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Differential Branching Fraction and Angular Analysis of the Decay $B^0 \rightarrow K^{*0} \mu^+ \mu^-$

R. Aaij et al.*
(LHCb Collaboration)

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The angular distributions and the partial branching fraction of the decay $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ are studied by using an integrated luminosity of 0.37 fb$^{-1}$ of data collected with the LHCb detector. The forward-backward asymmetry of the muons, $A_{FB}$, the fraction of longitudinal polarization, $F_L$, and the partial branching fraction $dB/dq^2$ are determined as a function of the dimuon invariant mass. The measurements are in good agreement with the standard model predictions and are the most precise to date. In the dimuon invariant mass squared range $1.00–6.00$ GeV$^2/c^4$, the results are $A_{FB} = -0.06^{+0.13}_{-0.14} \pm 0.04$, $F_L = 0.55 \pm 0.10 \pm 0.03$, and $dB/dq^2 = (0.42 \pm 0.06 \pm 0.03) \times 10^{-7}$ GeV$^{-2}$. In each case, the first error is statistical and the second systematic.

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The process $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ is a flavor changing neutral current decay. In the standard model (SM) such decays are suppressed, as they can proceed only via loop processes involving electroweak penguin or box diagrams. As-yet undiscovered particles could give additional contributions with comparable amplitudes, and the decay is therefore a sensitive probe of new phenomena. A number of angular observables in $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ decays can be theoretically predicted with good control of the relevant form factor uncertainties. These include the forward-backward asymmetry of the muons, $A_{FB}$, and the fraction of longitudinal polarization, $F_L$, as functions of the dimuon invariant mass squared, $q^2$ [1]. These observables have previously been measured by the BABAR, Belle, and CDF experiments [2]. A more precise determination of $A_{FB}$ is of particular interest as, in the 1.00 < $q^2$ < 6.00 GeV$^2/c^4$ region, previous measurements favor an asymmetry with the opposite sign to that expected in the SM. If confirmed, this would be an unequivocal sign of phenomena not described by the SM. This Letter presents the most precise measurements of $A_{FB}$, $F_L$, and the partial branching fraction $dB/dq^2$ to date. The data used for this analysis were taken with the LHCb detector at CERN during 2011 and correspond to an integrated luminosity of 0.37 fb$^{-1}$. The $K^{*0}$ is reconstructed through its decay into the $K^+ \pi^-$ final state.

The LHCb detector [3] is a single-arm spectrometer designed to study $b$-hadron decays. A silicon strip vertex detector positioned around the interaction region is used to measure the trajectory of charged particles and allows the reconstruction of the primary proton-proton interactions and the displaced secondary vertices characteristic of $B$-meson decays. A dipole magnetic field and further charged particle tracking stations allow momenta in the range 5 < $p$ < 100 GeV/c to be determined with a precision of $\delta p/p = 0.4\%–0.6\%$. The experiment has an acceptance for charged particles with pseudorapidity between 2 and 5. Two ring imaging Cherenkov detectors allow kaons to be separated from pions or muons over a momentum range 2 < $p$ < 100 GeV/c. Muons are identified on the basis of the number of hits in detectors interleaved with an iron muon filter.

The $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ angular distribution is governed by six $q^2$-dependent transversity amplitudes. The decay can be described by $q^2$ and the three angles $\theta_t$, $\theta_K$, and $\phi$. For the $B^0 (B^0)$, $\theta_t$ is the angle between the $\mu^+$ ($\mu^-$) and the opposite of the $B^0 (B^0)$ direction in the dimuon rest frame, $\theta_K$ the angle between the kaon and the direction opposite to the $B$ meson in the $K^{*0}$ rest frame, and $\phi$ the angle between the $\mu^+ \mu^-$ and $K^+ \pi^-$ decay planes in the $B$ rest frame. The inclusion of charge conjugate modes is implied throughout this Letter. At a given $q^2$, neglecting the muon mass, the normalized partial differential width integrated over $\theta_K$ and $\phi$ is

$$
\frac{1}{\Gamma} \frac{d^2\Gamma}{d\cos\theta_t dq^2} = \frac{3}{4} F_L(1 - \cos^2 \theta_t) + \frac{3}{8} (1 - F_L) (1 + \cos^2 \theta_t) + A_{FB} \cos \theta_t,
$$

and integrated over $\theta_t$ and $\phi$ it is

$$
\frac{1}{\Gamma} \frac{d^2\Gamma}{d\cos\theta_K dq^2} = \frac{3}{2} F_L \cos^2 \theta_K + \frac{3}{4} (1 - F_L)(1 - \cos^2 \theta_K).
$$

These expressions do not include any broad $S$-wave contribution to the $B^0 \rightarrow K^+ \pi^- \mu^+ \mu^-$ decay and any

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The angular and $q^2$ distributions. For example, no additional requirement is made on the $p_T$ of both of the muons, as, at low $q^2$, this would remove a large proportion of events with $|\cos \theta_K| \sim 1$. The BDT is trained entirely on data, using samples that are independent of that which is used to make the measurements: Triggered and fully reconstructed $B^0 \to J/\psi K^{*0}$ events are used as a proxy for the signal decay, and events from the upper $B^0 \to K^{*0} \mu^+ \mu^-$ mass sideband (5350 $< m_{K^+ \pi^- \mu^+ \mu^-} < 5600$ MeV/$c^2$) are used as a background sample. The lower mass sideband is not used, as it contains background events formed from partially reconstructed $B$ decays. These events make a negligible contribution in the signal region and have properties different from the combinatorial background which is the dominant background in this region.

A cut is made on the BDT output in order to optimize the sensitivity to $A_{FB}$ averaged over all $q^2$. The selected sample has a signal-to-background ratio of three to one.

Peaking backgrounds from $B^0 \to K^+ \mu^+ \mu^-$ (where $K \to \phi \mu^+ \mu^-$), $B^0 \to J/\psi K^{*0}$, and $B^0 \to \psi(2S)K^{*0}$ are considered and reduced with a set of vetoes. In each case, for the decay to be a potential signal candidate, at least one particle needs to be misidentified. For example, $B^0 \to J/\psi K^{*0}$ events where a kaon or pion is swapped for one of the muons peak around the nominal $B^0$ mass and evade the $J/\psi$ veto described above. Vetoes for each of these backgrounds are formed by changing the relevant particle mass hypotheses and recomputing the invariant masses and by making use of the particle identification information. In order to avoid having a strongly peaking contribution to the $cos \theta_K$ angular distribution in the upper mass sideband, $B^+ \to K^+ \mu^+ \mu^-$ candidates are removed. Events with $K^+ \mu^+ \mu^-$ invariant mass within 60 MeV/$c^2$ of the nominal $B^+$ mass are rejected. The vetoes for all of these peaking backgrounds remove a negligible amount of signal.

After the application of the BDT cut and the above vetoes, a fit is made to the $K^+ \pi^- \mu^+ \mu^-$ invariant mass distribution in the entire accepted mass range (see Fig. 1). A double-Gaussian distribution is used for the signal mass shape and an exponential function for the background. The signal shape is fixed from data using a fit to the $B^0 \to J/\psi K^{*0}$ mass peak. In the full $q^2$ range, in a signal mass window of $\pm 50$ MeV/$c^2$ ($\pm 2.5 \sigma$) around the measured $B^0$ mass, the fit gives an estimate of $337 \pm 21$ signal events with a background of $97 \pm 6$ events.

The residual peaking background is estimated by using simulated events. As detailed below, the accuracy of the
simulation is verified by comparing the particle (mis)identification probabilities with those derived from control channels selected from the data. The residual peaking backgrounds are reduced to a level of 6.1 events, i.e., 1.8% of the 337 observed signal events. The backgrounds from $B_0^0 \rightarrow \phi \mu^+ \mu^-$ and $B^0 \rightarrow J/\psi K^{*0}$ decays do not give rise to any forward-backward asymmetry and are ignored. However, in addition to the above backgrounds, $B_0^0 \rightarrow K^{*0} \mu^+ \mu^-$ decays with the kaon and pion swapped give rise to a 0.7% contribution. The change in the sign of the particle which is taken to be the kaon results in a $0.7\%$ contribution. The change in the sign of the particle which is taken to be the kaon results in a 0.7% contribution.

In order to obtain a positive probability density function over the entire angular range, Eqs. (1) and (2) imply that the conditions $|A_{FB}| \leq \frac{1}{2} (1 - F_L)$ and $0 < F_L < 1$ must be satisfied. To account for this, the maximum likelihood values for $A_{FB}$ and $F_L$ are extracted by performing a profile-likelihood scan over the allowed range. The uncertainty on the central value of $A_{FB}$ and $F_L$ is calculated by integrating the probability density extracted from the likelihood, assuming a flat prior in $A_{FB}$ and $F_L$, inside the allowed range. This gives an (asymmetric) 68% confidence interval.

The partial branching fraction is measured in each of the $q^2$ bins from a fit to the efficiency corrected $K^+ \pi^- \mu^+ \mu^-$ mass spectrum. The efficiencies are determined relative to the $B^0 \rightarrow J/\psi K^{*0}$ decay which is used as a normalization mode.

The event weighting and fitting procedure is validated by fitting the angular distribution of $B^0 \rightarrow J/\psi K^{*0}$ events, where the physics parameters are known from previous measurements [6]. The product of the $B^0 \rightarrow J/\psi K^{*0}$ and $J/\psi \rightarrow \mu^+ \mu^-$ branching fractions is ~75 times larger than the branching fraction of $B^0 \rightarrow K^{*0} \mu^+ \mu^-$, allowing a precise test of the procedure to be made. Fitting the $B^0 \rightarrow J/\psi K^{*0}$ angular distribution, weighted according to the event-by-event procedure described above, yields values for $F_L$ and $A_{FB}$ in good agreement with those found previously.

For $B^0 \rightarrow K^{*0} \mu^+ \mu^-$, the fit results for $A_{FB}$, $F_L$, and $d\overline{B}/dq^2$ are shown in Fig. 2 and are tabulated together with the signal and background yields in Table I. The fit projections are available online [7]. Signal candidates are observed in each $q^2$ bin with more than 5$f$ significance. The compatibility of the fits and the data are assessed by using a binned $\chi^2$ test, and all fits are found to be of good quality. The measurements in all three quantities are more precise than those of previous experiments and are in good agreement with the SM predictions. The predictions are taken from Ref. [8]. In the low $\sqrt{s}$ region, they rely on the factorization approach [9], which loses accuracy when approaching the $J/\psi$ resonance; in the high $\sqrt{s}$ region, an operator product expansion in the inverse $b$-quark mass, $1/m_b$, and in $1/\sqrt{q^2}$ is used [10], which is valid only above the open charm threshold. In both regions the form factor calculations are taken from Ref. [11], and a dimensional estimate is made on the uncertainty from expansion corrections [12].
previous measurements from the Belle, CDF, and BABAR Collaborations [2] which are, respectively, $A_{FB} = 0.26^{+0.27}_{-0.30} \pm 0.07$, $A_{FB} = 0.29^{+0.20}_{-0.23} \pm 0.07$, and, for $q^2 < 6.25$ GeV$^2/c^4$, $A_{FB} = 0.24^{+0.18}_{-0.23} \pm 0.05$. The positive value of $A_{FB}$ preferred in the $1.00 < q^2 < 0.00$ GeV$^2/c^4$ range in these previous measurements is not favored by the LHCb data. The previous measurements of $F_L$ in the same $q^2$ regions are $F_L = 0.67 \pm 0.23 \pm 0.05$ (Belle), $F_L = 0.69^{+0.19}_{-0.21} \pm 0.08$ (CDF), and $F_L = 0.35 \pm 0.16 \pm 0.04$ (BABAR). These are in good agreement with the LHCb result.

For the determination of $A_{FB}$ and $F_L$, the dominant systematic uncertainties arise from the event-by-event weights which are extracted from simulated events and from the model used to describe the angular distribution of the background. The uncertainty on the event-by-event weights is evaluated by fluctuating these weights within their statistical uncertainties and repeating the fitting procedure. The uncertainty from the background model which is used is estimated by changing this model to one which uses binned templates from the upper mass sideband rather than a polynomial parameterization.

The dominant systematic errors for the determination of $d\bar{B}/dq^2$ arise from the uncertainties on the particle identification and track reconstruction efficiencies. These efficiencies are extracted from control channels and are limited by the relevant sample sizes. The systematic uncertainty is estimated by fluctuating the efficiencies within the relevant uncertainties and repeating the fitting procedure. An additional systematic uncertainty of $\sim 4\%$ arises from the uncertainty in the $B^0 \to J/\psi K^0$ and $J/\psi \to \mu^+ \mu^-$ branching fractions [13].

The total systematic error on each of $A_{FB}$ and $F_L$ ($d\bar{B}/dq^2$) is typically $\sim 30\%$ (50%) of the statistical error and, hence, adds $\sim 4\%$ ($\sim 11\%$) to the total uncertainty.

In summary, by using $0.37$ fb$^{-1}$ of data taken with the LHCb detector during 2011, $A_{FB}$, $F_L$, and $d\bar{B}/dq^2$ have been determined for the decay $B^0 \to K^{*0} \mu^+ \mu^-$. These are the most precise measurements of these quantities to date.

![Figure 2](image-url)  
**FIG. 2** (color online). $A_{FB}$ (a), $F_L$ (b), and $d\bar{B}/dq^2$ (c) as a function of $q^2$. The SM prediction is given by the cyan (light) band, and this prediction rate-averaged across the $q^2$ bins is indicated by the purple (dark) regions. No SM prediction is shown for the region between the two regimes in which the theoretical calculations are made (see the text).

### TABLE I

Central values with statistical and systematic uncertainties for $A_{FB}$, $F_L$, and $d\bar{B}/dq^2$ as a function of $q^2$. The $B^0 \to K^{*0} \mu^+ \mu^-$ signal and background yields in the $\pm 50$ MeV/$c^2$ signal mass window with their statistical uncertainties are also indicated, together with the statistical significance of the signal peak that is observed. The significance is computed from the change in the likelihood, fitting with and without the signal component to the mass shape. In the case with the signal component, the signal shape is fixed from data using a fit to the $B^0 \to J/\psi K^{*0}$ mass peak.

<table>
<thead>
<tr>
<th>$q^2$ (GeV$^2/c^4$)</th>
<th>$A_{FB}$</th>
<th>$F_L$</th>
<th>$d\bar{B}/dq^2$ ($\times 10^{-7}$ c/$\text{GeV}^2$)</th>
<th>Signal yield</th>
<th>Background yield</th>
<th>Significance</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.10 &lt; $q^2$ &lt; 2.00</td>
<td>-0.15 ± 0.20 ± 0.06</td>
<td>0.00 ± 0.13 ± 0.02</td>
<td>0.61 ± 0.12 ± 0.06</td>
<td>48.6 ± 8.1</td>
<td>16.2 ± 2.3</td>
<td>8.6</td>
</tr>
<tr>
<td>2.00 &lt; $q^2$ &lt; 4.30</td>
<td>0.05 ± 0.18 ± 0.04</td>
<td>0.77 ± 0.15 ± 0.03</td>
<td>0.34 ± 0.09 ± 0.02</td>
<td>26.5 ± 6.5</td>
<td>15.7 ± 2.2</td>
<td>5.4</td>
</tr>
<tr>
<td>4.30 &lt; $q^2$ &lt; 8.68</td>
<td>0.27 ± 0.09 ± 0.02</td>
<td>0.60 ± 0.07 ± 0.01</td>
<td>0.69 ± 0.08 ± 0.05</td>
<td>104.7 ± 11.9</td>
<td>31.7 ± 3.3</td>
<td>12.4</td>
</tr>
<tr>
<td>10.09 &lt; $q^2$ &lt; 12.86</td>
<td>0.27 ± 0.08 ± 0.02</td>
<td>0.41 ± 0.11 ± 0.03</td>
<td>0.55 ± 0.09 ± 0.07</td>
<td>62.2 ± 9.2</td>
<td>20.4 ± 2.6</td>
<td>9.6</td>
</tr>
<tr>
<td>14.18 &lt; $q^2$ &lt; 16.00</td>
<td>0.47 ± 0.08 ± 0.03</td>
<td>0.37 ± 0.09 ± 0.05</td>
<td>0.62 ± 0.09 ± 0.05</td>
<td>42.2 ± 7.0</td>
<td>4.2 ± 1.3</td>
<td>10.2</td>
</tr>
<tr>
<td>16.00 &lt; $q^2$ &lt; 19.00</td>
<td>0.16 ± 0.11 ± 0.06</td>
<td>0.26 ± 0.08 ± 0.03</td>
<td>0.50 ± 0.08 ± 0.05</td>
<td>53.4 ± 8.1</td>
<td>7.0 ± 1.7</td>
<td>9.8</td>
</tr>
<tr>
<td>1.00 &lt; $q^2$ &lt; 6.00</td>
<td>-0.06 ± 0.13 ± 0.04</td>
<td>0.55 ± 0.10 ± 0.03</td>
<td>0.42 ± 0.06 ± 0.03</td>
<td>76.5 ± 10.6</td>
<td>33.1 ± 3.2</td>
<td>9.9</td>
</tr>
</tbody>
</table>
All three observables show good agreement with the SM predictions.

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(LHCb Collaboration)

1Centro Brasileiro de Pesquisas Físicas (CBPF), Rio de Janeiro, Brazil
2Universidade Federal do Rio de Janeiro (UFRJ), Rio de Janeiro, Brazil
3Center for High Energy Physics, Tsinghua University, Beijing, China
4LAPP, Université de Savoie, CNRS/IN2P3, Annecy-Le-Vieux, France
5Clermont Université, Université Blaise Pascal, CNRS/IN2P3, LPC, Clermont-Ferrand, France
6CPPM, Aix-Marseille Université, CNRS/IN2P3, Marseille, France
7LAL, Université Paris-Sud, CNRS/IN2P3, Orsay, France
8LPNHE, Université Pierre et Marie Curie, Université Paris Diderot, CNRS/IN2P3, Paris, France
9Fakultät Physik, Technische Universität Dortmund, Dortmund, Germany
10Max-Planck-Institut für Kernphysik (MPIK), Heidelberg, Germany
11Physikalisches Institut, Ruprecht-Karls-Universität Heidelberg, Heidelberg, Germany
12School of Physics, University College Dublin, Dublin, Ireland
13Sezione INFN di Bari, Bari, Italy
14Sezione INFN di Bologna, Bologna, Italy
15Sezione INFN di Cagliari, Cagliari, Italy
16Sezione INFN di Ferrara, Ferrara, Italy
17Sezione INFN di Firenze, Firenze, Italy
18Laboratori Nazionali dell’INFN di Frascati, Frascati, Italy
19Sezione INFN di Genova, Genova, Italy
20Sezione INFN di Milano Bicocca, Milano, Italy
21Sezione INFN di Roma Tor Vergata, Roma, Italy
22Sezione INFN di Roma La Sapienza, Roma, Italy
23Nikhef National Institute for Subatomic Physics, Amsterdam, The Netherlands
24Nikhef National Institute for Subatomic Physics and Vrije Universiteit, Amsterdam, The Netherlands
25Henryk Niewodniczanski Institute of Nuclear Physics Polish Academy of Sciences, Kraków, Poland
26AGH University of Science and Technology, Kraków, Poland
27Soltan Institute for Nuclear Studies, Warsaw, Poland
28Horia Hulubei National Institute of Physics and Nuclear Engineering, Bucharest-Magurele, Romania
29Petersburg Nuclear Physics Institute (PNPI), Gatchina, Russia
30Institute of Theoretical and Experimental Physics (ITEP), Moscow, Russia
31Institute of Nuclear Physics, Moscow State University (SINP MSU), Moscow, Russia
32Institute for Nuclear Research of the Russian Academy of Sciences (INR RAN), Moscow, Russia
33Budker Institute of Nuclear Physics (SB RAS) and Novosibirsk State University, Novosibirsk, Russia
34Institute for High Energy Physics (IHEP), Protvino, Russia
35Universitat de Barcelona, Barcelona, Spain
36Universidad de Santiago de Compostela, Santiago de Compostela, Spain
37European Organization for Nuclear Research (CERN), Geneva, Switzerland
38Ecole Polytechnique Fédérale de Lausanne (EPFL), Lausanne, Switzerland
39Physik-Institut, Universität Zürich, Zürich, Switzerland
40NSC Kharkiv Institute of Physics and Technology (NSC KIPT), Kharkiv, Ukraine
41Institute for Nuclear Research of the National Academy of Sciences (KINR), Kyiv, Ukraine
42H. H. Wills Physics Laboratory, University of Bristol, Bristol, United Kingdom
43Cavendish Laboratory, University of Cambridge, Cambridge, United Kingdom
44Department of Physics, University of Warwick, Coventry, United Kingdom
45STFC Rutherford Appleton Laboratory, Didcot, United Kingdom
46School of Physics and Astronomy, University of Edinburgh, Edinburgh, United Kingdom
47School of Physics and Astronomy, University of Glasgow, Glasgow, United Kingdom
48Oliver Lodge Laboratory, University of Liverpool, Liverpool, United Kingdom
49Imperial College London, London, United Kingdom
50School of Physics and Astronomy, University of Manchester, Manchester, United Kingdom
51Department of Physics, University of Oxford, Oxford, United Kingdom
52Syracuse University, Syracuse, New York, USA
53CC-IN2P3, CNRS/IN2P3, Lyon-Villeurbanne, France, associated member
54Pontifícia Universidade Católica do Rio de Janeiro (PUC-Rio), Rio de Janeiro, Brazil, associated to Universidade Federal do Rio de Janeiro (UFRJ), Rio de Janeiro, Brazil
55University of Birmingham, Birmingham, United Kingdom
Physikalisches Institut, Universität Rostock, Rostock, Germany, associated to Physikalisches Institut, Ruprecht-Karls-Universität Heidelberg, Heidelberg, Germany

Also at P. N. Lebedev Physical Institute, Russian Academy of Science (LPI RAS), Moscow, Russia.

Also at Università di Bari, Bari, Italy.

Also at Università di Bologna, Bologna, Italy.

Also at Università di Cagliari, Cagliari, Italy.

Also at Università di Ferrara, Ferrara, Italy.

Also at Università di Firenze, Firenze, Italy.

Also at Università di Urbino, Urbino, Italy.

Also at Università di Modena e Reggio Emilia, Modena, Italy.

Also at Università di Genova, Genova, Italy.

Also at Università di Milano Bicocca, Milano, Italy.

Also at Università di Roma Tor Vergata, Roma, Italy.

Also at Università di Roma La Sapienza, Roma, Italy.

Also at Università della Basilicata, Potenza, Italy.

Also at LIFAELS, La Salle, Universitat Ramon Llull, Barcelona, Spain.

Also at Hanoi University of Science, Hanoi, Vietnam.