisection method is utilized to decouple \( Q^l \) and \( c_{u,t}^{l-1} \). We decompose the problem in (57) into a series of convex problems by setting \( Q^l \) and solve it iteratively. The details are shown in Table IV. In the \( m \)-th iteration, let \( U_{m-1} \) and \( L_{m-1} \) respectively denote the upper bound and lower bound of \( Q^l \). For \( Q^m = (U_{m-1} + L_{m-1})/2 \), with given \( c_{u,t}^{l-1}, v_{u,t}^{l-1} \) and \( P_{u,t}^{l-1} \), obtained by solving the problem in (56), the convex problem can be formulated as

\[ \text{find } c_{u,t}^{l-1}, v_{u,t}^{l-1}, a_{u,t}^{l-1} \]  
\[ \text{subject to } (20), (21), (22), (33), (34), \]  
\[ (47), (50), (51), (52). \]

where \( P_{u,t}^{l-1}, c_{u,t}^{l-1}, v_{u,t}^{l-1}, a_{u,t}^{l-1}, Q \) are replaced with \( P_{u,t}^{l-1}, c_{u,t}^{l-1}, v_{u,t}^{l-1}, a_{u,t}^{l-1}, Q^m \) respectively. Besides, \( v_{u,t}^{l-1} \) and \( c_{u,t}^{l-1} \) are replaced with \( v_{u,t}^{l-1} \) and \( c_{u,t}^{l-1} \) respectively. When the maximum \( Q^m \) is found, with which the convex problem (58) is solved, we achieve the related vectors \( c_{u,t}^{l-1}, v_{u,t}^{l-1}, a_{u,t}^{l-1} \). The
shortest distance between the UAV and the mobile user is \( z_{\text{min}} \). Given \( P_{\eta,t}^{U,U} \), we set the upper bound of \( Q^1 \) to be

\[
U^0 = P_{\eta,t}^{U,U}B_{\eta,t}^U z_{\text{min}}. \quad (59)
\]

The lower bound of \( Q^1 \) is set to be 0.

### IV. Simulation Results and Discussion

In this section, simulation is performed to validate the performance of our proposed algorithm. The \( \gamma \)-th TBS connected to the \( \eta \)-th UAV is located at \((0, 0, 100)\) m. The \( \eta \)-th UAV provides the communication services for the mobile user. We uniformly sample \( T = 10 \) points from the positions of the user served by the \( \eta \)-th UAV for simplicity analysis. The \( \eta \)-th UAV flies according to the optimized trajectory. The antenna gains of TBSs, UAVs and satellites are set to be 12 dB, 8 dB and 52 dB. The antenna gains of users served by UAVs and satellites are set to be 8 dB and 30 dB. The system is operated at the 5 GHz carrier frequency. We take the geosynchronous Earth orbit satellite (GEO) as an example. The transmit power of satellites is 49.03 dBm. The distance between satellites and UAVs (users) is 3.6 \( \times \) 10\(^7\) m. The path loss for the UAV-to-ground link is set to be

\[
L_{U,u,t}^{U,U} \text{ (dB)} = 116.7 + 15 \log 10 \left( \frac{d_{U,u,t}^{U,U}}{2600} \right) + X_{U,u,t}. \quad (60)
\]

The path loss for the satellite-to-UAV (user) link is set to be

\[
L_{E,U,t}^{U,U} \text{ (dB)} = 46.4 + 20 \log 10 \left( \frac{d_{E,U,t}^{U,U}}{2600} \right) + X_{E,U,t}. \quad (61)
\]

where the standard deviation of \( X_{U,u,t}^{U,U} \) and \( X_{E,U,t}^{U,U} \) is 0.1. The bandwidth allocated to satellites, UAVs and TBSs is set to be 5 MHz. The main parameters are given in Table V. For each experiment, we randomly generate the small-scale fading for 1000 rounds to achieve ergodic achievable rates according to the parameters given in Table V.

#### A. Performance Comparison between the Optimal Solution and the Approximate Solution

Because the optimization problem (25) is not convex and cannot be directly solved, the Taylor approximations and the bisection method are used to solve the problem in this paper. To validate the performance in loss caused by the Taylor approximations and the bisection method, we consider a scenario where the optimization problem (25) is simplified and the optimal values of the simplified problem can be achieved. In the scenario, the constraints on UAV kinematics, backhaul and the total energy of the UAV can be ignored. The UAV trajectory and in-flight transmit power are mainly determined by the interference. The optimization problem can be rewritten as

\[
\max_{P_{\eta,t}^{U,U},c_{\eta,t}} \frac{P_{\eta,t}^{U,U}G_{\eta}L_{U,\eta,t}^{U,U}}{\sigma^2}
\]

subject to (22), (24), (36)

\[
\text{ Lemma 2: If } I_0 \left\| \mathbf{c}^\ast - \mathbf{c}_0 \right\|_2 \geq B_{\alpha,t}^\ast P_{\max}, \text{ the optimal values of } P_{\eta,t}^{U,U} \text{ and } \mathbf{c}_{\eta,t} \text{ in the optimization problem (62) are } P_{\max} \text{ and } \mathbf{c}^\ast, \text{ where } \mathbf{c}^\ast = \left[ \mathbf{c}_{\eta,t} \mathbf{c}_{\eta,t} \mathbf{z}_{\text{min}} \right]^T.
\]

Proof: See Appendix C.

Assume that the users served by the UAV and the satellite are respectively located at \((5.0 \times 10^4, 0, 10)\) m to \((5.0 \times 10^4, -5 \times 10^5, 10)\) m. The interference temperature limitation \( I_0 \) is \(-74\) dBm and \( K_U = 31.3\). The maximum transmit power \( P_{\max}^{U,U} \) is in the range \([20, 28]\) dBm and then \( I_0 \left\| \mathbf{c}^\ast - \mathbf{c}_0 \right\|_2 \geq B_{\alpha,t}^\ast P_{\max} \) can be satisfied. The initial location of the UAV is set to be \((4.5 \times 10^4, 0, 3000)\). By using the solutions obtained with Taylor approximations and the bisection method and those given in Lemma 2, the minimum ergodic achievable rate is compared by simulation. The simulation result is shown in Fig. 3. For this scenario, using Taylor approximations and the bisection method, the minimum ergodic achievable rate of the approximate solution is close to that of the optimal solution.

#### B. Performance Comparison among Different Algorithms

In this part, we compare our proposed algorithm with those in [20] and [22]. In these works, the full CSI was used for the whole trajectory optimization. The user served by the \( \eta \)-th UAV travels from the position \((5.0 \times 10^4, 0, 10)\) m to \((6.8 \times 10^4, 0, 10)\) m along x axis. Let \( \mathbf{c}_{\eta,t} = \left[ \mathbf{c}_{\eta,t}^\ast \mathbf{v}_{\eta,t} \mathbf{z}_{\text{min}} \right]^T \) be the positions of the user served by the \( \eta \)-th UAV and \( \mathbf{v}_{\eta,t} \) be the user's velocity. For comparison, we adopt a basic trajectory which is denoted as \( \mathbf{c}_{\eta,t} = \left[ \mathbf{c}_{\eta,t}^\ast \mathbf{v}_{\eta,t} \mathbf{z}_{\text{min}} \right]^T \). The transmit power is set to satisfy the constraints on tolerable interference, backhaul, maximum transmit power and the total communication energy of the UAV. Besides, the positions of the users served by

<table>
<thead>
<tr>
<th>Table IV: Bisection Method for Solving the Problem (57).</th>
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<tbody>
<tr>
<td><strong>Initialization:</strong></td>
</tr>
<tr>
<td>1) ( \varepsilon = 1.0 \times 10^{-3} ), ( M_0 = 50 ),</td>
</tr>
<tr>
<td>2) Set ( U^0 = P_{\eta,t}^{U,U}B_{\eta,t}^U z_{\text{min}} ).</td>
</tr>
<tr>
<td>FOR ( m = 1 ) TO ( m = M_0 ), ( Q^m = (U^{m-1} + L^{m-1})/2 ),</td>
</tr>
<tr>
<td>4) Solve the convex problem in (58) with given ( c_{\eta,t}^{U,U} ), ( y_{\eta,t}^{U,U} ), ( P_{\eta,t}^{U,U} ) and ( Q^m ), and denote the optimal values as ( c_{\eta,t}^{U,U} ), ( y_{\eta,t}^{U,U} ), ( u_{\eta,t}^{U,U} ), ( u_{\eta,t}^{U,U} ), ( u_{\eta,t}^{U,U} ), ( u_{\eta,t}^{U,U} ), ( u_{\eta,t}^{U,U} ), ( u_{\eta,t}^{U,U} ), ( u_{\eta,t}^{U,U} ), ( u_{\eta,t}^{U,U} ), ( u_{\eta,t}^{U,U} ).</td>
</tr>
<tr>
<td>5) If the problem is solved, ( U^m = U^{m-1} ), ( L^m = Q^m ); otherwise ( U^m = Q^m ), ( L^m = L^{m-1} ).</td>
</tr>
<tr>
<td>6) If (</td>
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<td>END</td>
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<th>Table V: Simulation Parameters.</th>
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<tr>
<td>Symbol</td>
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<tr>
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<tr>
<td>( z_{\text{min}} )</td>
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<tr>
<td>( z_{\max} )</td>
</tr>
<tr>
<td>( \mathbf{v}_{t} )</td>
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<td>( \sigma^2 )</td>
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</table>
The total communication energy $/u1D438$ is mainly determined by backhaul and total communication energy. When the transmit power is bounded by the maximum transmit power, $/u1D443$ the interference temperature limitation $/u1D43C$ is compared. The simulation results are shown in Fig. 4, where $E_0 = 500$ J and $P_{\text{min}} = 40$ dBm. We set that the interference temperature limitation $I_0 = -40$ dBm and vary maximum transmit power $P_{\text{max}}$ in the range $[22, 36]$ dBm. Because $I_0$ is large, the interference can be ignored. The transmit power is bounded by the maximum transmit power, backhaul and total communication energy. When $P_{\text{max}} \geq 30$ dBm, the performance is mainly determined by backhaul and maximum transmit power. The existing algorithms ignore the constraint of maximum transmit power. We decrease their transmit power to satisfy this constraint. One sees that the performance can be improved with the optimization problem subject to the constraint of maximum transmit power. When $P_{\text{max}} \geq 30$ dBm, the total transmit power during $T$ is larger than the total communication energy and the performance is mainly determined by backhaul and total communication energy. The algorithm in [20] investigated the optimization problem with full CSI subject to constraints of backhaul and total communication energy. Our proposed algorithm achieves better performance than that in [20]. To further validate the performance of our proposed algorithm using the large-scale CSI, we vary Rician factor $K_U$. The simulation results are shown in Fig. 5. One sees that by reducing $K_U$, our proposed algorithm obtains much better performance than the existing ones. One sees that the performance can be improved with the large-scale CSI.

To illustrate the performance gain achieved by using interference constraint, the comparison of minimum ergodic...
achievable rate is shown in Fig. 6, where $K_U = 31.3$. We set $E_0 = 3 \times 10^4$ J and $P_{U,t}^{\text{max}} = 40$ dBm. Because $E_0$ is large, the transmit power is limited by interference, maximum transmit power and backhaul. We set that the interference temperature limitation on transmit power is limited by interference, maximum transmit power.

In [20] and [22] neglect the constraints of interference and maximum transmit power. We reduce their transmit power to satisfy those constraints. By varying $I_0$ and $P_{U,t}^{\text{max}}$, the minimum ergodic achievable rate is increased when $P_{U,t}^{\text{max}} \geq 36$ dBm. One sees that the transmit power is determined by interference constraint when $P_{U,t}^{\text{max}} \geq 36$ dBm and $I_0 = -55$ dBm. The performance of our proposed algorithm is best of all when $P_{U,t}^{\text{max}} \geq 36$ dBm and $I_0 = -55$ dBm. Thus, our proposed algorithm can improve minimum ergodic achievable rate by a joint optimization of the whole trajectory and the transmit power with interference constraints.

In this part, the minimum ergodic achievable rate of the backhaul link and the access link of the UAV and the satellite-to-user link is simulated. The user served by the $u$-th UAV travels from the position $(1.0 \times 10^5, 0, 10)$ m to $(2.8 \times 10^5, 0, 10)$ m along $x$ axis. The positions of users served by satellites are set as $\mathbf{c}_{t, t'}^{C_u} = [x_{t, t'}, y_{t, t'}, z_{\min}^{u,t}]^T$. Set $P_{U,t}^{\text{max}} = 37$ dBm, $P_{U,t}^{\text{max}} = 40$ dBm and $E_0 = 6000$ J. The interference temperature limitation $I_0$ is in the range $[-94, -74]$ dBm. When the $\gamma$-th TBS provides the backhaul link for the $u$-th UAV, the simulation result is shown in Fig. 7, where the initial trajectory of the $u$-th UAV is $[0.9y_{\min}^{u,t}, y_{\min}^{u,t}, z_{\min}^{u,t}]^T$. When $I_0$ is increased, the minimum ergodic achievable rate of the satellite-to-user link is reduced because of the interference. When $I_0 \leq -82$ dBm, the minimum ergodic achievable rate of the access link of the $u$-th UAV is lower than that of the backhaul link of the $u$-th UAV because the interference constraint is tighter than the backhaul constraint. When $I_0 \geq -82$ dBm, the performance is jointly
determined by the interference constraint and the backhaul constraint. When the satellite provides the backhaul link for the UAV, the simulation result is shown in Fig. 8, where the initial trajectory of\( U_A V \) is \([x_{u,t}^w, y_{u,t}^w, z_{\min}]^T\). Obviously, when \( I_0 \leq -86 \) dBm, the minimum ergodic achievable rate of the access link of the \( u \)-th UAV is lower than that of the backhaul link of the \( u \)-th UAV because the interference constraint is tighter than the backhaul constraint. When \( I_0 \geq -86 \) dBm, the minimum ergodic achievable rate is unvaried because the performance is mainly determined by the backhaul constraint.

We also analyze the impact of the total energy and the interference on the minimum ergodic achievable rate. Set \( P_{f,t}^w = 37 \) dBm, \( P_{m}^{U_{max}} = 40 \) dBm and \( K_{U} = K_{S} = 31.3 \). When the \( y \)-th TBS provides the backhaul link for the \( u \)-th UAV, the simulation result is shown in Fig. 9, where the total energy \( E_0 \) is in the range \([1, \ 10^4]\) J. The interference temperature limitation \( I_0 \) is set to be \(-94 \) dBm, \(-82 \) dBm and \(-74 \) dBm, respectively. The initial trajectory of the \( u \)-th UAV is \([x_{u,t}^w, y_{u,t}^w, z_{\min}]^T\), \([x_{u,t}^w, y_{u,t}^w, z_{\min}]^T\) and \([0.9x_{u,t}^w, y_{u,t}^w, z_{\min}]^T\), respectively. When the satellite provides the backhaul link for the UAV, the simulation result is shown in Fig. 10, where the total energy \( E_0 \) is in the range \([1, \ 10^2]\) J. The interference temperature limitation \( I_0 \) is set to be \(-94 \) dBm, \(-90 \) dBm and \(-86 \) dBm, respectively. The initial trajectory of the \( u \)-th UAV is \([x_{u,t}^w, y_{u,t}^w, z_{\min}]^T\). As shown in Fig. 9 and Fig. 10, when \( I_0 \) and \( E_0 \) are increased, better performance can be obtained. When the energy constraint is tight, the performance is determined by \( E_0 \). By increasing \( E_0 \), when the interference constraint is tight, the performance is determined by \( I_0 \).

An optimized trajectory and transmit power of a UAV in the \( x \)-\( y \) plane are shown in Fig. 11, where \( P_{f,t}^w = 40 \) dBm, \( P_{m}^{U_{max}} = 40 \) dBm, \( I_0 = -55 \) dBm, \( E_0 = 4000 \) J, and \( K_{U} = K_{S} = 31.3 \). The mobile user travels from the position \((5.0 \times 10^4, 0, 10)\) m to \((6.8 \times 10^4, 0, 10)\) m along the \( x \) axis. The positions of users served by satellites are set as \( c_{d,t}^u = [x_{d,t}^w, y_{d,t}^w, z_{\min}]^T \). The initial trajectory of the UAV is \([1/2, y_{u,t}^w, z_{\min}]^T\). The UAV flying according to the blue curve serves the user moving along the dark line. Because of constraints of wireless backhaul, the optimized trajectory is between the TBS and the mobile user. Besides, because the users interfered by the UAV appear on the sides of the mobile user, the optimized trajectory is bent to satisfy interference constraints. The obtained transmit power of the UAV satisfies the constraints on maximum transmit power and allowable communication energy.

D. Convergence Performance of the Proposed Algorithm

The convergence is analyzed in this part. The experiment is implemented 100 times by generating different scenes. The user served by the UAV travels from the position \((5.0 \times 10^4, 0, 10)\) m to \((6.8 \times 10^4, 0, 10)\) m along the \( x \) axis. The users served by satellites and interfered by the UAV appear randomly. The distance between the user served by satellites and the one served by the UAV is 8000 m. The maximum numbers of iterations are shown in Fig. 12, where \( P_{m}^{U_{max}} \) is in the range \([22, \ 38]\) dBm, \( P_{f,t}^w = 40 \) dBm, \( K_{U} = 31.3 \), and \( E_0 \) is 500 J and 4000 J. The interference temperature limitation \( I_0 \) is \(-55 \) dBm and \(-40 \) dBm and the initial trajectory of UAV is \([3x_{u,t}^w/4, y_{u,t}^w, z_{\min}]^T\) and \([x_{u,t}^w/2, y_{u,t}^w, z_{\min}]^T\), respectively. Different values of parameters represent different cases, where the performance is either separately or jointly determined by the constraints on maximum transmit power, interference, backhaul and the allowable communication energy. One sees that, the maximum number of iterations is smaller than 25 in all cases. Thus, the algorithm converges within 25 iterations in the cases considered.

V. CONCLUSIONS

In this paper, UAVs have been used for on-demand satellite-terrestrial maritime communications. The coordination with existing satellites/terrestrial systems has been investigated to realize spectrum sharing and efficient backhaul. This paper has adopted a typical composite channel model consisting of both large-scale and small-scale fading, under which UAVs have been deployed for accompanying coverage. The UAV's whole
trajectory and transmit power during the fight have been jointly optimized, subject to constraints on UAV kinematics, tolerable interference, backhaul, and the total communication energy of the UAV. Different from previous studies, we have assumed that only the large-scale CSI is available, as the positions of mobile ships can be obtained via the maritime AIS and be used as the prior information. Then, we have solved the non-convex problem by problem decomposition, successive convex optimization and bisection searching tools. Simulation results have shown that the UAV fits well with existing satellite and terrestrial systems. Besides, the performance gain can be achieved via joint optimization of UAV trajectory and transmit power with only the large-scale CSI. In future work, we will explore more possibility of improving the quality of service by utilizing UAVs and jointly investigate trajectory optimization, interference management and user association among UAVs, TBSs and satellites.

APPENDIX A

**Proof of Theorem 1**

Let \( R_{u,a,t}^{U,W} = P_{u,a} G_U G_W \left( L_{u,a,t}^{U,W} \right)^{-1} \sigma^{-2} \). According to (5), \( R_{u,a,t}^{U,W} \) can be expressed as

\[
R_{u,a,t}^{U,W} = \log_2 \left( 1 + \eta_{u,a,t} b_{U,W}^{u,a,t} \right),
\]

where

\[
b_{U,W}^{u,a,t} = \frac{1}{1 + K_U} \left[ \frac{K_U}{1 + K_U} + \sqrt{\frac{1}{1 + K_U} U_{u,a,t}^{U,W}} \right]^2.
\]

We analyze the relationship between \( R_{u,a,t}^{U,W} \) and \( \eta_{u,a,t}^{U,W} \) via the first-order and second-order derivatives. Since \( \eta_{u,a,t}^{U,W} \in \mathcal{CN}(0, 1) \), the variable \( b_{U,W}^{u,a,t} \) follows a non-central chi-square probability density function with two degrees of freedom as

\[
f_{b_{U,W}^{u,a,t}}(\rho) = (1 + K_U) e^{-\frac{K_U}{1 + K_U}} I_0 \left( 2 \sqrt{K_U (1 + K_U)} \rho \right),
\]

where \( \rho \geq 0 \) and \( I_0(\cdot) \) is the zeroth-order modified Bessel function of the first kind [53]. Then, \( R_{u,a,t}^{U,W} \) can be expressed as

\[
R_{u,a,t}^{U,W} = \log_2 e \int_0^{\infty} \ln \left( 1 + \eta_{u,a,t}^{U,W} \rho \right) f_{b_{U,W}^{u,a,t}}(\rho) d\rho.
\]

The first-order derivative with respect to \( \eta_{u,a,t}^{U,W} \) is

\[
R_{u,a,t}^{U,W} = \log_2 e \int_0^{\infty} \frac{\rho}{1 + \eta_{u,a,t}^{U,W}} f_{b_{U,W}^{u,a,t}}(\rho) d\rho.
\]

The second-order derivative with respect to \( \eta_{u,a,t}^{U,W} \) is

\[
R_{u,a,t}^{U,W} = \log_2 e \int_0^{\infty} \frac{-\rho^2}{(1 + \eta_{u,a,t}^{U,W})^2} f_{b_{U,W}^{u,a,t}}(\rho) d\rho.
\]

Because \( \eta_{u,a,t}^{U,W} \geq 0 \) and \( f_{b_{U,W}^{u,a,t}}(\rho) > 0 \), \( R_{u,a,t}^{U,W} > 0 \) and \( R_{u,a,t}^{U,W} < 0 \). So, \( R_{u,a,t}^{U,W} \) is an increasing function of \( \eta_{u,a,t}^{U,W} \) and strictly concave. Thus, the theorem is proved.

**Appendix B**

**Proof of Lemma 1**

According to that any convex function is globally lower-bounded by its first-order Taylor expansion at any point [58], with the given \( v_{u,t}^{U,R} \) and \( c_{u,t}^{U,R} \), we have the following inequalities

\[
\|v_{u,t}^{U,R}\|^2_2 \geq \|v_{u,t}^{U,R}\|^2_2 + 2 \left( \vspace{-1pt} v_{u,t}^{U,R} \right)^T \left( v_{u,t}^{U,R} - v_{u,t}^{U,R} \right),
\]

\[
\|c_{u,t}^{U,R} - c_{u,t}^{U,R}\|^2_2 \geq \|c_{u,t}^{U,R} - c_{u,t}^{U,R}\|^2_2 + 2 \left( c_{u,t}^{U,R} - c_{u,t}^{U,R} \right)^T \left( c_{u,t}^{U,R} - c_{u,t}^{U,R} \right).
\]  

Then, combining the constraints in (19), (45) and (46), the lemma is proved.

**Appendix C**

**Proof of Lemma 2**

We rewrite the objective function in (62) with \( c_{u,t}^{U,R} \) as

\[
P_{u,a,t}^{U} G_U G_W \left( L_{u,a,t}^{U,W} \right)^{-1} \sigma^2 = B_{u,a,t}^{c} P_{u,a}^{c} \left\| c_{u,a,t}^{U,R} - c_{u,a,t}^{U,R} \right\|_2^2.
\]

Obviously, considering the constraints (22) and (24), when \( P_{u,a}^{c} = P_{u,a}^{\text{max}} \) and \( c_{u,a,t}^{U,R} = \left[ v_{u,a,t}^{U,R}, y_{u,a,t}, z_{\text{min}} \right]^T \), the objective function can be maximized. However, the constraint (36) also should be satisfied. Let \( c^* = \left[ v_{u,a,t}^{U,R}, y_{u,a,t}, z_{\text{min}} \right]^T \). According to (36), if \( I_0 \left( c^* - c_{u,a,t}^{U,R} \right) \geq B_{u,a,t}^{c} P_{u,a}^{c} \left( \max \right) \), the optimal values of \( P_{u,a}^{c} \) and \( c_{u,a,t}^{U,R} \) in the optimization problem (62) are \( P_{u,a}^{\text{max}} \) and \( c^* \). The lemma is proved.

**References**


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