Development of a high speed and precision wire clamp with both position and force regulations

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Abstract: This paper presents the mechanism and robust control of a monolithic wire clamp to achieve fast and precision operations for strong and robust micro device packaging. The wire clamp is piezoelectrically actuated and a two-stage flexure-based amplification was designed to obtain large and parallel jaw displacements. The grasping forces of the wire clamp were evaluated based on finite element analysis (FEA), and the force measurement was presented. The wire clamp was manufactured using wire EDM technique and the position and force transfer functions were obtained based on the frequency response approach. The position/force switching control strategy was employed to regulate the motion position and grasping force, and the position/force switching controller composed of a PID controller for position control and a sliding model controller (SMC) for force control was designed. Experimental tests were carried out to investigate the performance of wire clamp with the position/force switching controller during the grasping and releasing operations. The results show that the wire clamp exhibits good performance and demonstrate that high speed and precision grasping operations can be realized through the developed wire clamp and the control strategy.

Keywords: Wire clamp, flexure mechanism, mechanical design, position/force regulation

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1. INTRODUCTION

Recently with the rapid development of microelectronic industries, the demand for electronic products with high pin-count IC installations and high assembly density has been increasingly growing[1-3]. As an important cost-effective and flexible interconnecting technology for microdevice packaging, thermosonic wire bonding has been widely used for the microelectronic packaging of nearly any type of daily used electronic products [4]. Automatic wire bonders are important equipments for wire bonding, and high performance wire bonders are required to produce smaller pad size and finer pitch of microelectronic products in extreme conditions[5, 6].

As an important component of automatic wire bonders, wire clamps perform high-frequency open and close operations during wire bonding process, and thus the characteristics of wire clamps can directly affect the packaging quality and efficiency[7]. During the extreme motion with short strokes and high acceleration[8, 9], there will be some undesired disturbances to the wire and wire clamps, affecting the motion of the clamps, which will further have influence on the bonding quality. As a result, it is necessary to develop high performance wire clamps with a novel mechanism and robust controller to provide stable and high speed microelectronic wire bonding.

In the literature, there are some research reported on the wire clamps, most of which mainly focused on the wire clamp actuators and mechanisms, and little attention has been paid to their position/force control issues. The presently used wire clamps usually adopt electromagnetic and piezoelectric actuators as drivers, and they can realize position tracking using position feedback control. However, few of them have a real-time grasping force controller [10, 11]. Even if the grasping forces of some clamps were regulated, the
grasping force control was mainly carried out in indirect ways, such as through the installation of preload springs or force calibration, making it difficult to achieve real time and precision force control. However, the robust position/force control is of great importance for the wire clamps to achieve robust and precision grasping and releasing operations.

The position/force control has been receiving considerable attention from the researchers. Impedance control strategy can be used to indirectly regulate the force using a single controller through establishing the dynamic relation between the force and position or velocity. However, the environmental conditions of wire clamps for thermosonic wire bonding are not always certain, which makes it difficult to accurately control the force using the indirectly control approach \cite{12, 13}. Through hybrid position/force control scheme, the grasping and releasing operations can be implemented by controlling the position of the clamp jaws and monitoring the contact forces at the same time, but the control performance largely depends on the division of force and position subspaces, which requires to accurately identify the environmental constrains \cite{14}. To overcome this issue, intelligent control methodologies, such as fuzzy and neural network control, have been proposed to control forces \cite{15, 16}. However, the calculation amount becomes larger and the practical implementation process becomes more complicated. Hence, a simple yet efficient approach is desirable to realize the stable and precision force/position control of wire clamps.

Intuitively, a position/force switching control can be used to regulate the grasping jaw position and contact force alternately \cite{17, 18}. As for the control scheme, proportional-integral-derivative (PID) controllers have been widely used in industrial
applications. However, traditional PID control can not accomplish the wire clamp position/force regulation, because there may be high-frequency dynamic force vibrations when the jaw contacts with the object during the fast grasping and releasing operations. Some advanced control theories including the robust control [19], adaptive control [20], iterative learning control [21] and neural networks control[22], were presented to control precision positioning systems, which show appropriate level of performance. However, their applications are limited in the fast and precision wire clamp control because of the computationally expensive calculations [23]. Sliding mode control has the advantages of fast response and strong robustness for the disturbances, and thus exhibits great potential for the control of high-speed precision wire clamps [24].

This paper presents the mechanism and robust position/force switching control of a novel monolithic piezoelectric actuated wire clamp. Firstly, the mechanism of the wire clamp is introduced. The grasping force is investigated based on finite element analysis (FEA), and the grasping force measurement is presented. The dynamic models of position and force are obtained through frequency response approach, based on which the position/force switching controller, composed of a PID position controller and a sliding model force controller, is designed. The wire clamp is fabricated, and experimental tests are carried out to investigate the performance of the wire clamp and controller.

2. MECHANISM AND GRASPING FORCE INVESTIGATION

2.1 Configuration of the wire clamp

Figure 1 shows the mechanical structure of the piezoelectric actuated flexure-based wire clamp consisting of a stack piezoelectric ceramic actuator (SPCA), a pair of grasping jaws, a pair of flexible beams, a preload bolt, a base and a flexible motion
transmission mechanism designed as a two-stage amplification including a homothetic bridge type mechanism and a parallelogram leverage mechanism. The SPCA is connected with the flexible motion transmission mechanism by the preload bolt at one end of the SPCA, and the preload force to the SPCA can be adjusted by the bolt. Both of the grasping jaws connected with the motion transmission mechanism through two flexible beams, and because of the space limit, a stain gauge is adopted and surface bonded on the left flexible beam to measure the grasping force during the grasping and releasing operations. In order to avoid shear force and bending torque acting on the actuator, the wire clamp is designed symmetrically along the longitudinal axis of the SPCA. Due to the symmetric architecture, the measurement of a single flexible beam is sufficient. A stain gauge is glued on the base end of the flexible beam where is the maximum stress point under the grasping force to generate a high sensitivity and high signal/noise ratio.

Through the two-stage amplification, the motion transmission and displacement amplification from the SPCA to the grasping jaws are realized. As the first-stage amplification the homothetic bridge-type mechanism is composed of a connecting rod mechanism (A-B-C-D) based on double-notch circular flexure hinges, and its working principle is that once actuated with an input displacement, the device produces two vertical output displacements towards the SPCA. In order to obtain a large displacement amplification ratio, a leverage mechanism (E-F-G) integrated within a parallelogram mechanism (F-G-H-I) at each side of the wire clamp is designed as the second-stage amplification connected with the homothetic bridge-type mechanism by two flexure hinges. Through the parallelogram mechanism pure jaw translations can be realized, thus avoiding the sliding between the wire and jaws during the operations, and more stable
and firm wire grasping can be ensured due to the fact that the grasping force will act normal to the wire compared with the angular grasping mode.

In order to grasp a wire, a voltage should be applied to the SPCA to make it expand and push the homothetic bridge-type mechanism (A-B-C-D); then the homothetic bridge-type mechanism will pull the leverage mechanisms (E-F-G-H-I), which causes the grasping jaws to close to grasp the manipulated wire. After power is switched off, the SPCA retracts to its initial position, causing the grasping jaws to open and release the manipulated wire.

![Diagram of the wire clamp mechanism](image)

**Fig. 1** The mechanism of the wire clamp.

### 2.2 Kinematic analysis of the wire clamp

There are various approaches to model a compliant mechanism, such as the pseudorigidbody (PRB) method\[^{25}\], the compliance matrix method\[^{26}\], the finite element
PRB method is utilized to analyze the kinematic characteristics of the wire clamp. Due to the symmetric architecture, only half of the wire clamp is considered and the kinematic model is established as shown in Fig 2, where \( i \) (\( i = A, B, \ldots, J \)) denotes the rotational centers of flexure hinges. From Fig. 2 it is can be seen that A-B-C-D-E-F is equivalent to a six-bar linkage mechanism with one degree of freedom. Based on the geometric and motion relationships the following equations can be get:

\[
l_{AB}e^{i\varphi_1} + l_{BC}e^{i\varphi_2} + l_{CD}e^{i\varphi_3} = se^{iz/2} \quad (1)
\]

\[
l_{AB}e^{i\varphi_1} + l_{BE}e^{i(\varphi_2 + \alpha)} = l_{AF}e^{i\beta} + l_{EF}e^{i\varphi_4} \quad (2)
\]

where \( s \) is the distance between the flexure hinges A and D, \( \alpha \) is the angle between the linkages BC and BE, \( \beta \) is the angle between linkage AF and the x-axis positive direction, \( l_j \) (\( j = AB, BC, \ldots, AF \)) is the length of the linkage \( j \), \( \varphi_1, \varphi_2, \varphi_3 \) and \( \varphi_4 \) are the initial angular positions of the linkages AB, BC, CD and FE, respectively.

![Fig. 2 The kinematic model of the wire clamp.](image)
Differentiate Eqs (1) and (2) with respect to time and let the real and imaginary parts be equal. The following equation can be obtained:

\[ A \omega = B \hat{s} \]  

(3)

where

\[ A = \begin{pmatrix} l_{AB} \sin \varphi_1 & l_{BC} \sin \varphi_2 & l_{CD} \sin \varphi_3 & 0 \\ l_{AB} \cos \varphi_1 & l_{BC} \cos \varphi_2 & l_{CD} \cos \varphi_3 & 0 \\ l_{AB} \sin \varphi_1 & l_{BE} \sin(\varphi_2 + \alpha) & 0 & -l_{EF} \sin \varphi_4 \\ l_{AB} \cos \varphi_1 & l_{BE} \cos(\varphi_2 + \alpha) & 0 & -l_{EF} \cos \varphi_4 \end{pmatrix}, \quad \omega = \begin{pmatrix} \omega_1 \\ \omega_2 \\ \omega_3 \\ \omega_4 \end{pmatrix}, \quad B = \begin{pmatrix} 0 \\ 1 \\ 0 \\ 0 \end{pmatrix}. \]

The displacement amplification ratio can be calculated as

\[ \lambda = \frac{2d_{out}}{d_{in}} \cong \frac{2\varphi d_{out}}{\varphi d_{in}} = \frac{2\omega l_{FG}}{\hat{s}} = A^{-1}B(4,1)l_{FG} \]  

(4)

where \(d_{in}\) and \(d_{out}\) are the displacements of input end and moveable jaw, respectively.

From Eq. (4), it can be found that the amplification ratio of the wire clamp has no relations with flexure hinges. The amplification ratio can be calculated of 21.7 depending on the geometric parameters of the linkages.

The kinematic characteristics of the wire clamp were investigated using FEA, and the finite element model was established with the aid of ANSYS software. The actuation displacement was applied by the SPCA on the input terminal of the wire clamp, and the deformation behavior of the jaw as well as flexure hinges and moving linkages under the input displacement of 10μm applied by the SPCA is shown in Fig. 3. The maximum displacement of a jaw can reach 97μm which can enable firm and robust grasping operations with a large range of wires. Thus the displacement amplification ratio of the wire clamp is 19.4, which is in good agreement with the calculated result.
2.3 Grasping force analysis

FEA was carried out to analyze the grasping force of the wire clamp. Since the grasping force that the jaws apply on the wire can be affected by the initial position between the jaws and the wire, the sketch of jaws and wire is defined and shown in Fig. 4, where $D$ is the initial distance between the jaws, $d$ is the diameter of wire and $\delta$ is the distance between the jaw and wire. The FEA model was established using ANSYS software, and the physical and mechanical parameters of the wire clamp are listed in Table 1.
Table 1 Physical and mechanical parameters of the wire clamp.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Young’s modulus (GPa)</th>
<th>Tensile (MPa)</th>
<th>Poisson’ ratio</th>
<th>Density (kg/m³)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Value</td>
<td>71.7</td>
<td>503</td>
<td>0.33</td>
<td>2810</td>
</tr>
</tbody>
</table>

For FEA, the surfaces of the two fixing holes were fixed through applying zero displacements, and the input displacements with a range from 0 μm to 10 μm were applied on the input terminal of the wire clamp and the grasping force under the input displacement was extracted when δ = 40 μm, δ = 50 μm and δ = 60 μm, respectively. The relationship between the grasping force and the input displacement is summarized in Fig. 5. From Fig. 5, it can be seen that the grasping force is zero before the jaws contact the wire, and increases linearly with the input displacement after contact. When δ = 40 μm, δ = 50 μm and δ = 60 μm, the maximum grasping forces can reach 206.12 mN, 167.08 mN and 128.06 mN, respectively.
2.4 Grasping force measurement

It is necessary to accurately measure the grasping forces before control them. The stain gauge glued on flexible beam can sense the force applied to it as a change in resistance, which is produced by the strain induced by the applied force. In order to reduce the stress concentration of the flexible beam, two fillets are adopted to connect the jaw and end of the parallelogram mechanism, respectively, which is shown in Fig. 1. According to the bending deformation theory of flexible beams, the strain of the flexible beam at the position of the stain gauge can be calculated as

\[ \varepsilon_b = \frac{6F}{EBh^2} \delta \]  

where \( F \) is the grasping force applied on the jaw, \( L_s \) is the distance between the point of applying force and the strain gauge, \( E \) is the Young's Modulus of the material, \( B \) is the beam thickness, and \( h \) is the beam width.

The resistance change of the strain gauge is given by
\[ \Delta R = \varepsilon_b S_g R_0 \] (6)

where \( \varepsilon_b \) is the beam strain, \( S_g \) is the gauge factor of the strain gauge and \( R_0 \) is the nominal resistance of the strain gauge.

The strain gauge is then connected to a Wheatstone bridge whose output is connected to a dynamic strain gauge to amplify the signal. The output voltage of the strain gauge is given by

\[ U_{\text{out}} = \frac{n}{4} k_s \varepsilon_b S_g U_b \] (7)

where \( n \) denotes the number of the strain gauges in Wheatstone bridge, \( k_s \) is the amplification ratio of the dynamic strain gauge, and \( U_b \) is the excitation voltage of the Wheatstone bridge.

Substituting Eq. (5) into Eq. (7), yields

\[ U_{\text{out}} = \frac{3nk_s L_s S_g U}{2EBh^2} F \] (8)

Based on Eq. (8), the following equation can be obtained:

\[ F = \Re U_{\text{out}} \] (9)

where \( \Re = \frac{2EBh^2}{3nk_s L_s S_g U} \).

Equation (9) describes the relationship between the grasping force applied on the jaw and the output voltage of the strain gauge. It can be found that it is a linear relationship between the grasping force and the output voltage on the condition that the parameters of the flexible beam and the measurement system are certain. Therefore, the grasping force measurement method is feasible.

3. PROTOTYPE DEVELOPMENT AND SYSTEM IDENTIFICATION
3.1 Prototype development and experimental setup

Figure 6 shows the prototype of the wire clamp actuated by a SPCA (type: XP 5×5/18, output displacement: 0–18µm, applied voltage: 0–150V, maximum driving force: 1400N). The wire clamp was fabricated through wire electro-discharge machining (wire EDM) technique to guarantee the geometrical accuracy of the crucial sections, and it was made from the material of AL7075-T651, which has the property of high elasticity, yield strength and light mass. The overall dimension of the wire clamp is 45 mm×28 mm×5 mm, and the initial gap between the grasping jaws is 500 µm.

A laser displacement sensor (LK-H050 from Keyence, Inc) was employed to measure the position of the grasping jaw, which provides a 50 nm resolution within a 20 mm measuring range. A strain gauge (BE120-1AA from Sichuanger, Inc) was glued on the base end of the flexible beam to form a quarter bridge for the grasping force measurement. The strain gauge has a nominal length and width of 4.3 mm and 3.5 mm, respectively and
the gauge factor is 2.22. A dynamic strain gauge (SDY2105) was adopted to measure the
dynamic strain of the beam with the aid of the strain gauge and Wheatstone bridge. A
voltage amplifier (E505.00 from PI, Inc) was used to amplify the input voltage by an
adjustable gain of 10 for the SPCA actuation. The controller system of the prototype was
realized by the dSPACE DS1103 controller, which picks up the outputs from the grasping
force sensor system and the tip displacement sensor system to determine the state of the
wire clamp. According to the determined state of the wire clamp, the controller calculates
the control algorithm and generates the command voltage, which was applied to the
voltage amplifier to realize the corresponding operation. All the devices were placed on a
vibration-isolated Newport RS-4000 table and the experimental setup is displayed in
Fig.7.
3.2 System identification

Experimental system identification based on the frequency response was adopted to capture the dynamic model for the design of a controller for the wire clamp. Swept sine
waves with the amplitude of 0.6 V and frequency range of 0.1–1200 Hz were produced by a dSPACE DS1103 controller to actuate the SPCA through the voltage amplifier in order to obtain the experimental data to identify the two empirical models for position/force control. During the identification of position model, the wire clamp was operated freely, while a 25.4-µm gold wire was selected as a grasped object to identify force model. The position response was measured by the laser displacement sensor, and the force response was measured by the strain gauge. The output signals of position and force responses were acquired within 10kHz, and then the Matlab System Identification Toolbox was used to process the data, and the results are summarized in Figs 8 and 9. The transfer functions of position and force are achieved from the input-output sequences, and they are given as

\[
G_p(s) = \frac{-7540s^3 + 4.261 \times 10^7 s^2 - 3.097 \times 10^{11} s + 7.422 \times 10^{14}}{s^4 + 2976s^3 + 3.213 \times 10^7 s^2 + 7.421 \times 10^{10} s + 1.496 \times 10^{14}} 
\]

\[
G_f(s) = \frac{1.726 \times 10^6}{s^2 + 217.3s + 4.193 \times 10^7}
\]

4. POSITION/FORCE SWITCHING CONTROLLER DESIGN

4.1 Strategy of position/force switching controller

Since the distance between the two jaws is larger than the diameter of the wire, the grasping task during the working process of wire clamp can be classified into three phases, namely the closing phase, contact phase and opening phase. The closing phase occurs prior to the contact of the jaws and wire, the contact phase begins from the touch to the separation of the jaws and wire, and the opening phase is the subsequent time of the jaws motion towards both sides. Precision position control, force control and position
control are employed in the closing phase, contact phase and opening phase, correspondingly, which is shown in Fig. 10. In this research, a strategy of position/force switching controller was employed to regulate the position and force alternately. The position and force controller design can be seen in sections 4.2 and 4.3, respectively.

![Strategy of position/force switching control](image)

**Algorithm 1**  

```
Algorithm 1  position/force switching control( d_r, F_r, F_0, t_0)

1: Initialize  ( d_r, F_r, F_0, t_0)

2:  if F < f_0 then

3:      (u_{s1})  ← position control (d_r): u=f_p(d_r)

4: else if t < t_0 then

5:      (u_{s2}, d_s) ← force control (f_r, u_{s1}): u=f_f(F_r)+ u_{s1}

6: else

7:      position control (d_s, u_{s2}): u=f_p(d_s)+ u_{s2}

8:  end if
```
Since the same control input voltage applied on the SPCA was adopted in the three phases, the switching between each of the two phases may cause instability or undesired responses of the position and force outputs. In order to guarantee a stable and smooth transition between the two consecutive phases, the final voltage in previous phase should be the base value for the next phase. In this way, a smooth transition between the two phases can be accomplished [28].

The position/force switching control is shown in Algorithm 1, where $F_0$ is the threshold force, and $t_0$ is the time to release the wire. During the closing phase, the position control was employed to control the displacement of the grasping jaw following a desired displacement $d_r$ until the grasping force $F$ exceeds the threshold force. The final control voltage $u_{s1}$ can be obtained by the algorithm of position control $f_p(d_r)$. Once the jaws touch the wire and the force sensor indicates the grasping force exceeding the threshold force, the control system switches to the force control to regulate the grasping force following the desired force $F_r$ and the control voltage can be obtained through adding the final voltage $u_{s1}$ in the closing phase to the voltage calculated by the algorithm of force control $f_F(F_r)$. When it is time to release the wire ($t > t_0$), the control system will switch to the position control again which controls the jaws to return to the initial position. The control voltage can be calculated based on the final displacement $d_s$ and the final voltage $u_{s2}$ in the contact phase which can be calculated by the algorithm of force control $f_F(F_r)$.

4.2 Position controller

The PID feedback loop has a simple structure, and the parameters of the PID controller are relatively easy to tune. Thus the PID controller was employed to control the
displacement of the grasping jaw $d$ to follow a desired displacement trajectory $d_r$. The transfer function of a traditional PID control can be expressed as

$$G_{PID}(s) = K_p (1 + \frac{1}{T_i s} + T_D s)$$  \hspace{1cm} (12)$$

where $K_p$ is the proportional gain, $T_i$ is the integral time constant, and $T_D$ is the differential time constant.

Equation (12) can be written as

$$G_{PID}(s) = K_p + \frac{K_i}{s} + K_D s$$  \hspace{1cm} (13)$$

where $K_i = \frac{K_p}{T_i}$ is the integral gain and $K_D = K_p T_D$ is the differential gain.

Defining $e_d(t) = d_r(t) - d(t)$ as the position error, the PID position controller equation is expressed as following:

$$u_d(t) = K_p e_d(t) + K_i \int_0^t e_d(t) dt + K_D \frac{de_d(t)}{dt}$$  \hspace{1cm} (14)$$

Generally, the PID controller can be adjusted with Ziegler-Nichols (Z-N) method by several simulation studies, and then the parameters are tuned finely through experimental investigations.

**4.3 Force controller**

Considering there may be some dynamic force vibrations during the contact process, sliding mode control with strong robustness to uncertainties and disturbances has been adopted for the force control. The sliding model controller (SMC) design focuses on the following domains: the selection of the sliding surface and the design of the sliding control law.
Traditional SMC featured with PD-type sliding surface usually produces a slow response speed while the SMC with PID-type sliding surface offers a faster transient response and less steady-state error. Hence, SMC with PID-type sliding surface was designed for the force control. According to the identified transfer function of grasping force, the force model of the wire clamp during the contact phase can be written as

\[
\frac{d^2 f(t)}{dt^2} + a_1 \frac{df(t)}{dt} + a_2 f(t) = b_0 u(t) \tag{15}
\]

where \(a_1, a_2\) and \(b_0\) are constants, which can be confirmed by Eq. (11).

Assuming there is perturbation of the force system, and the perturbation \(p\) can be written as

\[
p(t) = \frac{d^2 f(t)}{dt^2} + a_1 \frac{df(t)}{dt} + a_2 f(t) - b_0 u(t) \tag{16}
\]

The perturbation can be estimated by

\[
p^*(t) = p(t-T) = \frac{d^2 f(t-T)}{dt^2} + a_1 \frac{df(t-T)}{dt} + a_2 f(t-T) - b_0 u(t-T) \tag{17}
\]

Then the force model can be expressed as

\[
\frac{d^2 f(t)}{dt^2} + a_1 \frac{df(t)}{dt} + a_2 f(t) = b_0 u(t) + p^*(t) + p_e(t) \tag{18}
\]

where \(p_e(t) = p(t) - p^*(t)\) represents the error between the estimated perturbation and the real perturbation of the system.

In the contact phase, the force controller was designed to control the grasping force \(f\) between the grasping jaws and the wire to follow a desired force trajectory \(f_r\), and the force error can be defined as

\[
e_f(t) = f_r(t) - f(t) \tag{19}
\]
Then a sliding function of PID-type can be represented as

\[ s(t) = c_p e_f(t) + c_1 \int_0^t e_f(\tau) d\tau + \frac{de_f(t)}{dt} \]  \hspace{1cm} (20)

where \( c_p \) and \( c_1 \) are positive parameters and the parameters should be chosen strictly Hurwitz.

Designing the sliding control law as

\[ u_{SMC} = \frac{1}{b_0} [(a_1 - c_p) \frac{df}{dt} + (a_2 - c_1) f + \frac{d^2 f_r}{dt^2} + c_p \frac{df_r}{dt} + c_1 f_r - p^* - \text{slaw}] \]  \hspace{1cm} (21)

The exponential reach law is adopted as the reach law, and it can be expressed as

\[ \text{slaw} = -\eta \text{sgn}(s) - ks \]  \hspace{1cm} (22)

where \( \eta > 0 \) and \( k > 0 \) are constant parameters, and \( \text{sgn}(s) \) is the sign function.

Define a Lyapunov function as

\[ V = \frac{s^2}{2} \]  \hspace{1cm} (23)

The first derivative of Eq. (23) can be obtained as

\[ \frac{dV}{dt} = s \frac{ds}{dt} \]  \hspace{1cm} (24)

Differentiating Eq. (20) with respect to time, yields

\[ \frac{ds}{dt} = c_p \left( \frac{df_r}{dt} - \frac{df}{dt} \right) + c_1 (f_r - f) + \frac{d^2 f_r}{dt^2} + a_1 \frac{df_r}{dt} + a_2 f - b_0 u - p^* - p_e \]  \hspace{1cm} (25)

Then substitute Eqs. (21) and (25) into Eq. (24), and the following equation can be gotten:

\[ \frac{dV}{dt} = c_p \left( \frac{df_r}{dt} - \frac{df}{dt} \right)s + c_1 (f_r - f)s + \frac{d^2 f_r}{dt^2}s + a_1 \frac{df_r}{dt}s + a_2 fs - b_0 us - p^*s - p_e s \]

\[ = (-\eta \text{sgn}(s) - ks - p_e)s \]

\[ = -\eta |s| - ks^2 - p_e s \]  \hspace{1cm} (26)
If the gain $\eta$ is designed to meet the condition

$$\eta > |p| + \varepsilon \quad (27)$$

where $\varepsilon > 0$ is an arbitrary constant, then the following relationship can be obtained:

$$\frac{dV}{dt} = -\eta |s| - ks^2 - p_s s < -ks^2 - \varepsilon |s| < 0 \quad (28)$$

Equation (28) implies that the system is stable and the trajectory reaches the sliding surface in finite time and remains on the sliding surface $s=0$. Besides, it also ensures that the states will be confined to the surface $s=0$ for all future time since leaving the surface requires $\dot{s}$ to be positive, which is impossible as implied by the inequality.

Due to changes in the function $\text{sgn}(s)$, when $s$ is next to zero, the chattering problem can appear. To avoid this undesirable effect, the sign function is substituted by a saturation function with the following form:

$$\text{sat}(s) = \begin{cases} 1, & s > \Delta \\ \frac{s}{\Delta}, & |s| \leq \Delta \\ -1, & s < -\Delta \end{cases} \quad (29)$$

where the positive constant $\Delta$ represents the boundary layer thickness, which ensures that $s$ is always bounded by $\Delta$.

The sliding control law can be written as

$$u_{\text{SMC}} = \frac{1}{b_0} \left[ (a_{1} - c) \frac{df}{dt} + (a_2 - c) f + \frac{d^2 f}{dt^2} + c_p \frac{df_r}{dt} + c_i f_r - p^* + \eta \text{sat}(s) + ks \right] \quad (30)$$

5. EXPERIMENTS
Several control experiments were carried out to examine the performance of the position/force switching controller. During the experiments, gold wires with a diameter of 25.4 µm were employed to verify the effectiveness of the switching control strategy.

5.1 Position control

Step response was investigated and the desired displacement trajectory was defined as a step signal with a final value as 20 µm. The parameters of the position PID controller are chosen as: $K_P=0.016$, $K_I=45$, $K_D=0.002$. The step response of the position control is shown in Fig. 11. From the result it can be seen that the setting time is 12 ms, the overshoot is 2.5%, and the steady-state error is ±0.2 µm.

![Fig.11 Displacement step response of the wire clamp.](image)

5.2 Force control
To compare the performance of PID force controller and sliding mode force controller, step response was investigated and the desired force trajectory was defined as a step signal with a final value as 50 mN. The parameters of the force PID controller are chosen as: \( K_P = 0.5 \), \( K_I = 2100 \), \( K_D = 0.0015 \) and the parameters of the sliding mode controller are chosen as \( c_I = 720 \), \( c_P = 129600 \), \( \eta = 20 \), \( k = 7500 \). These parameters are adjusted by trial and error through experimental studies. Besides the threshold force \( F_0 \) is 5 mN. The results of PID and sliding mode controllers are shown in Fig. 12. From the results it can be seen that the setting time of PID controller is 30 ms, the overshoot is 1.3%, and the steady-state error is ±0.4 mN. The setting time of sliding mode controller is 20 ms, the overshoot is 1.8%, and the steady-state error is ±0.4 mN. It can be seen that the setting time of sliding mode controller is less than that of PID controller.

Fig. 12 Results of PID and sliding mode controllers.

### 5.3 Position/force switching controller
The jaw velocity in the closing phase is important in the transition between the closing phase and contact phase, which can cause instability and undesired responses of the force output. A series of experiments about different velocities have been conducted. The PID controller was employed to control the displacement of the grasping jaw, while the sliding mode controller was utilized to control the grasping force. The parameters of controllers are the same with those in sections 5.1 and 5.2. In the closing phase the jaw was controlled by PID position controller to close at different velocities of 100 µm/s, 200 µm/s, 300 µm/s, 400 µm/s, and 500 µm/s until the grasping force arrives at the threshold force $F_0$. Then the grasping force was controlled by the sliding mode force controller. The results of force control with different switching velocities are shown in Fig. 13. It can be seen that the overshoots increase with the increase of switching velocities from 100 µm/s to 400 µm/s. The chattering phenomenon which causes instability appears in the force response at velocity of 500 µm/s. Thus the switching velocity can be in 0-500 µm/s to alleviate the chattering effect. The chattering phenomenon may be caused by the jaw inertia or the controller and the related research has been done in different applications [29]. In order to avoid the chattering phenomenon fast control is required, which will be studied in future work.
In order to achieve a complete and efficient grasp-hold-release operation, the position and force trajectories were planned and shown in Fig. 14. During the closing phase the homothetic trapezoidal velocity planning was employed to control the jaw displacement, leading to the contact of the jaws and wire with a constant velocity. In the contact phase a step force signal was utilized as the reference signal of the grasping force. In order to make the jaws return to their initial positions, the trapezoidal velocity planning was used based on the final position in the contact phase.
Figure 15 shows the results of position/force switching control in the grasp-hold-release operation. The parameters of position and force controller are the same with those in sections 5.1 and 5.2. A switching velocity of 200 µm/s and switching time $t_s$ of 75 ms were chosen in the closing phase, and the desired force trajectory was defined as a step signal with a final value as 50 mN in the contact phase. Besides the threshold force of 10 mN was chosen to realize the switching from the closing phase to contact phase. The results show that the steady-state error of grasping force is ±0.4 mN, the setting time is 20 ms and the overall time of the operation is within 200 ms. The results are compared with those reported in some similar works which are summarized in Table 2. It is found that the developed wire clamp outperforms the others in terms of a larger amplification ratio, high first vibration frequency and faster overall operation time.
Results of position/force switching control in the grasp-hold-release operation: (a) displacement response, and (b) force response.
Table 2 Comparison with other similar works.

<table>
<thead>
<tr>
<th>Actuation</th>
<th>Amplification ratio</th>
<th>First vibration frequency (Hz)</th>
<th>Overall operation time (s)</th>
<th>Position/force control</th>
<th>Reference</th>
</tr>
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<tr>
<td>Thermo-Piezoelectric</td>
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<td>667</td>
<td>120</td>
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<td>[30]</td>
</tr>
<tr>
<td>Voice coil motor</td>
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<td>N/A</td>
<td>N/A</td>
<td>No</td>
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<tr>
<td>Piezoelectric</td>
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<td>500</td>
<td>N/A</td>
<td>Yes</td>
<td>[32]</td>
</tr>
<tr>
<td>PZT</td>
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<td>244</td>
<td>&gt;5</td>
<td>Yes</td>
<td>[28]</td>
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<tr>
<td>PZT</td>
<td>16</td>
<td>359.56</td>
<td>&gt;12</td>
<td>No</td>
<td>[33]</td>
</tr>
<tr>
<td>PZT</td>
<td>19.4</td>
<td>810</td>
<td>0.2</td>
<td>Yes</td>
<td>This works</td>
</tr>
</tbody>
</table>

6. CONCLUSION

In this paper, the mechanism, characteristics and control of a novel piezoelectric actuated wire clamp have been reported. The grasping forces have been investigated based on FEA, and the grasping force measurement has been described. Based on frequency response approach, the transfer functions of position and force were achieved. A position/force switching controller has been designed and employed to regulate the position and force alternately, which is composed of a PID controller for the position control and a slide model controller (SMC) for the force control. Experimental tests have been carried out to investigate the performance of the wire clamp and the position/force switching controller during the grasp-hold-release operation. The position step response shows that the setting time is 12 ms, the overshoot is 2.5%, and the steady-state error is ±0.2 μm. For the force step response, the results show that the setting time of PID
controller is 30 ms, the overshoot is 1.3%, and the steady-state error is ±0.4 mN. The setting time of SMC is 20 ms, the overshoot is 1.8%, and the steady-state error is ±0.4 mN. Obviously, the sliding mode force controller outperforms the PID force controller in terms of the setting time. A series of experiments about different velocities have been conducted, the result shows that the chattering phenomenon which may cause instability appears in the force response at velocity of 500 µm/s, and the switching velocity can be in 0-500 µm/s to avoid the chattering effect. The control method to avoid the chattering effect will be studied in future works. Finally position/force switching control in the grasp-hold-release operation has been investigated based on position and force trajectory planning. The constant force regulation has been realized within 200 ms with the steady-state force error ±0.4 mN. The experiment results show that the wire clamp exhibits good performance and demonstrate that the new wire clamp and the control law are well suited for fast and high precision grasping and releasing operations.

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