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Modeling Pile Setup in Natural Clay Deposit Considering Soil Anisotropy, Structure and Creep Effects: Case Study

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Abstract: In this paper the behavior of a natural soft clay deposit under the installation of a case study pile is numerically investigated. The case study problem includes installation of an instrumented close-ended displacement pile in a soft marine clay deposit in Scotland, known as Bothkennar clay. The site has been used for a number of years as a geotechnical test bed site and the clay has been comprehensively characterized with both in-situ tests and laboratory experiments. The soft soil behavior, both after pile installation and subsequent consolidation, is reproduced by using an advanced critical state-based constitutive model, namely S-CLAY1S, that accounts for the anisotropy of soil fabric and destructuration effects during plastic straining. Furthermore, a time-dependent extension of S-CLAY1S model, namely Creep-SCLAY1S is used to study soil creep and the significance of its consideration on examining the overall pile installation effects. The simulation results are compared against field measurements; furthermore, for comparison the pile installation is also analyzed using the well-known isotropic modified...
Cam-clay model to highlight the importance of considering inherent features of natural soil such as anisotropy and structure in the simulations. A series of sensitivity analysis is also performed to evaluate the influence of initial anisotropy and bonding values on simulation results and to check the reliability of the numerical analyses.

**Introduction**

Since piles have to carry design loads for long periods of time, the consequences of soil modification around the pile, caused by its installation, are of great importance to variations of pile capacity. This is of more concern for piles in clays as for them the end bearing usually contributes a little to the overall pile capacity; while skin friction along the shaft constitutes the major portion of the pile function especially when there is no reliable soil layer at the end point of the pile. Therefore, field and laboratory investigations of the effects of pile installation on the properties of natural clays have been the subject of a large number of research studies over the past few decades (e.g., Holtz and Lowitz 1965; Roy et al. 1981; O’Neill et al. 1982; Heydinger and O’Neill 1986; Azzouz and Morrison 1988; Bond and Jardine 1991; Collins and Stimpson 1994; Burns and Mayne 1999; Pestana et al. 2002; Gallagher et al. 2005). However, there are still considerable uncertainties involved in the prediction of the capacity and performance of frictional driven piles in clays (Niarchos 2012). Particularly the increase in the capacity of displacement piles with time in clayey deposits, that are subject to significant increase in pore pressure during pile setup, has been widely debated (e.g., Randolph et al. 1979; Kavvas 1982; Konrad and Roy 1987; Fellenius et al. 1989; Svinkin et al. 1994; Clausen and Aas 2000; Augustesen et al. 2006; Liyanapathirana 2008; Gwizdała and Więcławski 2013). Reliable prediction of the installation effects of piles on the inherent properties of natural deposits in which they are installed is essential for accurate and efficient design of these CO2 heavy and relatively expensive geo-
structures. However, in spite of a few recent efforts (e.g., Sheil et al. 2015), in most of the studies so far primarily simple analytical methods have been developed or employed to simulate changes of soil properties around the pile shaft during and after installation. This is in large part due to the lack of numerical models capable of simulating the influential features of natural soil behavior, such as anisotropy, inter-particle bonding (structure), degradation of bonds (destructuration), rate dependency and etc., at a practical scale.

The main objective of this study is to numerically analyze the effects of a single pile setup in a cohesive soil layer, by primarily evaluating the effective stress variations and pore pressure dissipations around the pile after installation and during subsequent equalization (i.e., dissipation of excess pore pressures). It is also aimed to illustrate the practical capabilities of advanced soil models for evaluating soil alteration due to pile driving and prediction of pile capacity with time from a numerical standpoint. Pile installation has been modeled as an undrained expansion of a cylindrical cavity in the soil medium, commonly known as cavity expansion method (CEM) (Soderberg 1962; Carter et al. 1979; Randolph et al. 1979; Yu 1990; Yu 2000). Although, CEM does not model the full pile jacking procedure, it has proven to be practically a more versatile approach for conducting parametric studies of both short-term and long-term pile installation effects (Castro et al. 2013; Sheil et al. 2015). The numerical analyses are conducted using an anisotropic critical state-based effective stress soil model and a new time-dependent creep constitutive model. The analysis of the soil-pile load transfer mechanism and the mechanical response in the pile structure are beyond the scope of this paper and hence are not addressed here.

**Constitutive Models**

It is a well-established fact that the yield curves obtained from experimental tests (with triaxial or hollow cylinder apparatuses) on undisturbed samples of natural clays are inclined due
to the inherent fabric anisotropy in the clay structure (Graham et al. 1983; Dafalias 1987; Wheeler et al. 1999; Nishimura et al. 2007). Since consideration of full anisotropy in modeling soil behavior is not practical, due to the number of parameters involved, efforts have been mainly focused on the development of models with reduced number of parameters while maintaining the capacity of the model (Kim 2004). In order to capture the effects of anisotropy on soil behavior, a number of researchers have proposed anisotropic elasto-plastic constitutive models involving an inclined yield curve that is either fixed (Sekiguchi and Ohta 1977; Zhou et al. 2005) or is able to rotate in order to simulate the development or erasure of anisotropy during plastic straining (Davies and Newson 1993; Whittle and Kavvadas 1994; Wheeler et al. 2003; Dafalias et al. 2006). Among the developed anisotropic models, S-CLAY1 model (Wheeler et al. 2003) has been successfully used on different applications and accepted as a pragmatic anisotropic model for soft natural clays (Karstunen et al. 2006, Yildiz 2009, Zwanenburg 2013). In this model the initial plastic anisotropy is considered to be cross-anisotropic, which is a realistic assumption for normally consolidated clays deposited along the direction of consolidation. The model accounts for the development or erasure of anisotropy if the subsequent loading produces irrecoverable strains, resulting in a generalized plastic anisotropy. For simplicity, in this model the elastic behavior is assumed to be isotropic, which is a realistic assumption given the developed model is intended for applications with normally consolidated or lightly overconsolidated soft clays where even a small amount of stress increment is likely to cause yielding (Wheeler et al. 2003). The main advantages of the S-CLAY1 model over other proposed models are i) relatively simple model formulation, ii) realistic $K_o$ prediction, and most importantly iii) model parameters can be determined from standard laboratory tests using well-defined methodologies (Karstunen et al. 2005). The model has been further developed to also take account of bonding and destructuration effects (Karstunen et al. 2005), and very recently, time effects (Sivasithamparam et al. 2015) as
additional important features of natural soils’ behavior. In the following the basics of these two advanced extensions of S-CLAY1 model, employed in this study, are explained in further detail.

**S-CLAY1S Model**

S-CLAY1S (Karstunen et al. 2005) is an extension of S-CLAY1 model that, in addition to plastic anisotropy, accounts for inter-particle bonding and destructuration of bonds during plastic straining. In three-dimensional stress space the yield surface of the S-CLAY1S model forms a sheared ellipsoid (similar to S-CLAY1) that is defined as

\[
f_{\mathbf{y}} = \frac{3}{2} \left[ (\mathbf{d} - p' \mathbf{a}_d)^T (\mathbf{d} - p' \mathbf{a}_d) \right] - \left[ M^2 - \frac{3}{2} (\mathbf{a}_d)^T (\mathbf{a}_d) \right] (p'_m - p')p' = 0
\]

In the above equation \( \mathbf{d} \) and \( \mathbf{a}_d \) are the deviatoric stress and the deviatoric fabric tensors respectively, \( M \) is the critical state value, \( p' \) is the mean effective stress, and \( p'_m \) is the size of the yield surface related to the soil’s preconsolidation pressure (see Fig. 1). The effect of bonding in the S-CLAY1S model is described by an intrinsic yield surface (Gens and Nova 1993) that has the same shape and inclination of the natural yield surface but with a smaller size. The size of the intrinsic yield surface is specified by parameter \( p'_{mi} \) which is related to the size \( p'_m \) of the natural yield surface by parameter \( \chi \), the current amount of bonding

\[
p'_m = (1 + \chi)p'_{mi}
\]

S-CLAY1S model incorporates three hardening laws. The first of these is the isotropic hardening law similar to that of modified Cam-clay (MCC) model (Roscoe and Burland 1968) that controls the expansion or contraction of the intrinsic yield surface as a function of plastic volumetric strain increments \( (d e_p^p) \)

\[
dp'_m = \frac{v p'_{mi}}{\lambda_i - \kappa} d e_p^p
\]
where $\nu$ is the specific volume, $\lambda$ is the gradient of the intrinsic normal compression line in the compression plane ($\ln p' - \nu$ space), and $\kappa$ is the slope of the swelling line in the compression plane. The second hardening law is the rotational hardening law, which describes the rotation of the yield surface with plastic straining (Wheeler et al. 2003)

$$d\alpha_d = \omega \left[ \left( \frac{\eta}{4} - \alpha_d \right) \langle d\varepsilon^p \rangle + \omega_d \left( \frac{\eta}{3} - \alpha_d \right) |d\varepsilon^p_d| \right]$$

(4)

where $\eta$ is the tensorial equivalent of the stress ratio defined as $\eta = \sigma_d / p'$, $d\varepsilon^p$ is the increment of plastic deviatoric strain, and $\omega$ and $\omega_d$ are additional soil constants that control the absolute rate of the rotation of the yield surface toward its current target value, and the relative effectiveness of plastic deviatoric strains and plastic volumetric strains in rotating the yield surface, respectively. The third hardening law in S-CLAY1S model is destructuration, which describes the degradation of bonding with plastic straining. The destructuration law (Karstunen et al. 2005) is formulated in such a way that both plastic volumetric strains and plastic shear strains tend to decrease the value of the bonding parameter $\chi$ towards a target value of zero which reads

$$d\chi = -\xi \left( \langle d\varepsilon^p \rangle + \xi_d |d\varepsilon^p_d| \right)$$

(5)

where $\xi$ and $\xi_d$ are additional soil constants. Parameter $\xi$ controls the absolute rate of destructuration, and parameter $\xi_d$ controls the relative effectiveness of plastic deviatoric strains and plastic volumetric strains in destroying the inter-particle bonding. The elastic behavior in the model is formulated with the same isotropic relationship as in the MCC model requiring the values of two parameters, $\kappa$ and the Poisson's ratio, $\nu'$ (to evaluate the value of elastic shear modulus, $G'$).
Creep-SCLAY1S Model

The Creep-SCLAY1 model (Sivasithamparam et al. 2015) is an extension of S-CLAY1 to account for time-dependent response of clays. In this model the elliptical surface of the S-CLAY1 model is adopted as the normal consolidation surface (NCS) that is the boundary between small and large irreversible (creep) strains. Furthermore, in this model creep is formulated using the concept of a constant rate of visco-plastic multiplier (Grimstad et al. 2010) as

\[ \dot{\lambda} = \frac{\mu^*}{\tau} \left( \frac{p'_{eq}}{p'_{p}} \right)^\beta \left( \frac{M^2 - \alpha K_0^{nc}}{M^2 - \eta K_0^{nc}} \right) \]  

(6)

where \( p'_p \) is the size of the outer rotated ellipse (see Fig. 2) which defines the NCS, \( p'_{eq} \) is the size of the current stress surface (CSS) that is the inner ellipse passing through the current state of effective stress, \( \mu^* \) is the modified creep index, \( \tau \) is a reference time that is set to 1 day if the NCS is derived from a standard oedometer test (see Leoni et al. 2008 for details), \( \alpha K_0^{nc} \) defines the inclinations of the ellipses in normally consolidated state (assuming \( K_0 \) consolidation history), \( \eta K_0^{nc} = 3(1 - K_0^{nc})/(1 + 2 K_0^{nc}) \), and the additional term \((M^2 - \alpha K_0^{nc})/(M^2 - \eta K_0^{nc})\) is added to ensure that under oedometeric conditions the resulting creep strain corresponds to the measured volumetric creep strain rate (Sivasithamparam et al. 2015). Moreover, \( \beta \) is defined as \( \beta = (\lambda^* - \kappa^*)/\mu^* \) where \( \lambda^* \) and \( \kappa^* \) are the modified compression and swelling indices, respectively, and \( \mu^* \) is related to the one-dimensional secondary compression index \( C_a \) and the initial void ratio \( e_0 \) as

\[ \mu^* = C_a/[\ln 10 (1 + e_0)] \].

The size of NCS evolves with volumetric creep strains \( \varepsilon_v^c \) according to the following isotropic hardening law

\[ p'_p = p'_{po} \exp \left( \frac{\varepsilon_v^c}{\lambda^* - \kappa^*} \right) \]  

(7)
where $p'_{po}$ is the initial effective preconsolidation pressure. Adopting the same function as that of the NCS, the size of the CSS is obtained from the current stress state ($p'$ and $q$) using the intersection of the vertical tangent to the ellipse with the $p'$ axis as

$$p'_{eq} = p' + \frac{3}{2} \frac{[\sigma_d - p' \alpha_d^T (\sigma_d - p' \alpha_d)]}{M^2 - \frac{3}{2} \alpha_d^T \alpha_d} p'$$  (8)

where $p'_{eq}$ is also known as the equivalent mean effective stress. The Creep-SCLAY1 model incorporates the same rotational hardening law as S-CLAY1 and S-CLAY1S models. Recently, the Creep-SCLAY1 model has been further extended to take into account the soil structure by adopting the destructuration hardening law of the S-CLAY1S model, as described in the previous section. The new extended model is called Creep-SCLAY1S.

**Case Study**

Bothkennar clay is a normally consolidated to slightly overconsolidated marine clay deposited on the southern bank of the Forth River Estuary near Stirling, located approximately midway between Glasgow and Edinburgh in Scotland. Bothkennar was an Engineering and Physical Science Research Council’s geotechnical test site for which a comprehensive series of tests was performed in the early 90s to evaluate the properties of the high plasticity silty clay at the site. The resulting test data were reported and are available in the collection of papers in Géotechnique Symposium-in-Print (Vol. 42, No. 2, 1992). Since then it has also been the subject of a number of more advanced experimental investigations (e.g., Albert et al. 2003, Houlsby et al. 2005, McGinty 2006). Lehane and Jardine (1994) conducted a series of field experiments using high quality instrumented piles developed at Imperial College. The displacement piles employed in the investigation were equipped to measure pore pressures and effective stresses acting on the
soil-pile interface during pile installation and following consolidation. Two different pile lengths of 3.2m and 6m were studied, and the diameter of the case study piles was uniformly 102mm. From the base of a 1.2m deep cased hole, the cone-ended steel tubular piles were jacked into the ground at a rate of 500mm per minute in a series of 200mm pushes that were separated by pause periods of about 3 minutes. The general configuration of the 6m long model pile that has been selected for this study is shown in Fig. 3.

As shown in the figure different sensors to measure axial load, radial stress, shear stress and pore pressure were used at three clusters located along the lower 3m section of the pile, further details with regards to the instrumentation of the test piles can be found in Bond et al. (1991). Note that in the following the instruments are referred to by their distances from the pile tip (h) normalized by the pile radius (R) (see Fig. 3). The profile of the natural deposit penetrated by the instrumented piles can also be seen in Fig. 4, it includes a 1m deep overconsolidated dry crust followed by 5m deep layer of lightly overconsolidated Bothkennar clay with overconsolidation ratio (OCR) value of around 1.5.

**Numerical Model and Simulations**

The two advanced constitutive models described earlier in the paper have been implemented as user defined models in PLAXIS 2D AE version (Brinkgreve et al. 2013) using the fully implicit numerical solution proposed by Sivasithamparam (2012). Using each of the implemented models for the deformation calculations, PLAXIS carries out the coupled flow-deformation consolidation analysis based on Biot’s theory.

The geometry of the numerical model for pile installation and the schematic sketch of different soil layers are shown in Fig. 5. As it is shown in the figure the groundwater table is located 1m below the ground surface. Taking advantage of the symmetry of the problem,
axisymmetry condition is assumed in the finite element analysis. Parametric studies have been carried out to find out how wide the model should be to have a negligible influence of the outer boundary on the results. An extent of 3m from the symmetry axis in the horizontal direction was found to be sufficient. The depth of the model is selected to be the same as the length of the pile (i.e., 6m) in order to avoid modeling the pile tip, which can cause numerical instabilities. Roller boundaries are applied to all sides in order to enable the soil moving freely due to cavity expansion. Drained conditions and zero initial pore pressures are assumed above the water table. Also a drainage boundary is considered at the ground level and dynamic effects are ignored in the numerical model. A finite element mesh with 4048 15-noded triangular elements, resulting in 33021 nodes, is used in the analyses. Each element has pore water pressure degrees of freedom at corner nodes. Mesh sensitivity studies have been carried out to ensure that the mesh is dense enough to produce accurate results for both constitutive models. Towards the cavity wall much finer elements are used in order to provide better resolution in this zone with expected high strain gradients. The problem is modeled using large strain analyses with updated pore pressures, taking advantage of the updated Lagrangian formulation in PLAXIS.

Undrained pile installation is modeled as the expansion of a cylindrical cavity through development of a prescribed displacement from a small initial radius to a final, larger, radius (see Fig. 5). Similar to the pile, a cavity radius $r_c$ of 0.05m has been selected, and a time interval of 0.1 day has been specified for the application of the prescribed displacement. There are other techniques for modeling the expansion of the cavity, e.g., applying an internal volumetric strain, however a prescribed displacement has been proven to be more practical particularly in terms of numerical stability (Kirsch 2006). As stated above, there is extensive laboratory data available for Bothkennar clay which makes it possible to derive a consistent set of material parameters for the advanced constitutive models used in this study. The initial values of state variables, as well as the values of conventional soil constants and additional model parameters are summarized in...
Table 1. The initial state variables include the initial void ratio \(e_0\), OCR, the initial degree of anisotropy \(\alpha_0\), and the initial amount of structure \(\chi_0\) (see Table 1). The conventional soil constants include unit weight \(\gamma\), elastic constants (slope of the swelling line \(\kappa\) and Poisson’s ratio \(\nu'\)), and plastic constants (slopes of the normal compression line \(\lambda\) and the critical state line \(M\)). Based on the values of \(\lambda\), \(\kappa\) and \(e_0\), it is easy to calculate the corresponding values for the Creep-SCLAY1S model (\(\lambda' = 0.10\) and \(\kappa' = 0.0067\)). In Table 1, the additional soil constants related to the evolution of anisotropy (\(\omega\) and \(\omega_d\)) and destructuration (\(\xi\) and \(\xi_d\)), are also listed together with the intrinsic compressibility \(\lambda_i\). The latter needs to be used as the model parameter instead of \(\lambda\) for a natural soil, when the destructuration hardening law is used. The methodology for deriving these soil constants has been discussed by Leoni et al. (2008) and Sivasithamparam et al. (2015) and is not repeated here.

Table 2 lists the values for the viscosity parameters which are similar to the soft soil creep model (Vermeer et al. 1998), and the anisotropic creep model (Leoni et al. 2008). During the coupled consolidation analysis, the value of permeability coefficient \(k\) is assumed to be constant. The values for soil permeability (summarized in Table 3) are taken from literature (Géotechnique Symposium-in-Print 1992). In Table 3, \(k_v\) denotes vertical permeability obtained from tests on vertical soil samples and \(k_h\) denotes horizontal permeability obtained from tests on horizontal soil samples.

The behavior of the overconsolidated dry crust layer is modeled with a simple linear elastic-perfectly plastic Mohr-Coulomb model using the following relevant parameter values for the Bothkennar clay: \(E = 3\) MPa, \(\nu' = 0.2\), \(\varphi' = 30^\circ\), \(\psi' = 0^\circ\), \(c' = 6\) kPa, and \(\gamma = 19\) kN/m\(^3\). It should also be added that the initial state of stress is generated by adopting \(K_0\)-procedure (Brinkgreve et al. 2013). In addition to the two advanced models, S-CLAY1S and Creep-SCLAY1S, the boundary value problem is also modeled with the commonly used MCC.
model in order to better highlight the advantages of considering natural features of soil behavior such as anisotropy, structure and time effects on reliability of the simulation results. The simulation results presented in the following sections are all based on model predictions at a point on the surface of the cavity and at the depth of $h/R = 28$ (the same depth as the depth of the middle cluster sensors on the pile surface).

**Numerical Simulation Results**

*Total stress, pore pressure and effective stress variations*

Fig. 6 shows the experimental measurements and numerical predictions of radial total stresses $\sigma_{ri}$ during pile installation, at the pile surface. The field measurements in the figure were recorded by instruments at eight radii from the pile tip (i.e., at $h/R = 8$) and when the pile tip penetrated farther by instruments at $h/R = 28$. The figure illustrates that similar to the experimental results, the S-CLAY1S and Creep-SCLAY1S models predict the radial stresses, developed during pile jacking, to lie between the initial undisturbed horizontal stress $\sigma_{ho}$ and the limit pressure. The limit pressure was measured through self-boring pressuremeter tests (Lehane and Jardine 1994). The figure also shows that the MCC model overestimates the radial total stresses and predicts them to exceed the pressuremeter limit pressure at depths beyond 3.5m.

The numerical predictions of Fig. 6, which are qualitatively consistent with the experimental results, indicate that the radial total stresses in Bothkennar clay increase with the increase of penetration depth. Such trend has also been observed in similar studies on other types of clay (Doherty and Gavin 2011; Randolph 2003) which suggests that the increase of total radial stresses with depth intensifies with the preconsolidation pressure of clay layers. Moreover, a comparison between Figs. 4(b) and 6 shows that the variations of radial total stresses resemble
the end resistance changes with depth which implies that $\sigma_{rel}$ values are controlled by the soil state (Doherty and Gavin 2011), contrary to sandy soils in which variations of $\sigma_{rel}$ are independent of the soil state (Chow and Jardine 1996).

For a proper understanding of pile behavior and to draw a clearer picture of effective stress conditions, pore pressure values should be provided in addition to radial total stresses. Fig. 7 shows the experimentally measured installation pore pressures and their corresponding numerical predictions obtained through MCC, S-CLAY1 and Creep-SCLAY1S models. Note that in terms of field data the figure only shows the stationary values of pore pressure $u_z$ measured during the installation pause periods (Lehane and Jardine 1994). The figure illustrates that the numerical results fit well with the experimental measurements and predict similar trends. The predictions made by MCC and S-CLAY1S models are approximately equal while the Creep-SCLAY1S model predicts slightly higher pore pressure values. Nevertheless, all three models predict a linear increase in pore pressure as depth increases. Such overall trend can also be seen in the experimental data, except that in the field measurement data, depending on penetration depth, two different patterns of pore pressure increase can be observed. As it is indicated by Doherty and Gavin (2011), for penetration depths less than 2.5m, pore pressure increases rapidly and after this depth its rate reduces. Similar trend is also observed in Fig. 6 for the variations of radial total stress. This similarity could be attributed to friction fatigue (Xu et al. 2006) and as it can be seen in Figs. 6 and 7 SCLAY1S and Creep-SCLAY1S models can capture this effect well, and predict similar trends for the values of radial total stress and pore pressure.

Measurements of pore pressure variations and relaxation of radial total stresses, during equalization and after pile jacking, were two of the main features of the Imperial College pile tests (Doherty and Gavin 2011). These features are expressed through normalized quantities of pore pressure dissipation factor $U_d$, and relaxation ratio $H/H_i$, defined as
where \( u \) is the pore pressure after installation and subsequent consolidation, \( u_0 \) is the hydrostatic pore water pressure, \( u_{\text{max}} \) is the maximum pore pressure reached during pile installation, and \( \sigma_r \) is the radial total stress during consolidation. The variations of these two factors, based on field measurements, are shown in Figs. 8(a) and (b), and are compared with their numerical counterparts predicted by MCC, S-CLAY1S and Creep-SCLAY1S models. As field measurement data shows, \( H/H_i \) remained constant for the first few minutes and then reduced steadily, reaching an ultimate value of about 0.5 after seven days (Lehane and Jardin 1994). Such reduction would not occur if the soil next to the pile was elastic and isotropic (Sills 1975). This kind of behavior indicates that there is an interaction of a yield zone, developed next to the pile, with the surrounding soil that has not yielded. As Fig. 8(b) shows, in general all three elasto-plastic models are able to capture the reducing trend of \( H/H_i \); however, the MCC model can only provide reasonable prediction of the variations of relaxation ratio for the early stages of pile consolidation, and it overestimates the field data after half a day of consolidation (i.e., after 700 minutes). The S-CLAY1S and Creep-SCLAY1S models, that consider soil anisotropy, provide predictions that are noticeably closer to the field measurement data. Field dissipation curves shown in Fig. 8(a) are based on measurements taken at different soil depths. As this figure shows, the variations of pore pressure dissipation factor generally mirrors \( H/H_i \) changes. Based on field data, the typical times for 50% and 85% excess pore pressure dissipation were about 12 hours and 4 days, respectively. It can be seen in the figure that the MCC and Creep-SCLAY1S models provide comparably similar estimations of pore pressure equalization factors which are smaller than S-CLAY1S predictions. During consolidation as pore pressure dissipates, radial effective
stress $\sigma'_r$ increases towards a final equilibrium value $\sigma'_{rc}$. Fig 8(c) shows the comparison between experimental and numerical variations of normalized radial effective stress $\sigma'_r/\sigma'_{rc}$ during equalization. Based on field measurements, after about 2 minutes $\sigma'_r$ values increased rapidly with time, reaching 85% of $\sigma'_{rc}$ after about 1000 minutes and near equilibrium after about 4 days. The rate of $\sigma'_r$ equalization exceeded that for pore pressure dissipation, reportedly because the variations of pore pressures and radial stresses were equal during the later stages of equalization (Lehane and Jardine 1994). As it is shown in Fig. 8(c), all three models can capture the increasing trend of $\sigma'_r/\sigma'_{rc}$, and their quantitative consistency with field measurements reduces from S-CLAY1S to Creep-SCLAY1S and MCC models. Numerical predictions of the variations of equalized radial effective stresses with depth are shown in Fig. 9 and are compared with field data. This figure illustrates that all models predict $\sigma'_r$ to increase with depth, which is in agreement with field measurements; however, the most quantitatively comparable results to field data are provided by Creep-SCLAY1S model. As it was indicated by Randolph (2003), the reliability of existing predictive models for accurate evaluation of effective stresses is one of the main concerns regarding application of these models. The comparisons carried out in this section show that Creep-SCLAY1S model provides more accurate and reliable results compared to the other two time-independent models.

**Variations of Undrained shear Strength**

As the result of pile jacking into the ground, the undrained shear strength $c_u$ of the soil surrounding the pile deviates from its initial value corresponding to the undisturbed soil, $c_{u0}$. For the soil surrounding the pile, Figs. 10(a) and (b) show the variations of normalized undrained shear strength $c_u/c_{u0}$ predicted by MCC, S-CLAY1S and Creep-SCLAY1S models, both after pile installation and consolidation. Experimental studies show that, right after pile jacking, the installation of displacement piles in soft soil results in the reduction of undrained shear strength.
of the soil close to the pile (Serridge and Sarsby 2008). Fig. 10(a) illustrates that while S-CLAY1S and Creep-SCLAY1S predict this reduction, MCC model fails to capture such reduction and instead it predicts that shortly after installation the soil surrounding the pile gains an increased shear strength. The results shown in Fig. 10(a) also suggest that based on anisotropic models predictions the shear strength reductions are more significant for the soil that is within about three radii from the pile surface, and beyond that the decrease in soil’s undrained shear strength is more moderate, up to a distance of about 15 radii from the pile surface where shear strength changes are insignificant. As it was discussed by Castro and Karstunen (2010), the large reductions of undrained shear strength close to the pile can be attributed to the loss of soil structure, and the small reductions at further distances are owing to the reduction of effective mean pressure.

After consolidation, the undrained shear strength increases (see Fig. 10(b)). This increase in close vicinity of the pile surface is more noticeable, and further away from the pile surface in areas which are less affected by the pile, this increase is minimal. However, the three constitutive models provide different estimations of this shear strength increase. For instance, close to the cavity wall, MCC model provides predictions which can be up to 90% different from S-CLAY1S and Creep-SCLAY1S models, while beyond fifteen pile radii all three models are quantitatively similar. Fig. 11 shows the variations of undrained shear strength near the cavity wall and during the equalization period. As it can be seen in this figure, S-CLAY1S and Creep-SCLAY1S models predict that the undrained shear strength, right after pile installation, are 50% and 30% less than \( c_{u0} \), while MCC predicts it to be 40% more than \( c_{u0} \). As time elapses and excess pore pressure dissipates, all three models show increasing undrained shear strength due to excess pore pressure dissipation and increase in mean effective stresses. The Creep-SCLAY1S model, in the early stages of consolidation predicts higher undrained shear strength compared to the S-CLAY1S
model; however, its equalized undrained shear strength is smaller because creep causes additional relaxation of radial stresses.

**Sensitivity Analysis**

Penetration of a pile in a natural soft clay deposit results in destructuration, i.e., degradation of the soil internal structure, which consequently influences the yielding of the soil. In this section the sensitivity of numerical predictions of soil behavior during equalization is investigated against variations of initial anisotropy and bonding (represented by parameters $\alpha_0$ and $\chi_0$, respectively) which indicate the state of the yield surface inclination and structure of the soil at the onset of the consolidation stage. Fig. 12 shows the S-CLAY1S and Creep-SCLAY1S predictions of radial effective stresses for $\alpha_0$ values changing ±20% around its representative value. This figure illustrates that the higher the initial anisotropy parameter is, the lower the predicted radial effective stress would be. However, comparing these results with corresponding results in Fig. 9 shows that using $\alpha_0$ with ±20% different values does not have a significant qualitative and quantitative effect on numerical results. Similar trends can be distinguished in Fig. 13 which depicts the effect of $\chi_0$ variations on numerical predictions of radial effective stresses.

The sensitivity of numerical results, in time domain, to the alteration of initial bonding and anisotropy parameters is shown in Figs. 14 and 15, respectively. As these two figures show, ±20% variation of these parameters does not have considerable effect on numerical predictions. Overall, the sensitivity analyses performed in this section confirms that initial values of anisotropy and bonding parameters have negligible effects on numerical predictions of S-CLAY1S and Creep-SCLAY1S models, and therefore for a reasonably accurate evaluation of the initial values of anisotropy and bonding, these models’ performances are reliable.
Installation effect on soil structure

The effect of pile setup on surrounding soil structure can be investigated through the variations of bonding parameter $\chi$ which represents the sensitivity of the soil. Fig. 16 shows the S-CLAY1S and Creep-SCLAY1S predictions of normalized bonding parameter, in different distances from pile surface, after installation and soil consolidation phases. The results illustrated in this figure are obtained for different initial bonding parameter values to confirm that $\chi_0$ has no major effect on numerical simulations and hence can be reasonably utilized for normalization of $\chi$. Fig. 16 shows that installation of pile results in the reduction of bonding parameter. This reduction is understandably more intense close to the pile surface. Moreover, the figure also shows that the predictions of both S-CLAY1S and Creep-SCLAY1S models are comparably similar after installation. However, as time passes and the soil consolidates, the results of rate-dependent model deviates from the rate-independent S-CLAY1S model. The comparison between $\chi/\chi_0$ after installation and consolidation reveals that there is further reduction of bonding parameter after consolidation. This extra reduction predicted by S-CLAY1S model is smaller than that of Creep-SCLAY1S. Therefore, the Creep-SCLAY1S model predicts the contribution of consolidation process in reduction of $\chi$ to be bigger than what it was thought before (discussed in Castro and Karstunen 2010); however, it can still be concluded that the reduction of $\chi$ is mainly caused by the undrained cavity expansion.

Installation effect on soil anisotropy

Similar to $\chi$, installation of a pile affects the soil fabric orientation and consequently the inclination of the representative yield surface. Fig. 17 shows the variation of $\alpha$ for different $\alpha_0$ values after installation of the pile and consolidation of the soil predicted by the advanced anisotropic models. As it can be seen in this figure, after installation and consolidation, the value
of anisotropy parameter in close vicinity of the pile (distances up to 2 pile radii from the surface) is independent of $\alpha_0$ and both models provide similar predictions of $\alpha$. In further distances, up to 4 pile radii, while both models provide similar evaluation of $\alpha$ after installation, the Creep-SCLAY1S model predicts lower anisotropy parameter after consolidation. In distances beyond 4 pile radii, the value of $\alpha$ depends on $\alpha_0$, however the patterns of numerical predictions follow the aforementioned trends. In other words, in this radial distances from the pile both models have comparably similar evaluations of $\alpha$ after installation while S-CLAY1S model predicts higher $\alpha$ values after consolidation. Fig. 17 illustrates that, after installation, the value of $\alpha$ on the pile surface increases when $\alpha_0=0.47$ and decreases when $\alpha_0=0.59$ and 0.71. After consolidation, for $\alpha_0=0.47$ and 0.59, the anisotropy parameter on the pile surface exceeds $\alpha_0$ while remains smaller than $\alpha_0$ when $\alpha_0=0.71$. These trends are sustained in distances less than $1.5r_c$, and beyond that $\alpha$ is less than $\alpha_0$ and tends toward $\alpha_0$ at further distances from the pile.

To clarify the trends observed in Fig. 17, variations of radial $\alpha_r$ and axial $\alpha_y$ components of anisotropy tensor are shown in Figs. 18–21. Also to check the sensitivity of these components to the value of initial anisotropy parameter, the variations of $\alpha_r$ and $\alpha_y$ are evaluated for ±20% alteration of $\alpha_0$ around its representative value and the results are depicted in Figs. 18 and 19. Similar sensitivity analysis is also carried out for the effects of alteration of $\chi_0$ on the variations of $\alpha_r$ and $\alpha_y$ (Figs. 20 and 21). Figs. 18 and 20 suggest that $\alpha_r$ after installation and consolidation reduces as the distance from the surface of the pile increases; and, on the pile surface, $\alpha_r$ after consolidation is higher than that caused by undrained expansion of cavity. In contrary to this trend, Figs. 19 and 21 show that $\alpha_y$ increases as the distance from the pile surface increases. These figures also illustrate that both numerical models provide reasonably comparable results and these results are not sensitive to $\alpha_0$ and $\chi_0$ values.
Discussion

The comparison of the numerical results in two stages of pile setup history, installation and equalization, reveals that the models which take into account the natural features of the soil behavior, namely anisotropy, destructuration and time effects, provide comparable results during installation period (Figs. 6 and 7). The predictions of SCLAY1S and Creep-SCLAY1S models after installation are in good agreement with the experimental measurements while the MCC model provides less comparable results. In other words, after installation, both SCLAY1S and Creep-SCLAY1S models provide representative and approximately similar predictions of radial effective stresses, pore pressures, and undrained shear strengths (Figs. 6, 7 and 10, respectively). While MCC predictions in some cases (e.g., pore water pressure) are consistent with the two other models, in other cases its simulation results deviate from the measurement data as well as the predictions of the two advanced models. This is mainly due to the fact that pile installation significantly influences the fabric orientation and structure of the surrounding natural soils (Figs. 16 and 17), as well as their yielding characteristics, and these are the aspects of the natural soil behavior that are not taken into account by the MCC model.

Despite undrained expansion of cavity, considerable differences can be distinguished between numerical predictions of SCLAY1S and Creep-SCLAY1S models during equalization period (Figs. 18−21). This can be reasonably expected as the influence of creep increases with time. However, similar comparative studies by Sivasithamparam et al. (2015) showed that even during undrained loading stage, consideration of time-dependency has significant effects on the numerical simulation results, and hence it should be taken into account (particularly when modeling the behavior of soft and sensitive clay). The effects that pile setup has on the variations of soil anisotropy and natural structure, both after installation and consolidation periods, are well-pronounced in Figs. 18−21. From a qualitative standpoint, both models provide predictions which
are consistent with the experimental results. For instance, the experimental measurements indicate that as a result of total stress relaxations during consolidation, the final radial effective stresses become less than their corresponding initial values (Randolph 2003). Both models provide qualitatively similar results while it is the creep model that predicts more quantitatively consistent representation of the field measurements (see Fig. 9).

One of the main advantages of the recently developed Creep-SCLAY1S model is that, unlike the majority of visoplastic models that are based on Perzina's overstress theory (Hinchberger and Rowe 2005; Karstunen and Yin 2010), its viscous (i.e., creep) parameters have clear physical meaning and are relatively simple to determine. As indicated earlier in the paper, compared to the MCC the additional parameters of the S-CLAY1 family of models are physically plausible parameters with established procedures for their determination that are well-explained in the literature. This simplicity of parameter determination, and the fact that these advanced models are hierarchical extensions of the widely used MCC model, makes their practical application reasonably straightforward.

Conclusions

Piles are designed to carry loads for a long period of time. During pile installation, the soil around the pile experiences plastic deformations, destructuration, and pore pressure variations. These effects are more pronounced on natural clayey deposits, mainly due to their high sensitivity and low permeability. The consequences of soil alteration are essential on pile capacity; therefore, evaluation of the long term soil modification around the pile is important for proper design and construction of pile foundations, particularly in natural cohesive soils. In the present paper, alteration of a soft clayey soil due to installation of close-ended pile has been numerically investigated. For this purpose, two advanced constitutive models of S-CLAY1 family, which
account for soil anisotropy, destructuration and time effects (in case of the creep model) have been used. Using fully integrated implicit numerical scheme, these models have been implemented as user-defined models in PLAXIS 2D and were employed to investigate the soft soil response to pile setup. The advanced constitutive models provided reliable predictions of soil behavior, variations of pile capacity and soil’s structural alteration with time. To highlight the significance of considering natural features of soil behavior in the modeling, corresponding numerical predictions of MCC model have also been provided. The comparison between the predictions of the time-dependent model against field measurements of the case study pile validated the capability of the Creep-SCLAY1S model in qualitatively and quantitatively capturing the observed soil behavior. These comparisons also illustrated the shortcomings of classical MCC model and supported the impact of considering soil natural features for a reasonably accurate and reliable numerical modeling work. The series of sensitivity analyses that has been carried out showed that the variations of initial values of yield surface inclination and bonding parameters have almost negligible effects on numerical predictions. Furthermore, these analyses showed that, while time-independent and time-dependent S-CLAY1-based models provide reasonably comparable results of the soil behavior after pile setup, consideration of time effects better represent the changes in radial effective stresses (known as the underlying mechanism of pile installation effects for displacement piles in soft clays) that occur during installation and subsequent dissipation of excess pore pressures.

References


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Figure Captions:

**Fig. 1** Yield surfaces of the S-CLAY1S model in a) general stress space, and b) triaxial stress space (CSL, critical state line).

**Fig. 2** Schematic of the current state surface (CSS) and normal consolidation surface (NCS) of the Creep-SCLAY1 model (in triaxial stress space).

**Fig. 3** Configuration of the Imperial College test piles (Lehane and Jardine 1994).

**Fig. 4** Variations of a) OCR with depth obtained from oedometer tests, and b) end resistance $q_c$ and pore pressure $u_c$ with depth obtained from in-situ piezocone tests (data from Lehane and Jardine 1994).

**Fig. 5** Geometry of the boundary value problem and the idealised soil profile.

**Fig. 6** Comparison between measured and predicted values of radial total stress $\sigma_{ri}$, after pile installation ($\sigma_{h0}$ is the initial undisturbed horizontal stress) (data from Lehane and Jardine 1994).

**Fig. 7** Comparison between measured and predicted values of pore pressure $u_s$, after pile installation (data from Lehane and Jardine 1994).

**Fig. 8** Comparison between measured and predicted values of a) pore pressure; b) radial total stress; c) radial effective stress, during equalization (data from Lehane and Jardine 1994).

**Fig. 9** Comparison between measured and predicted values of radial effective stress after equalization (data from Lehane and Jardine 1994).
Fig. 10 Simulation results for variations of undrained shear strength due to pile jacking a) after installation, and b) after equalization.

Fig. 11 Simulation results for relative variations of undrained shear strength with time.

Fig. 12 Effect of anisotropy parameter alterations on radial effective stress predictions after equalization (data from Lehane and Jardine 1994).

Fig. 13 Effect of destrucution parameter alterations on radial effective stress predictions after equalization (data from Lehane and Jardine 1994).

Fig. 14 Effect of anisotropy parameter alterations on variations of radial effective stress during equalization (data from Lehane and Jardine 1994).

Fig. 15 Effect of destrucution parameter alterations on variations of radial effective stress during equalization (data from Lehane and Jardine 1994).

Fig. 16 Simulation results for relative variations of destrucution parameter due to pile setup.

Fig. 17 Simulation results for relative variations of $\alpha_0$ due to pile setup.

Fig. 18 Changes of $\alpha_x$ due to pile setup with different initial anisotropy values.

Fig. 19 Changes of $\alpha_y$ due to pile setup with different initial anisotropy values.

Fig. 20 Changes of $\alpha_r$ due to pile setup with different initial bonding values.

Fig. 21 Changes of $\alpha_y$ due to pile setup with different initial bonding values.
Table 1. Model parameter values for Bothkennar clay.

<table>
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<tr>
<th>Parameter</th>
<th>Value</th>
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<td>Anisotropy</td>
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<tr>
<td>Structure</td>
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Table 2. Additional creep parameter values for Bothkennar clay.

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<td>$\mu_1^*$</td>
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<td>$\tau$</td>
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Table 3. Permeability values for Bothkennar clay deposit.

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<th>Depth (m)</th>
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<th>$k_V$ (m/day)</th>
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<td>1.21x10^{-4}</td>
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<tr>
<td>1-6</td>
<td>1.21x10^{-4}</td>
<td>5.96x10^{-5}</td>
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