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Transport anisotropy in Ge quantum wells in the absence of quantum oscillations

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A recent study of a high-mobility two-dimensional hole gas in a strained Ge quantum well revealed strong transport anisotropy in the quantum Hall regime when the magnetic field was tilted away from the sample normal [Q. Shi, M. A. Zudov, C. Morrison, and M. Myronov, Phys. Rev. B 91, 201301(R) (2015)]. In the present study we demonstrate that the anisotropy persists to such high temperatures and filling factors that quantum oscillations are no longer observed. This finding rules out the formation of a stripe phase as a possible origin for the observed anisotropy. However, we also show that the observed anisotropy is not consistent with other known anisotropies, such as those arising from finite-thickness effects or surface roughness.

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It is well established that transport properties of two-dimensional (2D) systems could be modified by a pure in-plane magnetic field \( B = B_1 \) for several reasons. First, \( B_1 \) can align the spin of the charge carriers, leading to an increase of the resistivity due to suppression of screening by charged impurities [1,2]. Second, due to a finite thickness of a 2D system, \( B_1 \) distorts the Fermi contour and modifies the scattering rates, also producing positive magnetoresistance [3–6]. Finally, an increase in resistivity with \( B_1 \) could also occur because of interface roughness [7–9], due to local, anisotropic perpendicular magnetic fields. Both finite-thickness and roughness mechanisms imply some anisotropy in the resistivity tensor, albeit with different orientations of the anisotropy axis with respect to \( B_1 \). The spin-polarization scenario, on the other hand, does not lead to anisotropy, unless the crystal structure is anisotropic. An addition of a weak perpendicular magnetic field (\( B_1 \ll B_2 \)) can further modify the in-plane magnetoresistance and anisotropy. However, if one disregards the appearance of quantum oscillations, the effect of \( B_1 \) is usually rather small [3,10–14].

In a purely perpendicular magnetic field, \( B = B_2 \), 2D systems reveal a much wider variety of transport phenomena. At low \( B_2 \), these phenomena include several kinds of both positive and negative [15–22] magnetoresistances, which can originate from electron-electron interactions [23–26] or quasiclassical memory effects [27–33]. At higher \( B_2 \), much more dramatic phenomena, such as integer [34] and fractional [35] quantum Hall (QH) effects, stripe and bubble phases [36–39], as well as Wigner crystals [40–44], emerge due to the interplay among Landau/Zeeman quantizations, disorder, and electron-electron interactions. Added \( B_2 \) can significantly change the transport properties owing to, e.g., spin polarization [45–47], modification of scattering rates [48–50], and finite-thickness effects [51]. Unless already anisotropic, the system remains isotropic with few exceptions, such as a \( B_2 \)-induced stripe phase in the \( N = 1 \) Landau level [52,53].

It was recently realized that when a high-mobility 2D hole gas (2DHG) in a strained Ge quantum well is subject to both in-plane (\( B_1 = B \sin \theta \)) and out-of-plane (\( B_1 = B \cos \theta \)) magnetic fields, its low temperature transport properties in the QH regime become strongly anisotropic [54]. At \( T \approx 0.3 \) K, and \( B_1 \) larger than the onset of spin splitting, the resistivity ratio at half-integer filling factors was found to increase gradually with \( \theta \), reaching \( \rho_{xx}/\rho_{yy} \approx 11.5 \) at \( \theta = 80^\circ \). At smaller \( B_2 \), the anisotropy decreased roughly linearly with \( B_2 \) for all \( \theta \), until vanishing close to the onset of Shubnikov–de Haas oscillations. Finally, switching off either \( B_1 \) or \( B_2 \) resulted in a roughly isotropic state with \( \rho_{xx}/\rho_{yy} \approx 1 \) over a wide range of \( B_2 \) or \( B_1 \) (up to 7 T).

The observed anisotropy was examined in terms of a stripe/nematic phase [36–39], known to occur in high (\( 2 < N < 6 \)) Landau levels of ultraclean GaAs systems cooled down to \( T \lesssim 0.1 \) K [37,38]. While some features were consistent with the stripe scenario, the slow decay of anisotropy with \( T \) seemed to rule against it. As the focus of Ref. [54] was on near half-integer filling factors for \( 4 < v < 40 \) in the QH regime, measurements were limited to \( T < 1.5 \) K and moderate \( B_2 \), which implied \( B_2/B_x < 6 \). It is thus important to investigate if anisotropy can survive at higher \( T \) and higher tilt angles when the quantum oscillations are absent. It is also interesting to extend the study to the lower \( N < 2 \) Landau levels, where the nematic phases in GaAs are less likely to occur.

In this Rapid Communication we report on transport measurements in a high-mobility 2DHG in a Ge quantum well in tilted magnetic fields up to 18 T, focusing on the regime of (i) much higher \( B_1/B_2 \) and \( T \) up to 8 K and (ii) the \( N = 1 \) Landau level. We find that while the anisotropy smoothly increases with \( B_1 \), the addition of a small perpendicular magnetic field \( B_2 \lesssim 0.5 \) T significantly enhances the anisotropy without bringing in quantum oscillations. At \( B_2 \gtrsim 0.5 \) T, we find that the main result of Ref. [54], namely, that \( \rho_{xx}/\rho_{yy} \) is determined by the tilt angle alone, holds all the way up to \( B_1/B_2 \gtrsim 20 \) and to much higher \( T \), even in the absence of quantum oscillations. The existence of anisotropy in the regime where no quantum oscillations are seen allows us to rule out the formation of a stripe phase as a possible origin. We further demonstrate that our findings are not compatible with other known anisotropies, such as those arising from finite-thickness effects [2] or surface roughness [7–9], pointing towards a different mechanism of anisotropic transport. We also find that at low temperatures and at fixed tilt angle, anisotropy is significantly suppressed in the \( N = 1 \) Landau level, indicating that the “scaling” of anisotropy
with a tilt angle breaks down (see the Supplemental Material [55]).

Our sample is a 5 × 5 mm square fabricated from a fully strained, 17-nm-wide Ge quantum well grown by reduced pressure chemical vapor deposition on a relaxed Si_{0.16}Ge_{0.84}/Ge/Si (001) virtual substrate [56–62]. Holes are supplied by a 12-nm-wide B-doped layer separated from the interface by a 30-nm-wide undoped Si_{0.16}Ge_{0.84} spacer. At T = 0.3 K, our 2DHG has a density ρ ≈ 2.9 × 10^{11} cm^{-2} and mobility μ ≈ 1.3 × 10^{6} cm^{2}/Vs. The resistances R_{xx} and R_{yy} were measured using corner contacts by a low-frequency (a few Hz) lock-in technique. The sample was mounted on a rotator stage and the angle between the sample normal and the magnetic field could be changed in situ without warming up the sample. Magnetotransport measurements were done by either sweeping a magnetic field at a fixed angle or rotating the sample in a fixed magnetic field.

In Fig. 1 we compare magnetoresistances R_{xx}(B) [Fig. 1(a)] and R_{yy}(B) [Fig. 1(b)] measured in a parallel field (θ = 90°, B = B_{0} = B_{∥}, dashed line) to their values in a tilted field (θ = 80°, B ≈ 1.015 B_{∥}, solid line). All four traces shown in Figs. 1(a) and 1(b) are also presented in Fig. 1(c) on a log-linear scale. At B = 0, our 2DHG exhibits modest anisotropy with R_{xx} < R_{yy}, which likely originates from anisotropic surface roughness [63]. This anisotropy virtually disappears upon application of a purely perpendicular magnetic field, B = B_{z} > 0.1 T [54]. If a purely parallel field is applied, B = B_{0} (θ = 90°), R_{xx} increases, R_{yy} decreases, and at B_{z} ≈ 6 T one finds R_{xx} ≈ R_{yy}. On the other hand, when a small perpendicular field is added (θ = 80°), both R_{xx} and R_{yy} show much bigger changes, starting from B_{z} ≈ 0.5 T and differing by three orders of magnitude at B_{z} ≈ 2.8 T. This value of B_{z} corresponds to B_{z} = 0.5 T, marked by a dotted vertical line.

Since R_{xx} and R_{yy} are measured in a square sample, the decrease of R_{yy} does not necessarily mean a decrease of resistivity ρ_{yy}. Following the results of Ref. [64], we convert R_{xx}, R_{yy} to ρ_{xx}, ρ_{yy} and present the results versus B_{z} at θ = 90° in Fig. 1(d). We find that ρ_{yy} increases slower than ρ_{xx}, and the resistivity ratio becomes ρ_{xx}/ρ_{yy} ≈ 1.6 at B = B_{z} = 10 T, as illustrated in Fig. 1(e). We thus confirm that a purely parallel magnetic field produces only a modest transport anisotropy.

To examine the anisotropy in a regime when quantum oscillations are absent, we perform the transport measurements at an elevated temperature of T = 4 K and at large tilt angles. To access the high angle limit, we apply a fixed magnetic field B along the z axis and then rotate the sample about the y axis to introduce a small perpendicular field B_{z}. In Fig. 2 we present R_{xx} [Fig. 2(a)] and R_{yy} [Fig. 2(b)], measured at T = 4 K, versus B_{z}, introduced via rotation of the sample in different B ≈ B_{∥} from 5 to 18 T, as marked. We observe that R_{xx} (R_{yy}) initially increases (decreases) with B_{z} and then shows a maximum (minimum) at all B studied.

Having determined the range of B_{z} where the anisotropy is maximized, we present in Fig. 3 a false color plot of ρ_{xx}/ρ_{yy}
The strongest anisotropy, characterized by $\rho_{xx}/\rho_{yy} > 10$, occurs at $B_x > 10$ T in a region which is domed at $B_x \approx 0.5$ T. This dome has a considerably larger gradient on the lower $B_x$ side than at the higher $B_x$ side. Furthermore, the iso-anisotropy lines on the higher $B_x$ side are well described by constant $B_x/B_z$, as illustrated by dotted lines. While this result was already obtained for half-integer filling factors in the QH regime, the observed collapse once again confirms that in this parameter range the anisotropy is determined only by the tilt angle.

To examine the temperature dependence of the anisotropy in this regime, in Fig. 5 we present $R_{xx}$ [Fig. 5(a)] and $R_{yy}$ [Fig. 5(b)] vs $B_z$ measured at $B_x \approx B = 8$ T and $T = 0.3$, 4, and 8 K. (c) $\rho_{xx}/\rho_{yy}$ vs $T$ at $\theta = 60^\circ$, $72^\circ$, $86^\circ$, and $90^\circ$, as marked. We observe that at all tilt angles (except $\theta = 90^\circ$), the anisotropy decays with increasing temperature and that the rate of this decay drops considerably with increasing tilt angle. Indeed, while at $\theta = 60^\circ$, the anisotropy disappears at $T \approx 2$ K, the resistivity ratio measured at $\theta = 86^\circ$ remains significant, and $\rho_{xx}/\rho_{yy} > 4$, even at $T = 8$ K. At $\theta = 90^\circ$, on the other hand, we observe virtually no temperature dependence of the anisotropy. This finding suggests that the mechanism responsible for the temperature dependence in tilted fields is completely absent in pure $B_\|$.

The observation of strong anisotropy in small $B_z$ and at high temperatures unambiguously rules out QH stripes as a possible origin. First, the robustness against temperature suggests a much larger energy scale than expected of the charge density wave. In the Hartree-Fock approach, the latter scales with the exchange energy $[36,65]$, and is $\sim 1$ K at $B_x = 0.5$ T. Indeed, in clean GaAs systems, stripes manifest only at much lower $T$, even in tilted magnetic fields. Second, QH stripes are expected completely absent in pure $B_\|$. The observation of strong anisotropy in small $B_z$ and at high temperatures unambiguously rules out QH stripes as a possible origin.
The perpendicular magnetic field certainly plays a crucial role in the underlying mechanism of the anisotropy. Our Ge quantum wells exhibit a modest transport anisotropy both at $B = 0$ and in a purely in-plane magnetic field [see Fig. 1(e) and Ref. [54]]. It is known that an in-plane field could induce anisotropy due to the distortion of the Fermi contour [3,4] and surface roughness, via anisotropic, random perpendicular magnetic fields [7–9]. While the former can be ruled out because it leads to $\rho_{xx} < \rho_{yy}$ (when $B_1 = B_2$), the latter is consistent with our observations. We thus conclude that these modest anisotropies likely originate from the surface roughness [63].

One important question is whether the surface roughness can also result in huge anisotropy in our Ge quantum wells in tilted $B$. First, $B_1$-induced anisotropy is known to be temperature independent [7,9], whereas the anisotropy in tilted fields has a significant temperature dependence (see Fig. 5 and Ref. [54]). Second, because of the anisotropy at $B = 0$, the magnitude of $B_1$-induced anisotropy must depend on the orientation of $B_1$ [9], whereas the observed anisotropy in tilted magnetic fields was found to be insensitive to the orientation of $B_1$ [54]. Finally, no strong enhancement of anisotropy due to additional $B$, has been reported in experiments using GaAs samples with a much larger surface roughness [7] or predicted theoretically [66–68]. In fact, Ref. [7] reported a reduction of the anisotropy upon introduction of $B_z$. We therefore conclude that the anisotropy in a purely parallel magnetic field is unlikely to be related to the strong anisotropy in tilted magnetic fields.

In summary, we have investigated anisotropic transport in a high-mobility 2D hole gas in a strained Ge quantum well in tilted magnetic fields up to 18 T and at temperatures up to 8 K. We have found that the maximum of $\rho_{xx}/\rho_{yy}$ occurs at the highest available $B_z$, and at $B_1 \approx 0.5$ T, where it remains significant even at the highest temperature studied. The existence of anisotropy in a regime where no quantum oscillations are seen rules out the formation of stripes as a possible origin. Even though quantum oscillations are not required, the perpendicular magnetic field plays a crucial role both in the magnitude of the anisotropy and its temperature dependence. We have also shown that our findings are not compatible with other known anisotropies, such as those arising from finite-thickness effects or surface roughness, suggesting a different mechanism of anisotropic transport.

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TRANSPORT ANISOTROPY IN Ge QUANTUM WELLS IN . . .

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