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We show that financial correlations exhibit a non-trivial dynamic behavior. We introduce a simple phenomenological model of a multi-asset financial market, which takes into account the impact of portfolio investment on price dynamics. This captures the fact that correlations determine the optimal portfolio but are affected by investment based on it. We show that such a feedback on correlations gives rise to an instability when the volume of investment exceeds a critical value. Close to the critical point the model exhibits dynamical correlations very similar to those observed in real markets. Maximum likelihood estimates of the model’s parameter for empirical data indeed confirm this conclusion, thus suggesting that real markets operate close to a dynamically unstable point.

Financial markets – as prototypical examples of the collective effects of human interaction – have recently attracted the attention of many physicists. This is because, in spite of their internal complications, their aggregate behavior exhibits surprising regularities which can be cast in the form of simple, yet non-trivial, statistical laws, reminiscent of the scaling laws obeyed by anomalous fluctuations in critical phenomena. Such a suggestive indication has been put on even firmer basis by recent research on the statistical physics approach to interacting agent models. This has shown that quite realistic market behavior can indeed be generated by the internal dynamics generated by traders’ interaction.

The theoretical approach has, thus far, mostly concentrated on single asset models, whereas empirical analysis has shown that ensembles of assets exhibit rich and non-trivial statistical properties, whose relations with random matrix theory, complex networks, and multi-scaling have attracted the interest of physicists. The central object of study is the covariance matrix of asset returns (at the daily scale in most cases). The bulk of its eigenvalue distribution is dominated by noise and described very well by random matrix theory. The few large eigenvalues which leak out of the noise background contain significant information about market’s structure. The taxonomy built with different methods from financial correlations alone bear remarkable similarity with a classification in economic sectors. This agrees with the expectation that companies engaged in similar economic activities are subject to the same “factors”, e.g. fluctuations in prices or demands of common inputs or outputs. Besides their structure, market correlations also exhibit a highly non-trivial dynamics: Correlations “build up” as the sampling time horizon on which returns are measured increases (Epps effect) and saturate for returns on the scale of some days. Furthermore, these correlations are persistent over time and they follow recurrent patterns.

In what follows we shall mostly concentrate on the dynamics of the largest eigenvalue of the correlation matrix. The corresponding market mode describes the co-movement of stocks and it accounts for a significant fraction of the correlations. Fig. 1a shows the time dependence of the largest eigenvalue of the (exponentially averaged) correlation matrix of daily returns for Toronto Stock Exchange. Similar behavior has been reported earlier for different markets. Fig. 2 shows that fluctuations in the largest eigenvalue are broadly distributed, suggesting that Fig. 1a can hardly be explained entirely as the effect of few external shocks.

This leads us to formulate the hypothesis that such non-trivial behavior arises as a consequence of the internal market dynamics. One of the key functions of financial markets is indeed that of allowing companies to “trade” their risk for return, by spreading it across financial investors. Investors on their side, diversify (i.e. spread) their strategies across stocks so as to minimize risk, as postulated by portfolio optimization theory. The efficiency of portfolio optimization depends on the cross correlations among the stocks the financial market is composed of. The optimal portfolio is computed under the price taking assumption that investment does not affect the market. While this is reasonable for the single investor, the effect of many investors following this same strategy can be...
sizeable. If financial trading activity resulting from portfolio optimization strategies have an impact on prices’ dynamics, it will also affect the correlations which these strategies exploit. Hence financial correlations enter into a feedback loop because they determine in part those trading strategies which contribute to the price dynamics, i.e. to the financial correlations themselves. This feedback is somewhat implicit in the Capital Asset Pricing Model (CAPM), which concludes that since all traders invest according to the optimal portfolio, the market is well approximated by a one factor model [20] (see however [12]). While this explains why the largest eigenvalue of the correlation matrix is so well separated from the other ones, CAPM relies on rational expectation equilibrium arguments, and it does not address dynamical effects such as those of Fig. 1.

This Letter discusses a general phenomenological approach, in the spirit of Landau’s theory of critical phenomena [21], which shows that a non-trivial dynamics of correlations can indeed result from the internal dynamics due to trading on optimal portfolio strategies. The model predicts a dynamical instability if the investment volume $W$ exceeds a critical value. Not only we find very realistic dynamics of correlations close to the critical point (see Fig. 1b) but maximum likelihood parameter estimation from real data suggest that markets are indeed close to the instability. Phenomenological models are particularly suited for modeling complex systems, such as a financial market, were a bottom-up (microscopic) approach inevitably implies dealing with many complications and introducing ad hoc assumptions [23]. For the ease of exposition, we shall first introduce a minimal model which captures the interaction among assets induced by portfolio investment. Later we will show that this model contains the lowest order terms in a general expansion of the dynamics and that all the terms beyond these are irrelevant as far as the main conclusions are concerned. A further reason for focusing on the simplest model is that it will make the comparison with empirical data easier.

The last term of Eq. 1 describes the impact of portfolio investment on the price dynamics: $\xi_t$ is an independent Gaussian variable with mean $\epsilon$ and variance $\Delta$ and the vector $|z_t\rangle$ is the optimal portfolio with fixed return $R$ and total wealth $\langle z|1\rangle = W$. In other words, $|z_t\rangle$ is the solution of

$$|x_{t+1}\rangle = |x_t\rangle + |\beta_t\rangle + \xi_t|x_t\rangle.$$  \hspace{1cm} (1)

where $|\beta_t\rangle$ is the vector of bare returns, which describes all external “forces” which drive the prices, including economic processes. This is assumed to be a Gaussian random vector with

$$E[|\beta_t\rangle] = |b\rangle, \quad E[|\beta_t\rangle\langle \beta(t')|] = |b\rangle\langle b| + \hat{B}\delta_{t,t'}$$  \hspace{1cm} (2)

$|b\rangle$ and $\hat{B}$ will be considered as parameters in what follows.

The parameter $W$, the likelihood parameter estimation from real data suggest that markets are indeed close to the instability. The model contains the lowest order terms in a general expansion of the dynamics and that
can be used as a proxy for expected correlations and returns. Eqs. (15) also assume that portfolio investment is dominated by a single time scale $\tau$. Later we shall argue that a generic distribution of time scales would not change the main results. Finally, Eq. (1) assumes a linear price impact and gaussian bare returns. Both assumptions may be questionable, especially at high frequency [23, 24]. We shall see, however, that non-trivial dynamics and statistics (including a fat tailed distribution of returns) arises even in such a simplified setting, thus suggesting that the specific market mechanism and the statistics of bare returns are unessential ingredients.

Numerical simulations of the model show a very interesting behavior. In Fig. 1b we plot the temporal evolution of the maximum eigenvalue of the correlation matrix for a particular choice of parameters (see later). The dynamics is highly non-trivial, with the appearance of instabilities resembling that of a phenomenological expansion [21]. Higher orders, e.g. $|z_{t+1}| - |z_t|$, as well as terms proportional to $|\tau_t|$ and its time derivatives, can be included. Likewise, one can consider a generic matrix $B$, or add several components $|z^k|$ of portfolio investment in Eq. (1), each with different parameters $R^k, W^k$ and $\Delta^k$ or acting over different time horizons $\tau_k$. In all these cases, we confirmed [28] the existence of a dynamical instability when the volume of trading exceeds a critical value, as long as the time-scales ($\tau_k$) over which averages are taken in Eqs. (15) are very large. The analytic approach can be extended to finite $\tau$ by a systematic $1/\tau$ expansion in the $W < W^*$ phase [23]. This expansion describes how fluctuations in slow quantities, such as $|z_t|$ or $C_t$, vanish as $\tau \rightarrow \infty$. We find that the coefficients of the $1/\sqrt{\tau}$ expansion diverge as $W \rightarrow W^*$, signalling that fluctuations do not vanish for $W > W^*$. For example, we find that fluctuations in $\Lambda$ diverge as $\Delta \Lambda \sim |W^* - W|^{-1/2}$, when $W \rightarrow W^*$. This is why higher order terms such as $|z_t| - |z_{t-1}|$ in Eq. (1) are irrelevant, in the sense of critical phenomena, i.e. their presence does not affect the occurrence of the phase transition.

Numerical simulations fully confirm these results. Fig. 3 reports the relative fluctuations of $\Lambda_t$ as a function of $W$, for simulations carried out at different time scales $\tau$. For $W < W^*$, fluctuations vanish as $\tau$ increases and $\Lambda$ converges to the value of Eq. (7). For $W > W^*$, instead, the dynamics is characterized by persistent instabilities with fluctuations of the same order of $\Lambda$, and it does not attain a smooth limit as $\tau \rightarrow \infty$. For values of $W$ smaller but close to $W^*$ the model exhibits strong fluctuations, precursors of the instabilities for $W > W^*$. It is precisely in this critical region that we recover realistic results, such as those of Fig. 1. Moreover, the distribution of returns develops a power law behavior as $W$ approaches $W^*$ (with a cutoff which diverges as $1/\sqrt{W^* - W}$).

The presence of a phase transition from a stable to an unstable state and the strong resemblance of the dynamics of the model close to criticality with real data (see Fig. 1) suggests that real markets might be close to the phase transition. In order to investigate this issue systematically, we estimate the parameters of our model from real data. In doing this we implicitly assume that parameters $\epsilon, R, W$ etc. vary slowly on time scales of order $\tau$. We compute the likelihood that the particular set of time series of a given market are produced as output of Eq. (1) for a particular choice of parameters. Next we find the parameters which maximize the likelihood [28]. As a check, the procedure was run on synthetic data set generated by Eq. (1) and it allowed us to recover the parameters with which the data set was created. In the inset of Fig. 2 we plot the result of such a fit for (the assets of) four different indices in the time period 1997-2005 [18]. We used $\tau = 50$ and fits were taken on a time window of $T = 300$ days.
in this respect, that while in our model $\tau$ enters both in the 
dynamics and in the way we take averages, in the empirical 
analysis it only enters in the way we take averages, whereas 
we don’t have access to the time scale $\tau$ used by investors. We 
checked that the main results do not depend significantly on 
the choice of $\tau$. We see that fitted parameters for real markets 
tend to cluster close, but below, the transition line $W = W^\star$. 
This is also consistent with the similarity of the distribution of 
$\Lambda$ for real and synthetic data of Fig. 2.

Our model is very stylized and it misses many important 
Aspects. For example, it is undeniable that external factors 
and global events have an effect on financial markets. For 
example, the introduction of the Euro has a visible effect on 
markets as systems driven to a critical state, by speculative trading 
occuring and replacing traditional mechanisms. If, following Ref. [29], 
markets are interacting as if a sort of generalized Le Chatelier’s principle 
was at play.

Our results indicate the existence of an additional component 
of risk due to the enhanced susceptibility of the market. Such “market impact” risk arises because investing in 
risk minimization strategies affects the structure of correlations 
with those strategies were computed. This component of risk diverges as the market approaches the critical point $W^\star$, thus discouraging further investment. This provides a simple rationale of why markets “self-organize” close 
to the critical point. Such a scenario is reminiscent of the picture 
which Minority Games [8] provide of single asset markets 
as systems driven to a critical state, by speculative trading 
enters both in the way we take averages, whereas 

FIG. 3: Relative fluctuation of the maximum eigenvalue as a function of 
$W$ in a simulation of the model with $N = 20$, $\epsilon = 0.1$, $R = 1$, 
$\Delta = 1$, $B = 10^{-2}$, $\tau = 1000$ (+), $\tau = 20000$ (×) and $\tau = 50000$ 
(•). Vertical line is the theoretical critical value of $W$.

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479 (1997).
[8] Challet D., Marsili M. and Zhang Y-C. Minority Games. Inter-
acting agents in financial markets Oxford University Press 
[17] The persistence of the structure of correlations [11, 14] and 
their overlap with economic sectors [16, 18] suggests that it 
can be related to economic factors which evolve on long time 
scales. Financial activity is instead relevant over time scales of 
few days and it is responsible for the emergence of the market 
mode.
[18] Data was taken form finance.yahoo.com in the time pe-
riod June 16th, 1997 to May 25th, 2005 for all assets except for the 
Dow Jones, for which we used May 2nd, 1995 to May 23rd, 
2005. Correlations were measured on the set of assets compos-
ing the index at the final date.
[20] Elton E.J. and Gruber M.J., Modern Portfolio theory and invest-
ment analysis (J. Wiley & sons, New York, 1995).
[22] $|x|$ should be considered as a column vector, whereas $\langle x \rangle$ 
is a row vector. Hence $|x\rangle |y\rangle$ is the scalar product and $|x\rangle \langle y|$ 
is the direct product, i.e. the matrix with entries $a_{ij} = \langle x_i, y_j\rangle$.
[23] A simple generalization of single asset market models [8, 9] 
might also produce a complex dynamics. The emergence of a 
market mode is a natural consequence of ad hoc behavioral 
assumptions (herding). Such an approach, however, focuses on
speculative trading where the dynamics is driven by expected returns, and misses the peculiar role which risk and correlations play.

[24] Exponential moving averages such as that used in Eqs. (4-5) are widely used in finance (see [21] p. 59). Our main results are related to the behavior of the model for $\tau \to \infty$ and clearly remain unchanged if one assumes uniform averages over a finite window $T$ (as e.g. Refs. [11, 12, 14, 15]), and then lets $T \to \infty$.


[27] There are indeed two solutions for $\Lambda$. We choose the one for which $\Lambda \to B$ as $\epsilon \to 0$.


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