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Study of Beauty Hadron Decays into Pairs of Charm Hadrons

R. Aaij et al.*
(LHCb Collaboration)
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First observations of the decays \( \Lambda_b^0 \to \Lambda_c^+ D_{(s)}^- \) are reported using data corresponding to an integrated luminosity of 3 fb\(^{-1} \) collected at 7 and 8 TeV center-of-mass energies in proton-proton collisions with the LHCb detector. In addition, the most precise measurement of the branching fraction \( B(B^0 \to D^+ D_s^-) \) is made and a search is performed for the decays \( B^0 \to \Lambda_c^+ \Lambda_c^- \). The results obtained are

\[
\frac{\mathcal{B}(\Lambda_b^0 \to \Lambda_c^+ D_{(s)}^-)/\mathcal{B}(\Lambda_b^0 \to \Lambda_c^+ D_{(s)}^-)}{\mathcal{B}(\Lambda_b^0 \to \Lambda_c^+ \pi^-)/\mathcal{B}(\Lambda_b^0 \to \Lambda_c^+ \pi^-)} = 0.042 \pm 0.003\text{(stat)} \pm 0.003\text{(syst)},
\]

\[
\frac{\mathcal{B}(\Lambda_b^0 \to \Lambda_c^+ D_{(s)}^-)}{\mathcal{B}(\Lambda_b^0 \to \Lambda_c^+ \pi^-)} = 0.96 \pm 0.02\text{(stat)} \pm 0.06\text{(syst)},
\]

\[
\mathcal{B}(B^0 \to D^+ D_s^-)/\mathcal{B}(B^0 \to D^+ D_s^-) = 0.038 \pm 0.004\text{(stat)} \pm 0.003\text{(syst)},
\]

\[
\mathcal{B}(B^0 \to \Lambda_c^+ \Lambda_c^-)/\mathcal{B}(B^0 \to D^+ D^-) < 0.0022\text{[95\% C.L.]},
\]

\[
\mathcal{B}(B^0 \to \Lambda_c^+ \Lambda_c^-)/\mathcal{B}(B^0 \to D^+ D^-) < 0.30\text{[95\% C.L.]}.
\]

Measurement of the mass of the \( \Lambda_b^0 \) baryon relative to the \( \bar{B}^0 \) meson gives \( M(\Lambda_b^0) - M(\bar{B}^0) = 339.72 \pm 0.24\text{(stat)} \pm 0.18\text{(syst)} \text{ MeV}/c^2 \). This result provides the most precise measurement of the mass of the \( \Lambda_b^0 \) baryon to date.

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Hadrons are systems of quarks bound by the strong interaction, described at the fundamental level by quantum chromodynamics (QCD). Low-energy phenomena, such as the binding of quarks and gluons within hadrons, lie in the nonperturbative regime of QCD and are difficult to calculate. Much progress has been made in recent years in the study of beauty mesons [1]; however, many aspects of beauty baryons are still largely unknown. Many decays of beauty mesons into pairs of charm hadrons have branching fractions at the percent level [2]. Decays of beauty baryons into pairs of charm hadrons are expected to be of comparable size, yet none have been observed to date. If such decays do have sizable branching fractions, they could be used to study beauty-baryon properties. For example, a comparison of beauty meson and baryon branching fractions can be used to test factorization in these decays [3].

Many models and techniques have been developed that attempt to reproduce the spectrum of the measured hadron masses, such as constituent-quark models or lattice QCD calculations [4]. Precise measurements of ground-state beauty-baryon masses are required to permit precision tests of a variety of QCD models [5–11]. The \( \Lambda_b^0 \) baryon mass is particularly interesting in this context, since several ground-state beauty-baryon masses are measured relative to that of the \( \Lambda_b^0 \) [12].

This Letter reports the first observation of the decays \( \Lambda_b^0 \to \Lambda_c^+ D_s^- \) and \( \Lambda_b^0 \to \Lambda_c^+ D^- \). The decay \( \Lambda_b^0 \to \Lambda_c^+ D_s^- \) is used to make the most precise measurement to date of the mass of the \( \Lambda_b^0 \) baryon. Improved measurements of the branching fraction \( \mathcal{B}(B^0 \to D^+ D_s^-) \) and stringent upper limits on \( \mathcal{B}(B^0 \to \Lambda_c^+ \Lambda_c^-) \) are also reported. Charge conjugated decay modes are implied throughout this Letter. The data used correspond to an integrated luminosity of 1 and 2 fb\(^{-1} \) collected at 7 and 8 TeV center-of-mass energies in \( pp \) collisions, respectively, with the LHCb detector.

The LHCb detector is a single-arm forward spectrometer covering the pseudorapidity range \( 2 < \eta < 5 \), described in detail in Refs. [13–18]. Samples of simulated events are used to determine selection efficiencies, to model candidate distributions, and to investigate possible background contributions. In the simulation, \( pp \) collisions are generated using PYTHIA [19] with a specific LHCb configuration [20]. Decays of hadronic particles are described by EVTGEN [21], in which final-state radiation is generated using PHOTOS [22]. The interaction of the generated particles with the detector and its response are implemented using the GEANT4 toolkit [23] as described in Ref. [24].

In this analysis, signal beauty-hadron candidates are formed by combining charm-hadron candidate pairs reconstructed in the following decay modes: \( D^+ \to K^-\pi^-\pi^+ \), \( D_s^+ \to K^-K^+\pi^+ \), and \( \Lambda_c^+ \to pK^-\pi^+ \). The measured invariant mass of each charm-hadron candidate, the resolution on

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* Full author list given at the end of the article.

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which is about 6–8 MeV/c^2, is required to be within 25 MeV/c^2 of the nominal value [2]. To improve the resolution of the beauty-hadron mass, the decay chain is fit imposing kinematic and vertex constraints [25]; this includes constraining the charm-hadron masses to their nominal values. To suppress contributions from noncharm decays, the reconstructed charm-hadron decay vertex is required to be downstream of, and significantly displaced from, the reconstructed beauty-hadron decay vertex.

A boosted decision tree (BDT) [26] is used to select each type of charm-hadron candidate. These BDTs use five variables for the charm hadron and 23 for each of its decay products. The variables include kinematic quantities, track and vertex qualities, and particle identification (PID) information. The signal samples used to train the BDTs are obtained from large data sets of \( \bar{B}^0 \to D^+ \pi^- \), \( B^0 \to D^+ \pi^- \), and \( \Lambda_c^0 \to \Lambda_c^+ \pi^- \) decays that are background subtracted using weights [27] obtained from fits to the beauty-hadron invariant mass distributions. The background data samples are taken from the charm-hadron and high-mass beauty-hadron sidebands in the same data sets. To obtain the BDT efficiency in a given signal decay mode, the kinematical properties and correlations between the two charm hadrons are taken from simulation. The BDT response distributions are obtained from independent data samples of the decays used in the BDT training, weighted to match the kinematics of the signal.

Because of the kinematic similarity of the decays \( D^+ \to K^- \pi^+ \pi^+ \), \( D_{s1}^+ \to K^- \pi^+ \), and \( \Lambda_c^+ \to pK^- \pi^+ \), cross feed may occur among beauty-hadron decays into pairs of charm hadrons. For example, cross feed between \( D_s^+ \) and \( D_{s2}^+ \) mesons occurs when a \( K^- h^\pi^+ \) candidate is reconstructed in the \( D_s^+ \) mass region under the \( h^\pi^+ = \pi^+ \) hypothesis and in the \( D_{s2}^+ \) mass region under the \( h^\pi^+ = K^+ \) hypothesis. In such situations, an arbitration is performed: if the ambiguous track \( (h^\pi^+) \) can be associated to an oppositely charged track to form a \( \phi(1020) \to K^+ K^- \) candidate, the kaon hypothesis is taken, resulting in a \( D_s^+ \) assignment to the charm-hadron candidate; otherwise, stringent PID requirements are applied to \( h^\pi^+ \) to choose which hypothesis to take. The efficiency of these arbitrations, which is found to be about 90% per charm hadron, is obtained using simulated signal decays to model the kinematical properties and \( D^+ \to D^0 \pi^+ \) calibration data for the PID efficiencies. The misidentification probability is roughly 1% per charm hadron.

Signal yields are determined by performing unbinned extended likelihood fits to the beauty-hadron invariant-mass spectra observed in the data. The signal distributions are modeled using a so-called Apollonios function, which is the exponential of a hyperbola combined with a power-law low-mass tail [28]. The peak position and resolution parameters are allowed to vary while fitting the data, while the low-mass tail parameters are taken from simulation and fixed in the fits.

Four categories of background contributions are considered: partially reconstructed decays of beauty hadrons where at least one final-state particle is not reconstructed; decays into a single charm hadron and three light hadrons; reflections, defined as cases where the cross-feed arbitration fails to remove a misidentified particle; and combinatorial background. The only partially reconstructed decays that contribute in the mass region studied are those where a single pion or photon is not reconstructed; thus, only final states comprised of \( D_{s2}^+ \) or \( \Sigma_c^+ \) and another charm hadron are considered (e.g., \( \Lambda_b^0 \to \Lambda_c^+ D_{s2}^- \)). These background contributions are modeled using kernel probability density functions (PDFs) [29] obtained from simulation; their yields are free to vary in the fits. Single-charm backgrounds are studied using data that are reconstructed outside of a given charm-hadron mass region. These backgrounds are found to be \( O(1\%) \) of the size of the signal yield for signal decays containing a \( D_s^+ \) (e.g., \( \bar{B}^0 \to D^+ K^- \pi^- \)) and are negligible otherwise. The only non-negligible reflection is found to be \( \Lambda_b^0 \to \Lambda_c^+ D^- \) candidates misidentified as \( \Lambda_c^+ D^- \) candidates. The invariant-mass distribution for this reflection is obtained from simulation, while the normalization is fixed using simulation and the aforementioned PID calibration sample to determine the fraction of \( \Lambda_b^0 \to \Lambda_c^+ D^- \) decays that are not removed by the cross-feed criteria. Reflections of \( \bar{B}^0 \to D^+ D^- \) decays misidentified as final states containing \( \Lambda_c^+ \) particles do not have a peaking structure in the beauty-hadron invariant mass and, therefore, are absorbed into the combinatorial backgrounds, which are modeled using exponential distributions.

Figure 1 shows the invariant mass spectra for the \( \Lambda_b^0 \to \Lambda_c^+ D^- \) and \( \Lambda_b^0 \to \Lambda_c^+ D^- \) candidates. The signal yields obtained are 4633 \( \pm \) 69 and 262 \( \pm \) 19 for \( \Lambda_b^0 \to \Lambda_c^+ D^- \) and \( \Lambda_b^0 \to \Lambda_c^+ D^- \), respectively. This is the first observation of each of these decays. The ratio of branching fractions determined using the nominal \( D_s^+ \) [2] and \( D^- \) [30] meson branching fractions and the ratio of efficiencies is

\[
\frac{B(\Lambda_b^0 \to \Lambda_c^+ D^-)}{B(\Lambda_b^0 \to \Lambda_c^+ D^-)} = 0.042 \pm 0.003(\text{stat}) \pm 0.003(\text{syst}).
\]

The similarity of the final states and the shared parent particle result in many cancellations of uncertainties in the determination of the ratio of branching fractions. The remaining uncertainties include roughly equivalent contributions from determining the efficiency-corrected yields and from the ratio of charm-hadron branching fractions (see Table I). The dominant contribution to the uncertainty of the fit PDF is due to the low-mass background contributions, which are varied in size and shape to determine the effect on the signal yield. The uncertainty due to signal model is found to be negligible. The efficiencies of the cross feed and BDT criteria are determined in a data-driven manner that produces small uncertainties. The observed ratio is approximately the ratio of the relevant quark-mixing
depends on the determined relative to that of the served (see Fig. 2). The measurement of $B$ in Table I. The uncertainty in the fit model is due largely to fractions. The systematic uncertainties on this result are listed
production cross sections or on any charm-hadron branching

FIG. 1 (color online). Invariant mass distributions for (left) $\Lambda_b^0 \to \Lambda_c^+ D_s^-$ and (right) $\Lambda_b^0 \to \Lambda_c^+ D_s^-$ candidates with the fits described in the text overlaid.

The kinematic and vertex constraints used in the fits described previously reduce the statistical uncertainty of the beauty hadrons [32]. Figure 3 shows the ratio of efficiency-corrected yields, $N(\Lambda_b^0 \to \Lambda_c^+ D_s^-)/N(B^0 \to D^+ D_s^-)$, as a function of beauty-hadron $p_T$. The ratio of branching-fraction ratios is obtained using a fit with the shape of the $p_T$ dependence measured in $B(\Lambda_b^0 \to \Lambda_c^+ \pi^-)/B(B^0 \to D^+ \pi^-)$ [33] and found to be

$$\left[ \frac{B(\Lambda_b^0 \to \Lambda_c^+ D_s^-)}{B(B^0 \to D^+ D_s^-)} \right] / \left[ \frac{B(\Lambda_b^0 \to \Lambda_c^+ \pi^-)}{B(B^0 \to D^+ \pi^-)} \right] = 0.96 \pm 0.02 \text{(stat)} \pm 0.06 \text{(syst)}.$$

This result does not depend on the absolute ratio of production cross sections or on any charm-hadron branching fractions. The systematic uncertainties on this result are listed in Table I. The uncertainty in the fit model is due largely to the sizable single-charm background contributions to these modes and to contributions from the fits described in Ref. [33]. The $B(\Lambda_b^0 \to \Lambda_c^+ \pi^-)/B(B^0 \to D^+ \pi^-)$ result was obtained only using data collected at $\sqrt{s} = 7$ TeV. The ratio $N(\Lambda_b^0 \to \Lambda_c^+ D_s^-)/N(B^0 \to D^+ D_s^-)$ is observed to be consistent in data collected at $\sqrt{s} = 7$ and 8 TeV. The statistical uncertainty on this comparison is assigned as the systematic uncertainty on the energy dependence of the $\Lambda_b^0$ and $B^0$ production fractions. The ratio of branching ratios is consistent with unity, as expected assuming small nonfactorizable effects.

The kinematic similarity of the decay modes $\Lambda_b^0 \to \Lambda_c^+ D_s^-$ and $B^0 \to D^+ D_s^-$ permits a precision measurement of the mass difference of the $\Lambda_b^0$ and $B^0$ hadrons. The relatively small value of $[M(\Lambda_b^0) - M(\Lambda_c^+) - M(D_s^-)] - [M(B^0) - M(D^+) - M(D_s^-)]$ means that the uncertainty due to momentum scale, the dominant uncertainty in absolute-mass measurements, mostly cancels; however, it is still important to determine accurately the momenta of the final-state particles. The momentum-scale calibration of the spectrometer, which accounts for imperfect knowledge of the magnetic field and alignment, is discussed in detail in Refs. [12,34]. The uncertainty on the calibrated momentum scale is estimated to be 0.03% by comparing various particle masses measured at LHCb to their nominal values [34].

The kinematic and vertex constraints used in the fits described previously reduce the statistical uncertainty on $M(\Lambda_b^0) - M(B^0)$ by improving the resolution. These

| Source | $B(\Lambda_b^0 \to \Lambda_c^+ D_s^-)$ \cite{33} | $B(\Lambda_b^0 \to \Lambda_c^+ D_s^-)$ \cite{33} | $B(\Lambda_b^0 \to \Lambda_c^+ D_s^-)$ \cite{33} | $B(\Lambda_b^0 \to \Lambda_c^+ D_s^-)$ \cite{33} | $B(\Lambda_b^0 \to \Lambda_c^+ D_s^-)$ \cite{33} | $B(\Lambda_b^0 \to \Lambda_c^+ D_s^-)$ \cite{33} | $B(\Lambda_b^0 \to \Lambda_c^+ D_s^-)$ \cite{33} |
|---|---|---|---|---|
| Efficiency | 3.5 | 5.2 | 1.0 | 3.9 (5.0) |
| Fit model | 3.0 | 2.6 | 3.0 | ... |
| $B(D_s^\pm, \Lambda_c^+)$ | 5.2 | ... | ... | 8.8 |
| $\sigma(B_s^0)/\sigma(B^0)$ | ... | 5.8 | ... | ... |
| $\sigma(\Lambda_b^0)/\sigma(B^0)$ | ... | 2.0 | ... | ... |
| Total | 6.9 | 6.1 | 6.6 | 9.6 (10.1) |
constraints also increase the systematic uncertainty by introducing a dependence on the precision of the nominal charm-hadron masses. These constraints are not imposed in the mass measurement, as it is found that this approach produces a smaller total uncertainty. The mass difference obtained is

\[
M(\Lambda_b^0) - M(\bar{B}^0) = 339.72 \pm 0.24(\text{stat}) \\
+ 0.18(\text{syst}) \text{ MeV}/c^2.
\]

The dominant systematic uncertainty (see Table II) arises due to a correlation between the reconstructed beauty-hadron mass and reconstructed charm-hadron flight distance. The large difference in the \(\Lambda_c^+\) and \(D^+\) hadron lifetimes [2] could lead to only a partial cancellation of the biases induced by the charm-lifetime selection criteria. This effect is studied in simulation and a 0.16 MeV/c\(^2\) uncertainty is assigned. The 0.03% uncertainty in the momentum scale results in an uncertainty on the mass difference of 0.08 MeV/c\(^2\). Many variations in the fit model are considered, and none produce a significant shift in the mass difference. The systematic uncertainty in the mass difference due to the uncertainty in the amount of detector material in which charged particles lose energy is negligible [34]. Furthermore, the uncertainty on \(M(\Lambda_b^0) - M(\bar{B}^0)\) due to differences in beauty-hadron production kinematics, as seen in Fig. 3, is also found to be negligible.

Using the nominal value for \(M(\bar{B}^0)[2]\) gives \(M(\Lambda_b^0) = 5619.30 \pm 0.34 \text{ MeV}/c^2\), where the uncertainty includes both statistical and systematic contributions. This is the most precise result to date. The total uncertainty is dominated by statistics and charm-hadron lifetime effects; thus, this result can be treated as being uncorrelated with the previous LHCb result obtained using the \(\Lambda_b^0 \to J/\psi \Lambda^0\) decay [35]. A weighted average of the LHCb results gives \(M(\Lambda_b^0) = 5619.36 \pm 0.26 \text{ MeV}/c^2\). This value may then be used to improve the precision of the \(\Xi_c^-\) and \(\Omega_c^-\) baryons using their mass differences with respect to the \(\Lambda_b^0\) baryon, as reported in Ref. [35].

Using BDT criteria optimized for maximizing the expected significance of \(\bar{B}^0 \to D^+ D_s^-\), 14608 \(\pm\) 121 \(\bar{B}^0\) and 143 \(\pm\) 14 \(\bar{B}^0\) decays are observed (see Fig. 2), from which the ratio extracted is

\[
\frac{\mathcal{B}(\bar{B}^0 \to D^+ D_s^-)}{\mathcal{B}(\bar{B}^0 \to D^+ D_s^-)} = 0.038 \pm 0.004(\text{stat}) \pm 0.003(\text{syst}).
\]

This is the most precise measurement to date of \(\mathcal{B}(\bar{B}^0 \to D^+ D_s^-)\) and supersedes Ref. [36]. Since the two decay modes share the same final state, many systematic uncertainties cancel. The dominant contribution to the uncertainty comes from the beauty-hadron production fractions.

### Table II. Systematic uncertainties for \(M(\Lambda_b^0) - M(\bar{B}^0)\).

<table>
<thead>
<tr>
<th>Description</th>
<th>Value (MeV/c(^2))</th>
</tr>
</thead>
<tbody>
<tr>
<td>(\Lambda_c^+ - D^+) lifetime difference</td>
<td>0.16</td>
</tr>
<tr>
<td>Momentum scale</td>
<td>0.08</td>
</tr>
<tr>
<td>Fit model</td>
<td>0.02</td>
</tr>
<tr>
<td>Total</td>
<td>0.18</td>
</tr>
</tbody>
</table>

![FIG. 3 (color online). Efficiency-corrected ratio of the yields of \(\Lambda_b^0 \to \Lambda_c^+ D^-\) and \(\bar{B}^0 \to D^+ D_s^-\) vs \(p_T\). The points are located at the mean \(p_T\) value of the \(\Lambda_b^0\) in each bin. The curve shows the data fit with the shape of the \(p_T\) dependence measured in Ref. [33].](image-url)
A small additional uncertainty on the efficiency arises due to the uncertainty on the \(B^0\) lifetime. Uncertainty in the fit model is largely due to the size of the combinatorial background near the \(B^0\) peak. The measured ratio of branching fractions is approximately the ratio of quark-mixing factors, as expected assuming nonfactorizable effects are small.

A search is also performed for the decay modes \(B^0_{(s)} \rightarrow \bar{\Lambda}_c^+ \Lambda_c^-\). Regions centered around the nominal \(B^0_{(s)}\) meson masses with boundaries defined such that each region contains 95% of the corresponding signal are determined using simulation. The expected background contribution in each of these regions is obtained from the charm-hadron mass sidebands. Applying this technique to the \(\bar{B}^0 \rightarrow D^+ D_s^-\) and \(\Lambda_b^0 \rightarrow \bar{\Lambda}_c^+ D_s^-(s)\) decays produces background estimates consistent with those obtained by fitting the invariant mass spectra for those modes. The number of observed candidates in each signal region is then compared to the expected background contribution; no significant excess is observed in either \(\bar{\Lambda}_c^+ \Lambda_c^-\) signal region. The limits obtained using the method of Ref. [37] and the known \(D_s^-\), \(D^-\) \cite{[2]}, \(D^-\) \cite{[30]}, and \(\Lambda_c^-\) \cite{[38]} hadron branching fractions are

\[
\frac{B(\bar{B}^0 \rightarrow \bar{\Lambda}_c^+ \Lambda_c^-)}{B(\bar{B}^0 \rightarrow D^+ D_s^-)} < 0.0022(95\% \text{ C.L.},
\]

\[
\frac{B(B^0 \rightarrow \bar{\Lambda}_c^+ \Lambda_c^-)}{B(B^0 \rightarrow D^+ D_s^-)} < 0.30(95\% \text{ C.L.}).
\]

For these results the lifetime of the light-mass \(B^0\) eigenstate is assumed, as this produces the most conservative limits \cite{[1]}. This is the best limit to date for the \(\bar{B}^0\) decay mode and the first limit for the \(B^0\) decay mode.

In summary, first observations and relative branching-fraction measurements have been made for the decays \(\Lambda_b^0 \rightarrow \Lambda_c^+ D_s^-\). The most precise measurements of the \(\Lambda_b^0\) baryon mass and of \(B(B^0_{(s)} \rightarrow D^+ D_s^-)\) have been presented and the most stringent upper limits have been placed on \(B(B^0 \rightarrow \Lambda_c^+ \Lambda_c^-)\). Using \(B(\bar{B}^0 \rightarrow D^+ D_s^-) = (7.2 \pm 0.8) \times 10^{-3}\) \cite{[2]} and \(B(\Lambda_b^0 \rightarrow \Lambda_c^+ \pi^-) / B(\bar{B}^0 \rightarrow D^+ \pi^-)\) from Ref. [33], the absolute branching fractions obtained are

\[
B(\Lambda_b^0 \rightarrow \bar{\Lambda}_c^+ D_s^-) = (1.1 \pm 0.1) \times 10^{-2},
\]

\[
B(\Lambda_b^0 \rightarrow \Lambda_c^+ D^-) = (4.7 \pm 0.6) \times 10^{-4},
\]

\[
B(B^0 \rightarrow D^+ D^-) = (2.7 \pm 0.5) \times 10^{-4},
\]

\[
B(B^0 \rightarrow \Lambda_c^+ \Lambda_c^-) < 1.6 \times 10^{-5}(95\% \text{ C.L.}),
\]

\[
B(B^0_{(s)} \rightarrow \Lambda_c^+ \Lambda_c^-) < 8.0 \times 10^{-5}(95\% \text{ C.L.}).
\]

These results are all consistent with expectations that assume small nonfactorizable effects.

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(LHCb Collaboration)

1 Centro Brasileiro de Pesquisas Físicas (CBPF), Rio de Janeiro, Brazil  
2 Universidade Federal do Rio de Janeiro (UFRJ), Rio de Janeiro, Brazil  
3 Center for High Energy Physics, Tsinghua University, Beijing, China  
4 LAPP, Université de Savoie, CNRS/IN2P3, Annecy-Le-Vieux, France  
5 Clermont Université, Université Blaise Pascal, CNRS/IN2P3, LPC, Clermont-Ferrand, France  
6 CPPM, Aix-Marseille Université, CNRS/IN2P3, Marseille, France  
7 LAL, Université Paris-Sud, CNRS/IN2P3, Orsay, France  
8 LPNHE, Université Pierre et Marie Curie, Université Paris Diderot, CNRS/IN2P3, Paris, France  
9 Fakultät Physik, Technische Universität Dortmund, Dortmund, Germany  
10 Max-Planck-Institut für Kernphysik (MPIK), Heidelberg, Germany  
11 Physikalisches Institut, Ruprecht-Karls-Universität Heidelberg, Heidelberg, Germany  
12 School of Physics, University College Dublin, Dublin, Ireland  
13 Sezione INFN di Bari, Bari, Italy  
14 Sezione INFN di Bologna, Bologna, Italy  
15 Sezione INFN di Catania, Catania, Italy  
16 Sezione INFN di Ferrara, Ferrara, Italy  
17 Sezione INFN di Firenze, Firenze, Italy  
18 Laboratori Nazionali dell’INFN di Frascati, Frascati, Italy  
19 Sezione INFN di Genova, Genova, Italy  
20 Sezione INFN di Milano Bicocca, Milano, Italy  
21 Sezione INFN di Milano, Milano, Italy  
22 Sezione INFN di Padova, Padova, Italy  
23 Sezione INFN di Pisa, Pisa, Italy  
24 Sezione INFN di Roma Tor Vergata, Roma, Italy  
25 Sezione INFN di Roma La Sapienza, Roma, Italy  
26 Henryk Niewodniczanski Institute of Nuclear Physics Polish Academy of Sciences, Kraków, Poland  
27 AGH - University of Science and Technology, Faculty of Physics and Applied Computer Science, Kraków, Poland  
28 National Center for Nuclear Research (NCBJ), Warsaw, Poland  
29 Horia Hulubei National Institute of Physics and Nuclear Engineering, Bucharest-Magurele, Romania  
30 Petersburg Nuclear Physics Institute (PNPI), Gatchina, Russia  
31 Institute of Theoretical and Experimental Physics (ITEP), Moscow, Russia  
32 Institute of Nuclear Physics, Moscow State University (SINP MSU), Moscow, Russia  
33 Institute for Nuclear Research of the Russian Academy of Sciences (INR RAN), Moscow, Russia  
34 Budker Institute of Nuclear Physics (SB RAS) and Novosibirsk State University, Novosibirsk, Russia  
35 Institute for High Energy Physics (IHEP), Protvino, Russia  
36 Universitat de Barcelona, Barcelona, Spain  
37 Universidad de Santiago de Compostela, Santiago de Compostela, Spain  
38 European Organization for Nuclear Research (CERN), Geneva, Switzerland  
39 Ecole Polytechnique Fédérale de Lausanne (EPFL), Lausanne, Switzerland  
40 Physik-Institut, Universität Zürich, Zürich, Switzerland  
41 Nikhef National Institute for Subatomic Physics, Amsterdam, The Netherlands  
42 Nikhef National Institute for Subatomic Physics and VU University Amsterdam, Amsterdam, The Netherlands  
43 NSC Kharkiv Institute of Physics and Technology (NSC KIPT), Kharkiv, Ukraine  
44 Institute for Nuclear Research of the National Academy of Sciences (KINR), Kyiv, Ukraine  
45 University of Birmingham, Birmingham, United Kingdom  
46 H.H. Wills Physics Laboratory, University of Bristol, Bristol, United Kingdom  
47 Cavendish Laboratory, University of Cambridge, Cambridge, United Kingdom  
48 Department of Physics, University of Warwick, Coventry, United Kingdom  
49 STFC Rutherford Appleton Laboratory, Didcot, United Kingdom
School of Physics and Astronomy, University of Edinburgh, Edinburgh, United Kingdom
School of Physics and Astronomy, University of Glasgow, Glasgow, United Kingdom
Oliver Lodge Laboratory, University of Liverpool, Liverpool, United Kingdom
Imperial College London, London, United Kingdom
School of Physics and Astronomy, University of Manchester, Manchester, United Kingdom
Department of Physics, University of Oxford, Oxford, United Kingdom
Massachusetts Institute of Technology, Cambridge, Massachusetts, USA
University of Cincinnati, Cincinnati, Ohio, USA
University of Maryland, College Park, Maryland, USA
Syracuse University, Syracuse, New York, USA
Pontifícia Universidade Católica do Rio de Janeiro (PUC-Rio), Rio de Janeiro, Brazil (associated with Universidade Federal do Rio de Janeiro (UFRJ), Rio de Janeiro, Brazil)
Institute of Particle Physics, Central China Normal University, Wuhan, Hubei, China (associated with Center for High Energy Physics, Tsinghua University, Beijing, China)
Institut für Physik, Universität Rostock, Rostock, Germany (associated with Physikalisches Institut, Ruprecht-Karls-Universität Heidelberg, Heidelberg, Germany)
National Research Centre Kurchatov Institute, Moscow, Russia (associated with Institute of Theoretical and Experimental Physics [ITEP], Moscow, Russia)
Instituto de Fisica Corpuscular (IFIC), Universitat de Valencia-CSIC, Valencia, Spain (associated with Universitat de Barcelona, Barcelona, Spain)
KVI-University of Groningen, Groningen, The Netherlands (associated with Nikhef National Institute for Subatomic Physics, Amsterdam, The Netherlands)
Celal Bayar University, Manisa, Turkey (associated with European Organization for Nuclear Research [CERN], Geneva, Switzerland)

Also at Politecnico di Milano, Milano, Italy.
Also at Università di Firenze, Firenze, Italy.
Also at Università di Ferrara, Ferrara, Italy.
Also at Università della Basilicata, Potenza, Italy.
Also at Università di Modena e Reggio Emilia, Modena, Italy.
Also at Università di Padova, Padova, Italy.
Also at Università di Milano Bicocca, Milano, Italy.
Also at LIFAELS, La Salle, Universitat Ramon Llull, Barcelona, Spain.
Also at Università di Bologna, Bologna, Italy.
Also at Università di Roma Tor Vergata, Roma, Italy.
Also at Università di Genova, Genova, Italy.
Also at Universidade Federal do Triângulo Mineiro (UFTM), Uberaba-MG, Brazil.
Also at Università di Cagliari, Cagliari, Italy.
Also at Scuola Normale Superiore, Pisa, Italy.
Also at Hanoi University of Science, Hanoi, Viet Nam.
Also at Università di Bari, Bari, Italy.
Also at Università degli Studi di Milano, Milano, Italy.
Also at Università di Pisa, Pisa, Italy.
Also at Università di Roma La Sapienza, Roma, Italy.
Also at Università di Urbino, Urbino, Italy.
Also at P.N. Lebedev Physical Institute, Russian Academy of Science (LPI RAS), Moscow, Russia.