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Atomic structure study of the pyrochlore Yb$_2$Ti$_2$O$_7$ and its relationship with low-temperature magnetic order

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Abstract

There has been great interest in the magnetic behavior of pyrochlore oxides with the general formula $A_2B_2O_7$, in which rare-earth ($A$), and transition metal ($B$) cations are ordered on separate interpenetrating lattices of corner-sharing tetrahedra. Such materials exhibit behaviors including quantum spin-ice, (quantum) spin-liquid, and ordered magnetic ground states. Yb$_2$Ti$_2$O$_7$ lies on the boundary between a number of competing magnetic ground states. Features in the low-temperature specific heat capacity that vary in sharpness and temperature from sample to sample suggest that in some cases the magnetic moments order, while in others the moments remain dynamic down to temperatures as low as $\sim$16 mK. In this work, three different Yb$_2$Ti$_2$O$_7$ samples, all grown by the optical floating zone technique but exhibiting quite different heat capacity behavior, are studied by aberration-corrected scanning transmission microscopy (STEM). Atomic-scale energy-dispersive X-ray analysis shows that a crystal with no specific heat anomaly has substitution of Yb atoms on Ti sites (‘stuffing’). We show that the detailed intensity distribution around the visible atomic columns in annular dark field STEM images is sensitive to the presence of nearby atoms of low atomic number (in this case oxygen) and find significant differences between the samples that correlates both with their magnetic behavior and measurements of Ti oxidation state using electron energy loss spectroscopy. These measurements support the view that the magnetic ground state of Yb$_2$Ti$_2$O$_7$ is extremely sensitive to disorder.

Keywords: pyrochlore; magnetic frustration; Yb$_2$Ti$_2$O$_7$; annular dark field STEM; atomic resolution EDX

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I. INTRODUCTION

Pyrochlore oxides with general formula $A_2B_2O_7$, in which $A$ is a rare-earth ion and $B$ is a transition metal, exhibit a variety of interesting magnetic properties [1]. The $A$ and $B$ cations lie on distinct but interpenetrating lattices of corner-sharing tetrahedra. Such a lattice is incompatible with a simple organisation of magnetic moments and leads to geometric frustration [1]. By analogy with the large ground-state entropy of crystalline H$_2$O [2], which has an oxygen lattice of corner-sharing tetrahedra, the ground states of many magnetic $A_2B_2O_7$ materials have been proposed to be a spin-ice [1]. In a spin-ice, each tetrahedron has two spins pointing inwards and two outwards (so-called ice rules [1,3]). Nevertheless, other unusual behaviors have been observed in $A_2B_2O_7$ pyrochlores, including spin glass [4-6], and spin liquid [4] states, as well as magnetic configurations modified by quantum fluctuations [1,7-10]. The qualities of any given $A_2B_2O_7$ compound are principally dictated by the elements $A$ and $B$, but can be strongly altered by structural defects, particularly ‘stuffing’ of magnetic $A^{3+}$ ions onto nonmagnetic $B^{4+}$ sites and oxygen, $A$-site or $B$-site vacancies [1,7-10].

Here, we examine Yb$_2$Ti$_2$O$_7$. The picture for this material is complicated by reports of different results for polycrystalline and single crystal samples, and for different samples with nominally identical form, stoichiometry, and structure [11-13]. An early study found a peak in the temperature dependence of the heat capacity of Yb$_2$Ti$_2$O$_7$ at 214 mK [14], consistent with later neutron scattering, muon spectroscopy, and magnetization studies that associate the heat capacity anomaly with a first-order transition to ferromagnetic long-range magnetic order [13,15-18] with a collinear or nearly collinear magnetic structure [15,16], an ice-like splayed ferromagnetic structure [19] or all-in-all-out splayed ferromagnetic structure [20]. Other works have proposed that this system is a quantum spin-ice [11,12,21,22] or quantum spin liquid [23,24], or adopts a ground state with short-range correlations where the magnetic moments continue to fluctuate down to temperatures as low as 16 mK [25-27].

The origin of these discrepancies probably lies in subtle structural differences and a proximity to one or more magnetic phase boundaries [28-30]. In such a case, even small perturbations in exchange parameters, which could be driven by a number of (competing) factors, might be expected to produce significant changes in the nature of the magnetic ground state. Small differences in stoichiometry are known to have significant effects on the properties of Yb$_2$Ti$_2$O$_7$. For many rare earth pyrochlores, ‘stuffing’ of excess $A^{3+}$ ions onto the Ti$^{4+}$ site happens much more readily than ‘anti-stuffing’ of Ti onto the $A$-site [31]. This also seems to be the case for Yb$_2$Ti$_2$O$_7$; Ross and co-workers found that neutron diffraction of Yb$_2$Ti$_2$O$_7$ prepared as a powder was best fit by a stoichiometric model, while a float-zone grown single crystal, (prepared from stoichiometric starting materials), was best described
by stuffing of Yb onto 2.3% of Ti sites, rather than Ti vacancies or anti-stuffing [11]. However, Baroudi and co-workers in a synchrotron X-ray diffraction study proposed that Yb, being the smallest of the rare earth atoms, could swap with Ti, producing up to 2% anti-site defects in their Yb$_2$Ti$_2$O$_7$ powders [31].

We employ aberration-corrected scanning transmission electron microscopy (STEM) to investigate three different samples that have quite different low-temperature heat capacity behavior, in conjunction with atomically-resolved energy-dispersive X-ray spectroscopy (EDX) and electron energy loss spectroscopy (EELS). While diffraction studies, such as those mentioned above, measure average structure, electron microscopy at atomic resolution offers the opportunity to directly observe defects such as stuffing and atom swapping between cation sites as well as providing average measurements from regions several nm in size. We find significant differences between the samples that correlate with their magnetic behavior.

In order to interpret atomic resolution images of Yb$_2$Ti$_2$O$_7$ the pyrochlore structure ($Fd\bar{3}m$) [32] must be considered. One way to understand the structure of Yb$_2$Ti$_2$O$_7$ is examination of $\{111\}$ planes as shown in Fig. 1(a). On these planes, sheets of metal atoms have a hexagonal Kagome pattern and alternate between Yb$^{3+}$ (light blue) and Ti$^{4+}$ (dark blue) in Fig. 1. In each Yb layer, Ti atoms sit at the centre of an Yb hexagon (top, Fig. 1(a); most oxygen atoms have been omitted for clarity). These Ti atoms also lie at the vertex of a pair of opposing Ti tetrahedra that link to the Ti Kagome layers above and below. A similar pattern is found for Yb atoms in the Ti Kagome layer (bottom, Fig. 1(a)). Each metal atom is surrounded by an octahedron of oxygen ions that either lie on a Wyckoff $f$-site (red) or $b$-site (yellow). Note that all the cations of the same type are symmetrically identical, and this pattern is found on all of the symmetrically equivalent $\{111\}$ layers. Crystallographic parameters for a perfect Yb$_2$Ti$_2$O$_7$ crystal [33] are listed in Table SI in Supplemental Material [34].

When viewed along $[211]$, one set of $\{111\}$ planes is seen edge-on. In this projection there are four types of heavy atom column (Fig. 1(c)); those containing only Yb, those containing only Ti, and two different mixed ($M$) columns containing 50% Ti and 50% Yb. The difference in $M$ columns arises because there are twice as many oxygen atoms around 50:50 columns in the Yb Kagome layer ($M1$) in comparison with 50:50 columns in the Ti Kagome layer ($M2$). In this projection the oxygen atom columns lie $\sim$72 pm from the $M1$ columns while those next to $M2$ columns lie at a distance of $\sim$49 pm. The large difference in scattering power between oxygen and the metal atom columns with high Z in such images effectively renders oxygen invisible in comparison with adjacent atoms [35-37].
FIG. 1. (a) The pyrochlore structure of Yb$_2$Ti$_2$O$_7$ (see text for details). (b) [211] annular dark field STEM image of Yb$_2$Ti$_2$O$_7$ with Yb and Ti tetrahedra overlaid (scale bar is 1 nm). Four different types of atom columns are visible, marked by circles. The Yb columns are the brightest, followed by mixed columns $M1$ and $M2$, while the Ti columns are the faintest. (c) Corresponding projection of the crystal structure showing the Kagome layers and the four different types of atom column. Voronoi cells, used for measurement of intensities in the image, are illustrated in green in (b) and (c).

Our interest lies in the purity of the Yb and Ti sublattices – and the effect on adjacent oxygen atoms – that may result from the presence of an Yb atom on a Ti site, or vice versa. We thus consider a simple model in which an atomic column, which is nominally comprised completely of atoms of type $X$ in perfect material, has some atoms replaced by others of type $Y$. Now, moving atoms between different cation sublattices must involve changes in oxidation state and/or anion populations in order to maintain charge balance; rearrangements of oxygen atoms or oxygen vacancies may be necessary. We will return to these points later, but begin by assuming that there is no correlation between the different substitution sites, i.e. that there is no clustering or repulsion between substituted sites and there are no vacancies, interstitials or impurity atoms. In such a simple case, with a probability $p_{XY}$ for an atom of type $X$ to be replaced by one of type $Y$, the probability of finding a column of $n$ atoms which contains $m$ type $Y$ atoms is given by the binomial distribution, i.e.

$$P\left(\frac{n}{m}\right) = \frac{n!}{m!(n-m)!} (1-p_{XY})^{n-m} p_{XY}^m.$$

Thus, even stuffing of a few percent [11,31] should be detectable in compositional analysis sensitive to single atoms at the atomic scale (Fig. 2). For the [211] zone axis and a moderate specimen thickness
of 45 nm, replacement of 1% gives more than 50% of atomic columns that contain at least one foreign atom (yellow curve). Even if only 0.4% of atoms are replaced by a different type, more than 20% of atomic columns will have one foreign atom (red curve). Conversely, unaffected columns only form a small fraction of the image if significant amounts of stuffing occur; only 10% have no foreign atom at a stuffing of 3% (violet curve). Importantly, at stuffing fractions of a few percent, adjacent columns with widely differing substitutions should be quite common.

FIG. 2. The fraction of columns with 73 atoms that have between zero and five foreign atoms predicted by (Eq. 1), for different amounts of average atom swapping (0.4% to 3%). This is equivalent to a [211] Yb$_2$Ti$_2$O$_7$ specimen with thickness 45nm.

Aberration-corrected STEM images such as Fig. 1(b) contain quantifiable composition information [38,39] due to the atomic number sensitivity of high-angle (Rutherford) electron scattering [40-43]. Thus, it may be expected that analysis of image intensities may provide data that is sensitive to the composition of the Yb and Ti sublattices. Several schemes for quantitative analysis of annular dark field (ADF) images have been proposed. LeBeau and co-workers [44] have used the maximum pixel intensity in the vicinity of the centroid of each atom image, while Van Aert and co-workers assume the intensity of each atom column is a cylindrically-symmetric 2D Gaussian, and perform a least-squares fit. Neither of these is appropriate for the current case, where unresolved oxygen atoms lie close to the metal atoms; rather, we use intensities integrated over a Voronoi cell surrounding the atom column of interest. A Voronoi cell is an area bounded by the perpendicular bisectors of all vectors that link adjacent atom columns [40,45-47]. The mean integrated intensity in a Voronoi cell is proportional to the scattering cross section of the atom column, while retaining a useful degree of insensitivity to exact experimental conditions such as defocus and spatial incoherence [43]. For the [211] projection, the Voronoi cell is a simple rectangle as shown in Figs. 1(b) and 1(c). Nevertheless, the contrast of atomic
columns may not be directly interpretable in terms of composition, e.g. due to static atomic displacements [48,49] that may be a result of stuffing.

Here we show that O vacancies, along with stuffing of Yb atoms onto the Ti sites, are responsible for the breakdown of the long-range magnetic ordering in Yb$_2$Ti$_2$O$_7$ pyrochlore, resulting in a material that exhibits only short-range order or in which magnetic ordering is absent down to the lowest temperatures measured.

II. METHODS

We investigated three Yb$_2$Ti$_2$O$_7$ single crystals prepared by the floating zone method with quite different low-temperature specific heat characteristics. Stoichiometric quantities of Yb$_2$O$_3$ and TiO$_2$ powder were mixed, pressed into rods and then sintered at 1150 °C (Sample 1 and Sample 3) or 1350 °C (Sample 2) for 24 hours. Using these rods, single crystals were grown in air at a rate of 1.5 mm/h (Sample 1 and Sample 3) or 2 mm/h (Sample 2). The crystals had a typical diameter of ~6 mm and a length of 20 to 30 mm. The samples were used in the previous published works [15,16,18]. As shown in Fig. 3, Sample 1 exhibits a sharp transition at ~200 mK, consistent with the onset of long-range magnetic order, typical of stoichiometric powder samples although at a reduced temperature. Sample 2 shows two relatively broad anomalies at ~200 mK and 280 mK. This type of behavior could be explained by short-range magnetic ordering, with the magnetic correlation length limited by defects [11]. Finally, Sample 3 exhibits no clear specific heat anomaly, consistent with a disordered magnetic state, and is thus expected to have significant stuffing of Yb$^{3+}$ onto the Ti$^{4+}$ sites [11].

![FIG. 3. Specific heat as a function of temperature for the three Yb$_2$Ti$_2$O$_7$ samples in zero magnetic field [15,16,18].](image.png)
In order to avoid any issues associated with sample inhomogeneity and to be able to compare the microscopy and heat capacity results directly, the TEM specimens were taken from the same thin sections of the crystal used for the heat capacity measurements. Then, the TEM specimens were prepared using standard routes, i.e. mechanical grinding and polishing followed by ion milling to electron transparency using Ar$^+$ at 6 keV. Surface damage was minimised by a final low energy milling step at 500 eV. Images were obtained with a doubly-corrected JEOL ARM200F microscope at 200 kV. Defect-free, flat and uniform regions of interest were selected with thicknesses characterised using low-loss EELS [50], chosen to be $t/\lambda \approx 0.76$, i.e. ~45 nm. In order to obtain data with a good signal to noise ratio, unaffected by specimen drift, up to sixty images were collected sequentially, all with a short time of 10 µs/pixel. The resulting set of images was aligned using normalized cross-correlation and summed to produce high quality, low noise data.

At small scattering angles, i.e. when the inner angle of the ADF detector is only a little larger than the probe convergence angle $\alpha$, coherent diffraction effects can produce strain contrast that is very sensitive to crystal orientation that compromises the ability to relate intensities to atomic number [38]. Here, therefore, for images intended to be sensitive to composition we use an ADF detector inner angle at least 4.6 times the probe convergence angle $\alpha$, giving a scattered intensity proportional to a small power of the atomic number, $Z^{1.5}$ to $Z^2$ [51,52]. For images that show greater sensitivity to the configurations of oxygen atoms we use an ADF detector inner angle of only $\sim 2.4\alpha$. Data were normalized to the incident beam intensity using calibrated brightness/contrast levels, a map of the ADF detector response and an image of the diffraction pattern falling on the detector, following an approach similar to that of LeBeau and co-workers [53]. EDX measurements were obtained with a windowless Oxford Instruments X-max 100 silicon drift X-ray detector. EEL spectra were obtained with a Gatan Quantum EELS system operating in dual EELS mode, allowing correction of zero-loss offsets and removal of multiple scattering from high energy core-loss edges by Fourier-log deconvolution calculated from the low loss spectrum. Image simulations were performed with QSTEM [54] and STEMsim [55] multislice to compare with experimental data.

III. RESULTS

A. Annular dark field STEM intensities

Representative [211] annular dark field STEM images from the three samples are shown in Figs. 4(a-c), taken with an ADF detector inner angle of $2.4\alpha$. Voronoi intensity measurements for Sample 1 are shown in Figs. 4(d-f) (equivalents for Samples 2 and 3 are shown in Fig. S1 provided in
supplementary information). The four sublattices are readily distinguished in the false color image Fig. 4(d) and the intensity histogram Fig. 4(e). The higher mean intensity of $M1$ in comparison with $M2$ is caused by the presence of four oxygen columns in the Voronoi cell of every $M1$ column in comparison with two for $M2$ (Fig. 1(c)). Thus, even though oxygen atoms cannot be resolved in these ADF-STEM images it is clear that their effect can be seen in quantitative intensity measurements.

FIG. 4. ADF-STEM images taken with an ADF detector inner angle of 2.4 $\alpha$, (a) Sample 1, (b) Sample 2 and (c) Sample 3, viewed along [2 1 1] (scale bar is 2 nm) (d) shows extracted mean integrated intensities from (a) using Voronoi cells centred on each atomic column, plotted as a histogram in (e). Normalizing the intensities from each sublattice separately shows the intensity variations across the image (f). Mean radial intensity profiles for Sample 1 (g), Sample 2 (h) and Sample 3 (i).
One might hope that the range of intensities in the histograms for each type of atom might be governed in some way by Eq. (1). However, if the four sublattice intensities are each normalized separately to a range between zero and one (Fig. 4(f)) it becomes apparent that there is a systematic variation across the image, presumably due to a small variation in specimen thickness. The width of the intensity histograms in Fig. 4(e) is thus mainly caused by this thickness variation rather than atomic substitutions. Similar variations are present for Samples 2 and 3 (see supplementary Fig. S1). These thickness variations and/or damage/contamination of the specimen surface are sufficient to mask statistical measurements of stuffing, or anti-stuffing, from the ADF intensities of atomic columns, i.e. changes in the number of atoms per column \( n \) easily produce differences that are equal to or larger than the effect of a few atomic substitutions.

The difference in \( M1 \) and \( M2 \) column intensities indicates a sensitivity of ADF data to nearby oxygen atoms. We therefore investigated mean radial intensity as a function of distance from the centre of the visible atom columns, averaged over all equivalent columns in the images of Figs. 4(a-c). These mean radial intensity profiles are shown in Figs. 4(g-i), where the centre of the atom column is at the origin and the mean radial intensity decays following a quasi-Gaussian profile. In sample 1, the \( M2 \) columns have a higher peak intensity (Fig. 4(g)), consistent with oxygen atom columns close to their centres (49 pm in the nominal structure). The radial intensity of the \( M1 \) columns decays more slowly, consistent with more oxygen atom columns at larger distances (72 pm in the nominal structure). The intensity of \( M1 \) columns exceeds that of \( M2 \) columns at a radius of \( \sim 65 \) pm (see also Fig. S2(a) and Fig. S3 in Supplemental Material [56]). The same trend is observed in multislice simulations of the nominal Yb\(_2\)Ti\(_3\)O\(_7\) structure (Fig. S2(d) in Supplemental Material [56]), with the intensity at \( M2 \) columns becoming smaller than that of \( M1 \) columns at a certain radius depending the sample thickness.

Interestingly, the higher peak intensity of \( M2 \) columns shown in Fig. 4(g) is only found in Sample 1; for Samples 2 and 3, as illustrated in Figs. 4(h) and 4(i), the radial intensity of \( M2 \) never exceeds that of \( M1 \) (see also Figs. S2 in Supplemental Material [56]). This effect could be caused by fewer oxygen atoms in the Wyckoff \( f \)-site or their movement away from \( M2 \) columns, which would reduce the \( M2 \) intensity at small radii, and/or movements of \( f \)-site and \( b \)-site oxygen atoms closer to \( M1 \) columns, which would increase their intensity at small radii.

**B. Atomic resolution EDX**

Sample 3 is the most likely of the three samples to exhibit stuffing. Atomic columns with anomalous contrast in comparison with their neighbours in ADF images were observed, as shown in Fig. 5.
Anomalously bright Ti columns, consistent with stuffing of Yb onto Ti sites were observed (Fig. 5(a)) as well as anomalously dark Yb columns, consistent with anti-stuffing of Ti onto Yb sites (Fig. 5(c)). These were examined with atomic resolution EDX. Fig. 5(b) shows an EDX line scan across an anomalously bright Ti column, made using Ti $K\alpha$ (4.51 keV) and Yb $L\alpha$ (7.41 keV) X-rays. There is an obvious drop in Ti signal, and an increase in the Yb signal, for the brighter column in comparison with the others, particularly those to the left. The correlation between bright atom column contrast and a lower Ti / higher Yb signal was observed several times (see Fig. S4 in Supplemental Material [57]) and is direct evidence for stuffing in this sample. Figure 5(d) shows a line of Yb-$M1$ columns, in which a small Ti signal can be seen at each Yb column as well as the expected signal at the $M1$ columns. While this may indicate anti-stuffing of Ti onto Yb sites, it is also possible that a small amount of specimen drift (0.2 nm) during acquisition introduced some signal from the adjacent Ti-$M2$ row of atoms.

FIG. 5. ADF-STEM and EDX analysis of Sample 3. (a) Anomalously bright intensity from a Ti column. (b) Atomic scale EDX analysis along a line of Ti and $M2$ atom columns, showing a decrease in Ti signal and increase in Yb signal at an anomalously bright Ti atom column. (c) Anomalously weak intensity from a Yb atom column. (d) Atomic scale EDX analysis along a line of Yb and $M1$ atom columns.
C. EELS

Analysis of Yb$_2$Ti$_2$O$_7$ at atomic resolution using EELS is possible using the Ti-$L_{3,2}$ edge at $\sim$450 eV and the Yb-$N_{4,5}$ edge at 185 eV, although spatial resolution is limited for the latter due to delocalization effects [50], limiting the analysis to the [110] zone axis. Nevertheless, electron energy loss near-edge structure (ELNES) spectra can be used to obtain information on Ti bonding configurations [58-60]. Metallic Ti shows two white lines $L_3$ and $L_2$ at 456 eV and 462 eV, due to electron transitions from 2$p_{3/2}$ and 2$p_{1/2}$ subshells to unoccupied 3$d$ states respectively. In titanium oxides, the number of peaks in the Ti-$L_{3,2}$ ELNES spectrum depends on valence state, coordination and site symmetry of the Ti atoms [59]. In materials with a Ti oxidation state of +4, like Yb$_2$Ti$_2$O$_7$, titanium core-holes created by excitation of 2$p$ core electrons can be poorly screened since there is no electron in the Ti$^{4+}$ conduction band. Consequently, both $L_3$ and $L_2$ edges are shifted to higher energy losses than for metallic Ti [59]. Octahedral coordination of Ti atoms with oxygen splits the degenerate unoccupied 3$d$ states into a lower energy 2$t_{2g}$ molecular energy level and a higher 3$e_g$ level [61]. Hence, in Yb$_2$Ti$_2$O$_7$ the Ti $L_3$ and $L_2$ edges both consist of two white lines, $\alpha$ and $\beta$ for $L_3$ and $\gamma$ and $\delta$ for $L_2$. In fact, for each edge the first ($\alpha, \gamma$) and second ($\beta, \delta$) peak are due to transitions from the 2$p$ state to the 2$t_{2g}$ ($\pi^*$) and 3$e_g$ ($\sigma^*$) oxide levels, respectively.

A decrease in Ti valence, for example due to oxygen vacancies, has two effects on Ti-$L_{3,2}$ ELNES: a) a systematic shift to lower energies of $\sim$2 eV per valence state [59]; and b) the intensity ratios $I_\beta/I_\alpha$, $I_\delta/I_\gamma$ and $I_\beta/I_\delta$ all trend to larger values [58,59]. These changes are very sensitive indicators of change in Ti valence.

The experimental spectra from the three samples are shown in Fig. 6(a). Peak energies, extracted by fitting the data to four Lorentzian curves (Fig. 6(b)), as well as intensity ratios are listed in Table I. All of these indicators show that the Ti valence drops from Sample 1 to Sample 2 and still further for Sample 3.
FIG. 6. (a) Experimental EEL Ti $L_{2,3}$ spectra of the three samples ($t/\lambda = 0.30$). (b) Lorentzian curves fitted to the experimental EEL spectra shown in (a).

TABLE I. Ti ELNES energies and intensity ratios for the three Yb$_2$Ti$_2$O$_7$ samples.

<table>
<thead>
<tr>
<th></th>
<th>Sample 1</th>
<th>Sample 2</th>
<th>Sample 3</th>
</tr>
</thead>
<tbody>
<tr>
<td>$L_3$</td>
<td>460.08 ± 0.01</td>
<td>459.94 ± 0.01</td>
<td>459.82 ± 0.01</td>
</tr>
<tr>
<td></td>
<td>462.32 ± 0.02</td>
<td>462.23 ± 0.02</td>
<td>462.06 ± 0.02</td>
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<tr>
<td></td>
<td>2.13 ± 0.13</td>
<td>2.33 ± 0.13</td>
<td>2.91 ± 0.17</td>
</tr>
<tr>
<td>$L_2$</td>
<td>465.48 ± 0.02</td>
<td>465.32 ± 0.02</td>
<td>465.24 ± 0.02</td>
</tr>
<tr>
<td></td>
<td>467.74 ± 0.02</td>
<td>467.63 ± 0.02</td>
<td>467.52 ± 0.02</td>
</tr>
<tr>
<td></td>
<td>2.64 ± 0.15</td>
<td>3.13 ± 0.19</td>
<td>2.96 ± 0.18</td>
</tr>
</tbody>
</table>

IV. DISCUSSION

The above results are in agreement with the previous studies of Yb$_2$Ti$_2$O$_7$ that found evidence for Yb stuffing onto Ti sites even in nominally stoichiometric material, and that more stuffing correlates with more diffuse peaks in specific heat capacity. Ross et al. [11] discounted oxygen vacancies as the structural origin of the varying magnetic behavior of Yb$_2$Ti$_2$O$_7$, based on the lack of change in materials subjected to long anneals in an oxygen-rich environment. However, here we find changes in Ti valence that indicate an increasing oxygen vacancy content as stuffing and/or cation site swapping increases from Sample 1 to 3, and this correlates with the changes in magnetic behavior. These apparently contradictory findings can be reconciled by noting that, on average, replacing two Ti$^{4+}$ atoms by Yb$^{3+}$ will be balanced by one O$^{2-}$ vacancy if the Yb sublattice remains unchanged. Stuffing therefore may change the equilibrium oxygen stoichiometry in Yb$_2$Ti$_2$O$_7$, which is quite different to a non-equilibrium oxygen deficiency that can be remedied by annealing.
The EELS data (Fig. 6) thus show a correlation between magnetic properties and oxidation state. In order to link this to the differences in intensity profiles we observe in ADF-STEM data (Fig. 4), and the effects of stuffing, it is necessary to consider the position of the oxygen atoms in the crystal structure. One way to do this is to divide the crystal into regular tetrahedral and octahedral volumes (Fig. 7). Each cation sits at the vertex of six edge-sharing tetrahedra and six corner-sharing octahedra. These are shown for an Yb atom in Figs. 7(a) and 7(b); the octahedra are empty, while each tetrahedron contains an oxygen atom. There are two types of tetrahedron around an Yb atom, shown in colored shading in Fig. 7(b); two tetrahedra are comprised of four Yb\(^{3+}\) ions, 4Yb, with a Wyckoff \(b\)-site O\(^{2-}\) atom at their centres (green), while the remaining six (purple) have two Yb and two Ti atoms, 2Ti2Yb, and a Wyckoff \(f\)-site O\(^{2-}\) atom, displaced well off-centre, close to the mid-point of the edge connecting the Ti atoms. A similar structure surrounds the Ti atoms, except in this case there are six 2Ti2Yb tetrahedra and two 4Ti tetrahedra, comprised of four Ti\(^{4+}\) ions with no oxygen atom inside.

![Figure 7](image_url)

**FIG. 7.** Cation tetrahedra in Yb\(_2\)Ti\(_2\)O\(_7\). (a) Ball and stick model showing the eight cation tetrahedra that have a common vertex at an Yb atom. (b) The same tetrahedra, color-coded as 2Ti2Yb (purple) and 4Yb (green). (c) Ball and stick model showing the eight cation tetrahedra that have a common vertex at a Ti atom. (d) The effect of stuffing an Yb\(^{3+}\) atom onto the Ti\(^{4+}\) site. The six 2Ti2Yb tetrahedra (purple) become 1Ti3Yb and the two 4Ti (orange) become 3Ti1Yb. Stuffing produces an oxygen vacancy in one of the surrounding 1Ti3Yb tetrahedra (highlighted in red) and the conversion of an adjacent Ti atom from 4\(^+\) to 3\(^+\). The network of magnetic 4Yb tetrahedra are also shown, with six numbered 4Yb tetrahedra surrounding the stuffed atom site. (e) The Yb tetrahedra shown in (d) without any stuffing and possible all-in-all-out [20] (the left Yb tetrahedra) and two-in-two-out [20] (the right Yb tetrahedra) splayed ferromagnetic configurations (black arrows are along [1 0 0]). (f) Position of the oxygen atoms in the vicinity of the Ti atom (marked by a yellow star) before stuffing. (g) Frustrated triangular lattice of magnetic cations formed by replacing a Ti atom with Yb. (h) Formation an oxygen vacancy and reduction of a Ti\(^{4+}\) cation to Ti\(^{3+}\) as a consequence of stuffing.
Stuffing will change all eight tetrahedra that surround the affected site. A possible structure that results from replacing a Ti\(^{4+}\) atom with Yb\(^{3+}\) is shown in Fig. 7(d). The six 2Ti2Yb tetrahedra become 1Ti3Yb tetrahedra (purple) and the two 4Ti tetrahedra change to 3Ti1Yb. No other ytterbium titanates have been documented that could be used as a guide to the structural changes that will result, but we note that Ti-O bond lengths are much shorter than Yb-O bond lengths (~1.95 Å vs. ~2.3 Å) and Ti-O-Ti bond angles tend to be approximately 130°. Thus, oxygen atoms in the 1Ti3Yb tetrahedra will be displaced away from the stuffed atom towards the Ti atoms at the outer vertices of the orange tetrahedra in Fig. 7(d). Nevertheless, these changes still do not satisfy the normal oxygen bonding configurations with Ti\(^{4+}\) or Yb\(^{3+}\). It therefore seems likely – and is indeed indicated by our EELS results – that replacement of Ti\(^{4+}\) by Yb\(^{3+}\) will result in one of the adjacent Ti atoms reducing to Ti\(^{3+}\) with an accompanying vacancy in that 1Ti3Yb tetrahedron (highlighted red in Figs. 7(d) and 7(h)). Still further changes in structure are possible such as static distortions of the cation framework, with the tetrahedron containing the oxygen vacancy expanding due to Coulomb repulsion. There are likely to be significant effects on the magnetic 4Yb tetrahedra that surround the stuffed atom; there are six nearby 4Yb tetrahedra, numbered in Fig. 7(d). We note that a study of oxygen deficient Y\(_2\)Ti\(_2\)O\(_7\) [10] found that 4Y tetrahedra were much more likely to lose their oxygen atom and it is thus possible that the oxygen vacancy in the red tetrahedron moves into the adjacent 4Yb tetrahedron #2. In any case, tetrahedron #2 is most affected. It is clear from Figs. 7(e) and 7(g) that the replacement of a nonmagnetic Ti\(^{4+}\) cation by a magnetic Yb\(^{3+}\) can modify the nature of the magnetic exchange with the system through formation of the frustrated triangular lattice of magnetic cations. Furthermore, the introduction of a magnetic moment on the Ti site as a consequence of reduction of Ti\(^{4+}\) to magnetic Ti\(^{3+}\) as well as stuffing the Yb atom onto the Ti site will disrupt the magnetic order locally and may serve as pinning sites for magnetic defects (monopoles in spin ice) within the material [10].

The differences between the three samples examined here can be interpreted in terms of such structural rearrangements. As shown in Fig. 8, the [2 1 1] atom columns can be also pictured as chains of tetrahedra. For both the Yb and Ti atom columns the chain consists only of 2Ti2Yb tetrahedra, whereas M1 is made of alternating pairs of 2Ti2Yb and 4Yb tetrahedra and M2 is made of alternating pairs of 2Ti2Yb and 4Ti tetrahedra. There are 10 cations in the repeat motif in all cases, and each atom column type has a different Yb:Ti ratio in its tetrahedral chain.
FIG. 8. The four types of [2 1 1] atom columns in Yb$_2$Ti$_2$O$_7$, shown as a chain of cation tetrahedra. The black arrow indicates the direction of propagation of the electron beam. Partial transparency highlights the repeat motif of 10 cations; the number of Ti (dark blue) and Yb (light blue) atoms in the motif is given at the bottom of each panel. The [2 1 1] projection of each column is inset bottom right. Color scheme is the same as Fig. 1.

In a stuffed material, the oxygen atom inside a tetrahedron will be affected by all four atoms at its vertices, which means that the oxygen atoms close to any given [2 1 1] atom column depend upon the chains of tetrahedra shown in Fig. 8, not just the atoms in the column. The oxygen atoms are therefore very sensitive to stuffing. Furthermore, the difference in Yb:Ti ratio for each chain means that each has a different sensitivity. Thus, using the same binomial statistics (Eq. 1) for a 45 nm thick TEM specimen, and e.g. 1% stuffing and no anti-stuffing, we find that only 30% of $M$ columns and 50% of Ti columns are directly affected by stuffing (obviously, no Yb columns are affected). However, the nearby oxygen atoms are affected in around 67% of $M_1$ columns, 77% of Ti columns, 89% of Yb columns and 92% of $M_2$ columns. That is, the radial profiles of Yb and $M_2$ columns should be more affected by stuffing than the Ti and $M_1$ columns and this does indeed appear to be the case in Figs. 4(g-i). Furthermore, the structural rearrangements illustrated in Fig. 7 will tend to move oxygen atoms away from $M_1$ columns more readily than $M_2$ columns, producing the changes in radial profile shown in Figs. 4(g-i).

Taken together, the modifications to the delicate balance of magnetic interactions, which result from the stuffing and changes in Ti valence that we have observed, will lead to a breakdown in the onset of
long-range ferromagnetic order. These results are consistent with the magnetic properties of Sample 3 (Fig. 1(a)) showing no clear transition in the specific heat down to 50 mK.

V. CONCLUSIONS

We have examined three samples of Yb$_2$Ti$_2$O$_7$, with different low temperature specific heat capacity anomalies that indicate varying magnetic properties, using aberration-corrected STEM. We find direct evidence for stuffing of Yb onto Ti sites, using atomic resolution EDX of Ti atomic columns that have anomalously bright contrast, in Sample 3. We also observe Yb atomic columns that have anomalously dark contrast, but are unable to use the well-known compositional sensitivity of ADF-STEM to extract the statistics of stuffing (or anti-stuffing) due to the confounding effects specimen thickness variations and/or surface damage. Nevertheless, we clearly observe the influence of oxygen atoms on these images, and by examining the radial intensity profile of cation columns we observe rather different behavior of oxygen atoms near to the cation columns for the three samples. The sensitivity of the different types of atom column in the [211] ADF-STEM images is explained by considering them as chains of tetrahedra with different Ti:Yb ratios. The changes are consistent with the rearrangement of oxygen atoms away from Yb that occupies Ti sites. Using Ti-$L_{3,2}$ ELNES, we find that these differences in ADF-STEM radial intensity profile are accompanied by changes in Ti valence number, indicating the presence of magnetic Ti$^{3+}$ and oxygen vacancies. Samples that have more diffuse specific heat capacity anomalies have more stuffing, lower Ti valence numbers and more disordered oxygen sublattices.

The methods described here can readily be applied to other pyrochlore systems where a similar sensitivity to structural defects, including stuffing [9], has recently been shown to lead to significant differences in the magnetic behavior, for example, the magnetic ground state of the spin liquid candidate Tb$_2$Ti$_2$O$_7$ [62] and magnetic monopole dynamics in spin ice Dy$_2$Ti$_2$O$_7$ [63]. Studies of this kind should also prove useful in understanding the physics of other frustrated magnets where defects or low levels of doping rapidly modify the physics; examples include triangular lattice magnets such as CuFeO$_2$ and RbFe(MoO$_4$)$_2$, and order-by-disorder transitions that occur in several lattice motifs.

More generally, such methods could play a valuable role in the study of emergent phenomena, including superconductivity and magnetism, both in the bulk and at interfaces, when defects are known to be important.

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References

[34] See Supplemental Material at [URL will be inserted by publisher] for Crystallographic Information.
[56] See Supplemental Material at [URL will be inserted by publisher] for STEM Results.
[57] See Supplemental Material at [URL will be inserted by publisher] for EDS Results.