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Resource Allocation in UAV-Enabled Wireless Powered MEC Networks with Hybrid Passive and Active Communications

Qian Li, Liqin Shi, Zhongjun Zhang, and Gan Zheng, Fellow, IEEE

Abstract—This paper proposes a novel unmanned aerial vehicle (UAV) enabled wireless powered mobile edge computing (WP-MEC) network, where several Internet of Things (IoT) nodes use the energy harvested from the UAV's radio frequency signals to support the local computation and the hybrid activepassive communications based task offloading. Two weighted sum computation bits maximization problems are formulated under the partial and binary offloading, respectively, by jointly optimizing the local computing frequencies and time, the IoT nodes' reflection coefficients, the IoT nodes' transmit powers, the UAV's trajectory, etc., subject to the quality-of-service and energy-causality constraints per IoT node, the speed constraint of the UAV, etc. Since the formulated problems are highly nonconvex, two iterative algorithms are proposed to solve the formulated problems under two modes. Simulation results demonstrate that the proposed iterative algorithms have a fast convergence rate, and the proposed schemes achieve higher weighted sum computation bits than several baseline schemes.

Index Terms—UAV-enabled WP-MEC, hybrid active-passive communications, computation bits.

I. INTRODUCTION

T has been witnessed that the Internet of Things (IoT) plays a significant role in future applications by deploying massive IoT nodes to provide intelligent services. However, owing to the production cost limitation, IoT nodes are usually energyand computation-constrained, bringing many challenges in realizing IoT nodes based intelligent services. One of major challenges is how to timely process the computation-intensive tasks at IoT nodes while reducing or even avoiding energy consumption of their batteries [1]. Wireless powered mobile edge computing (WP-MEC), which seamlessly integrates wireless power transfer (WPT) [2] and mobile edge computing (MEC) [3], [4] as a whole, has been proposed as an efficient solution to address this challenge. The key idea of WP-MEC is to let IoT nodes harvest energy from radio frequency (RF) signals of a dedicated energy source, and use their harvested energy to support the data offloading and task computation under the binary or partial computation offloading [1], [5]. Accordingly, the energy harvesting (EH), data computation and offloading

are coupled with each other, which calls for new optimization frameworks.

In [5], the authors proposed a WP-MEC network with a single IoT node, and focused on maximizing the successful computation probability under a binary offloading mode, subject to the energy-causality and delay constraints. Considering a WP-MEC network with multiple IoT nodes, the authors of [6] maximized the weighted sum-computation rate maximization by optimizing the binary computation offloading decision, the EH time and the offloading time per IoT node. In [7], the total energy consumption at all IoT nodes and the power beacon (PB) was minimized under a partial offloading mode, while satisfying the minimal required computation bits, delay and energy-causality constraints per IoT node. In [8]-[11], the authors introduced the computation energy efficiency (CEE) that is calculated as the ratio of the computed task bits to the corresponding consumed energy, and designed various optimization frameworks for WP-MEC networks.

In the above works [5]–[11], the task data are offloaded to the MEC server via active communications (AC) that require power-consuming components, e.g., oscillators, analogto-digital/digital-to-analog converters. Owing to the use of high power-consuming components and the low efficiency of EH, more time will be allocated to the EH at each IoT node, leaving less time for data offloading and limiting the performance of data offloading in WP-MEC. Different from AC, the backscatter communication (BackCom), one of low power-consuming passive communications, enjoys a lower power consumption and a lower offloading rate than AC by allowing an IoT node to modulate and reflect the incident signals for task offloading [12]. In order to achieve efficient task offloading, BackCom has been integrated into WP-MEC to form WP-MEC with hybrid active-passive communications [13], where the advantages of hybrid active-passive communications can be fully exploited. Recent works [14]-[19] have validated the advantages of WP-MEC via hybrid active-passive communications over the WP-MEC via AC in terms of the computation bits, CEE, and computation delay. However, it was assumed in the existing works [14]-[19] that the location of the dedicated energy source is fixed. In such a case, the harvested energy of each IoT node is constrained by the distance from the dedicated energy source to the IoT node, and this calls for a mobile energy source to replace the fixed one, in order to make full use of the mobility of the energy source for increasing the harvested energy per IoT node. Recently, the unmanned aerial vehicle (UAV) has been considered as

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a mobile energy/signal source in multiple wireless communication networks, i.e., relaying communication systems [20], intelligent reflecting surface (IRS) assisted wireless networks [21], WP-MEC networks [22]–[26], etc. For example, in [20], the UAV was adopted as a relay to help transmit information and the minimum average secrecy rate among all users was maximized for UAV-relaying systems with local caching. In IRS-assisted UAV networks, the UAV was served as a mobile signal source and the secure communication between the UAV and the legitimate user was guaranteed [21]. In UAVenabled WP-MEC, the UAV is deployed as a mobile energy source for charging IoT nodes via line-of-sight (LoS) links and various resource allocation schemes have been proposed to achieve different optimization goals [22]-[26]. We note that the previous works [22]-[26] on UAV-enabled WP-MEC only considered the AC for data offloading, while the data offloading via hybrid active-passive communications has not been exploited. This motivates us to configure a new UAVenabled WP-MEC network to make full use of the advantages of hybrid active-passive communication based offloading.

In this work, we employ the hybrid active-passive communication in UAV-enabled WP-MEC for realizing more efficient data offloading, and propose to maximize the weighted sum computation bits (WSCB) of all IoT nodes. To the authors' best knowledge, this is the first work that studies the resource allocation problems for the UAV-enabled WP-MEC network with hybrid active-passive communications. Our main contributions are listed below.

- We propose a novel UAV-enabled WP-MEC network, in which a UAV is dispatched as a mobile energy source that provides energy to all IoT nodes and all IoT nodes take turns to perform hybrid active-passive communications based data offloading by fully exploiting the incident signals transmitted by the UAV.
- Considering the partial and binary offloading modes, we formulate two WSCB maximization problems, by optimizing multiple optimization variables, i.e., the IoT nodes' local computation frequencies and time, reflection coefficients and the transmit power of the IoT nodes, the UAV's trajectory, etc. In order to solve them, we first obtain the closed-form expression of the optimal computing time for the IoT node who performs local computation under two modes based on the proof by contradiction. Then for the partial offloading, we propose a two-stage alternating iterative algorithm to solve the formulated optimization problem and derive the closed-form expressions for the optimal local computing frequencies and time, the optimal power reflection coefficients and the optimal transmit powers at IoT nodes under any given trajectories. For the binary offloading, in order to solve the formulated mixed integer optimization problem, we propose a three-stage alternating iterative algorithm to obtain the IoT nodes' local computation frequencies and time, the reflection coefficients, the UAV's trajectory, the mode selection per IoT node for choosing either task offloading or local computation, etc.
- Simulation results validate the fast convergence of the



Fig. 1. The UAV-enabled WP-MEC network with hybrid passive and active communications and its frame structure.

proposed iterative algorithms and demonstrate that the superiorities of the proposed schemes in terms of WSCB.

II. SYSTEM MODEL

A UAV-enabled WP-MEC network with hybrid passive and active communications is considered, as shown in Fig. 1, where a UAV provides energy signals to K single-antenna IoT nodes and a MEC server is deployed to provide MEC services for these IoT nodes. Specifically, the IoT nodes should harvest energy from the RF signals of the UAV and then offload their task bits to the MEC server for computation by means of the combination of BackCom and AC, namely hybrid passive and active communications, and/or perform local computing by using its harvested energy. Suppose that each IoT node is energy-constrained and each IoT node only uses its harvested energy to perform task offloading and/or local computation. In order to realize tasks offloading and computing, all IoT nodes should be equipped with four separate circuits which are the energy harvester, the computing circuit, the backscatter circuit and the AC circuit, respectively. Accordingly, each IoT node can offload tasks when performing local computation.

Assume that the location of the k-th $(k \in \mathcal{K} = \{1, 2, \ldots, K\})$ IoT node is fixed on the ground, denoted by $\mathbf{q}_k = [x_k, y_k]$, where x_k and y_k are the k-th IoT node's horizontal plane coordinates. Denote the MEC server's location as $\mathbf{q}_m = [x_m, y_m]$ with the horizontal plane coordinates x_m and y_m . Following [22]–[26], the UAV is assumed to fly at a given altitude level, denoted by H (H > 0), and its location in the 2D horizontal plane is given by $\mathbf{q}_u(t) = [x_u(t), y_u(t)]$ with the horizontal plane coordinates $x_u(t)$ and $y_u(t)$ at the time instance t. Assume that both K IoT nodes' locations and the MEC server's location can be obtained at the UAV in order to design the UAV's trajectory [22]–[26].

Let T express the duration of the transmission block, which consists of the BackCom phase and the active transmission (AT) phase, respectively. Note that the computing and downloading time at the MEC server can be ignored here due to the fact that the MEC server's computation capacity is sufficiently large, leading to negligible computing and downloading time. Denote β ($0 \le \beta \le 1$) as the time allocation factor. In the BackCom phase with the duration of βT , the UAV keeps flying and broadcasting energy signals while multiple IoT nodes take turns to perform BackCom. For ease of exposition, the whole BackCom phase is discretized into N equal time slots, and then the duration of the n-th ($n \in \mathcal{N} = \{1, 2, \ldots, N\}$) time slot is given by $\frac{\beta T}{N}$. Following [22]–[26], we assume that the UAV is static in each time slot. Let $\mathbf{q}_{u}[n] = [x_{u}[n], y_{u}[n]]$ and $g_{n,k}$ denote the location of the UAV and the channel gain from the UAV to the k-th IoT node in the n-th time slot, respectively. Then $g_{n,k}$ is given by

$$g_{n,k} = \beta_0 d_{k,n}^{-2} = \frac{\beta_0}{H^2 + \|\mathbf{q}_u[n] - \mathbf{q}_k\|^2},$$
 (1)

where β_0 is the channel gain at a reference distance with $d_0 = 1 \text{ m}$, $d_{k,n}$ denotes the distance from the k-th IoT node to the UAV in the *n*-th time slot, and $\|\cdot\|$ expresses the Euclidean norm of a vector. In the AT phase with the duration of $(1 - \beta)T$, we consider that multiple IoT nodes take turns to transmit their task bits to avoid the co-channel interference among IoT nodes. Considering that each task can and cannot be partitioned into two parts, two offloading modes, namely the partial and binary offloading modes. The details for the considered network under partial and binary offloading modes are presented below.

A. Partial Offloading Mode

For the partial offloading, each task is partitioned into two parts, where one part will be computed locally and the other will be offloaded to the MEC server for computation. In the following, we will present how the considered network works. Under this mode, the *n*-th time slot in the BackCom phase can be further divided into K sub-slots, denoted by $t_{n,k}^{\rm b}$. In the kth sub-slot of the *n*-th time slot, the k-th IoT node modulates its part of computation tasks on a part of its received signals and backscatters the modulated signals for task offloading. The rest part of its received signals is used for EH. Note that the IoT nodes who do not perform BackCom will harvest energy during this period. Let $\alpha_{n,k}$ with $0 \le \alpha_{n,k} \le 1$ denote the power reflection coefficient at the k-th IoT node in the *n*-th time slot [27]. Then the computation bits of the k-th IoT node in this time slot are computed by

$$R_{n,k}^{\rm b} = t_{n,k}^{\rm b} B \log_2\left(1 + \frac{\xi \alpha_{n,k} P_{\rm u} g_{n,k} h_k}{B\sigma^2}\right),\tag{2}$$

where B represents the bandwidth of the system, ξ denotes the performance gap¹ reflecting the real modulation, P_u is the UAV's transmit power during the whole transmission block, h_k (SIC). This is because both the energy signals of the UAV and the corresponding channel information are known by the MEC server [28]. Then, at the end of the BackCom phase, the total computation bits of the k-th IoT node are given by

$$R_{k}^{b} = \sum_{n=1}^{N} R_{n,k}^{b} = \sum_{n=1}^{N} t_{n,k}^{b} B \log_{2} \left(1 + \frac{\xi \alpha_{n,k} P_{u} g_{n,k} h_{k}}{B \sigma^{2}} \right).$$
(3)

Correspondingly, the k-th IoT node's total harvested energy is given by

$$E_{\text{tot}}^{k} = \sum_{n=1}^{N} \left[\left(\frac{\beta T}{N} - t_{n,k}^{\text{b}} \right) P_{\text{u}} g_{n,k} \eta + t_{n,k}^{\text{b}} P_{\text{u}} g_{n,k} \eta \left(1 - \alpha_{n,k} \right) \right]$$
$$= \sum_{n=1}^{N} \left(\frac{\beta T}{N} P_{\text{u}} g_{n,k} \eta - t_{n,k}^{\text{b}} \alpha_{n,k} P_{\text{u}} g_{n,k} \eta \right), \tag{4}$$

where η with $0 \le \eta \le 1$ is the energy conversion efficiency. For analytical tractability, we consider a linear EH model, where η is fixed as a constant. Note that this work can be extended to the scenarios with a non-linear EH model by means of the approach used in [29] or [30].

Likewise, the AT phase is divided into K sub-slots for K IoT nodes' task offloading. Let p_k and t_k^a express the k-th IoT node's transmit power and time, respectively. Then the computation bits offloaded by the k-th IoT node in this phase are given by

$$R_k^{\rm a} = t_k^{\rm a} B \log_2 \left(1 + \frac{p_k h_k}{B\sigma^2} \right).$$
⁽⁵⁾

Based on (3) and (5), we can compute the total achievable computation bits at the *k*-th IoT node as $R_k^{\text{off}} = R_k^{\text{b}} + R_k^{\text{a}}$.

For local computing, let f_k and τ_k $(0 \le \tau_k \le T)$ denote local computation frequency and time at the k-th IoT node. Then the k-th IoT node's local computation bits are given by

$$R_k^{\text{Loc}} = \frac{f_k \tau_k}{C_{\text{cpu},k}},\tag{6}$$

where $C_{\text{cpu},k}$ reflects the k-th IoT node's required number of CPU cycles for computing one bit. Let ε_k be the effective capacitance coefficient of the processor's chip at the k-th IoT node. Then the consumed energy for the k-th IoT node's local computation is calculated by

$$E_k^{\text{Loc}} = \varepsilon_k (f_k)^3 \tau_k. \tag{7}$$

B. Binary Offloading Mode

Under this mode, each IoT node either performs complete task offloading or performs fully local computing. Specifically, K IoT nodes can be divided into two sets, which are the set of IoT nodes who perform fully local computing and the set of IoT nodes who perform complete task offloading, respectively. Let \mathcal{K}_L and \mathcal{K}_O denote the above two sets, where $\mathcal{K} = \mathcal{K}_L \cup$ \mathcal{K}_O and $\mathcal{K}_L \cap \mathcal{K}_O = \emptyset$, where \emptyset is the empty set. For the

¹Since the backscatter circuit is composed of passive components and is better suited to a simple modulation scheme instead of high-order modulation schemes in practice, there will be a performance gap between the channel capacity of BackCom and the Shannon capacity [18], [28].

IoT node belonging to \mathcal{K}_{L} , namely $i \in \mathcal{K}_{L}$, its total harvested energy is given by

$$E_i^{\mathrm{L,B}} = \sum_{n=1}^{N} P_{\mathrm{u}} g_{n,i} \eta \frac{\beta T}{N}, i \in \mathcal{K}_{\mathrm{L}}.$$
(8)

Accordingly, its computed bits are given by

$$R_i^{\mathrm{L,B}} = \frac{f_i \tau_i}{C_{\mathrm{cpu},i}}, i \in \mathcal{K}_{\mathrm{L}}.$$
(9)

For the IoT node belonging to \mathcal{K}_{O} , namely $l \in \mathcal{K}_{O}$, its total harvested energy can be expressed as

$$E_l^{\mathrm{O,B}} = \sum_{n=1}^N \left(\frac{\beta T}{N} P_{\mathrm{u}} g_{n,l} \eta - t_{n,l}^{\mathrm{b}} \alpha_{n,l} P_{\mathrm{u}} g_{n,l} \eta \right), l \in \mathcal{K}_{\mathrm{O}}.$$
 (10)

Then its corresponding computed bits are given by

$$R_l^{\text{O,B}} = \sum_{n=1}^N t_{n,l}^{\text{b}} B \log_2 \left(1 + \frac{\xi \alpha_{n,l} P_{\text{u}} g_{n,l} h_l}{B \sigma^2} \right) + t_l^{\text{a}} B \log_2 \left(1 + \frac{p_l h_l}{B \sigma^2} \right), l \in \mathcal{K}_{\text{O}}.$$
(11)

In the following two sections, we will study the WSCB maximization under the partial and binary offloading modes, respectively.

III. PARTIAL OFFLOADING BASED WSCB MAXIMIZATION

Considering the partial offloading mode at each IoT node, we first formulate a WSCB maximization problem by optimizing the BackCom time, the AT time allocation, the local computing frequencies and time, the reflection coefficients, and the transmit powers of the IoT nodes, as well as the UAV's trajectory, subject to the constraints of the quality-ofservice (QoS), energy causality, time, speed, the initial and final horizontal location, etc. The formulated problem is highly non-convex. To solve it, we propose a two-stage alternating algorithm to determine its solution.

A. Problem Formulation

The goal is to maximize the WSCB achieved by all IoT nodes for the considered network. Denote $w_k > 0$ as the weight of the k-th IoT node. Then w_k indicates the priority of the k-th IoT node in the WSCB maximization problem and

can be used to customize the service provisioning for different IoT nodes. Accordingly, the optimization problem is given by

$$\begin{split} \mathbf{P}_{1} &: \max_{\mathcal{V}} \quad \sum_{k=1}^{K} w_{k} \left(R_{k}^{\text{off}} + R_{k}^{\text{Loc}} \right) \\ \text{s.t. C1} &: R_{k}^{\text{off}} + R_{k}^{\text{Loc}} \geq L_{\min,k}, \forall k, \\ \text{C2} &: E_{k}^{\text{Loc}} + P_{\text{c},k} \left(\sum_{n=1}^{N} t_{n,k}^{\text{b}} \right) + p_{k} t_{k}^{\text{a}} + p_{\text{c},k} t_{k}^{\text{a}} \\ &\leq E_{\text{tot}}^{k}, \forall k, \\ \text{C3} &: 0 \leq f_{k} \leq f_{k}^{\max}, \forall k, \\ \text{C4} &: 0 < \beta < 1, \sum_{k=1}^{K} t_{n,k}^{\text{b}} \leq \frac{\beta T}{N}, \forall n, \sum_{k=1}^{K} t_{k}^{\text{a}} \leq (1 - \beta) T, \\ \text{C5} &: 0 \leq \tau_{k} \leq T, \forall k, \\ \text{C6} &: 0 \leq \alpha_{n,k} \leq 1, \forall k, \forall n, \\ \text{C7} &: t_{n,k}^{\text{b}} \geq 0, \forall n, \forall k, t_{k}^{\text{a}} \geq 0, p_{k} \geq 0, \forall k, \\ \text{C8} &: \|\mathbf{q}_{u} [n + 1] - \mathbf{q}_{u} [n]\| \leq V_{\max} \frac{\beta T}{N}, \forall n, \\ \text{C9} &: \mathbf{q}_{u} [1] = \mathbf{q}_{\text{I}}, \mathbf{q}_{u} [N + 1] = \mathbf{q}_{\text{F}}, \end{split}$$

where $\mathcal{V} = \{\beta, \{t_{n,k}^{b}\}, \{t_{k}^{a}\}, \{p_{k}\}, \{f_{k}\}, \{\tau_{k}\}, \{\alpha_{n,k}\}, \{\mathbf{q}_{u}\}\}$ is the set of the optimization variables, $L_{\min,k}$ denotes the minimum required computation bits for the k-th IoT node, $P_{c,k}$ and $p_{c,k}$ are the fixed power consumption at the k-th IoT node when performing BackCom and AT, respectively, f_{k}^{\max} expresses the k-th IoT node's maximum allowed computation frequency, V_{\max} is the UAV's maximum speed, \mathbf{q}_{I} and \mathbf{q}_{F} denote the initial and final horizontal locations of the UAV. Note that a constant circuit power consumption rate for BackCom is assumed by following [31]–[33] and then the consumed energy for BackCom at the k-th IoT node in the *n*-th time slot is computed as $P_{c,k}t_{n,k}^{b}$.

In the above optimization problem, C1 is the QoS constraint per IoT node. C2 denotes the energy-causality constraint for each IoT node, where each IoT node's total energy consumption for task offloading and execution can not be larger than its harvested energy. C3 limits the maximum computing frequency at each IoT node during the whole transmission block. C4 is the time allocation constraint for BackCom and AT phases while C5 guarantees the local computing time at each IoT node. C6 constrains the value of the power reflection coefficient at each IoT node. C8 represents the speed constraint while C9 is the constraint of the UAV's initial and final horizontal location.

By observing $\mathbf{P_1}$, we find that $\mathbf{P_1}$ is non-convex due to the existence of several coupled relationships among different variables, i.e., $t_{n,k}^{\mathrm{b}}$ and $\alpha_{n,k}$, etc, leading to non-convex objective function and constraints. Besides, the optimization of the trajectory of the UAV greatly improves the complexity of $\mathbf{P_1}$, bringing a great challenge to solve it.

B. Solution

As for P_1 , there is no standard methods to jointly optimize the UAV's trajectory and communication/computation resources. In order to solve P_1 , the block coordinate decent (BCD) technique is used to decouple P_1 into two subproblems first, and then a two-stage alternating iterative algorithm is proposed to obtain the solution to P_1 . Note that the BCD technique can be used to obtain a locally optimal solution to a non-convex problem that cannot be optimally solved by using the existing methods.

Specifically, with a fixed trajectory, the following subproblem can be obtained,

$$\mathbf{P_{1a}}: \max_{\mathcal{V}_1} \sum_{k=1}^{K} w_k \left(R_k^{\text{off}} + R_k^{\text{Loc}} \right)$$

s.t. C1 - C7,

where $\mathcal{V}_1 = \{\beta, \{t_{n,k}^{\mathrm{b}}\}, \{t_k^{\mathrm{a}}\}, \{p_k\}, \{f_k\}, \{\tau_k\}, \{\alpha_{n,k}\}\}.$ In order to simplify $\mathbf{P}_{1\mathrm{a}}$, Proposition 1 is presented to

decide the k-th IoT node's optimal computation time, denoted by τ_k^* .

Proposition 1: For achieving the maximum WSCB of all the IoT nodes in the considered network under the partial offloading mode, each IoT node should perform local computation throughout the transmission block, i.e., $\tau_k^* = T$.

Proof. Please see Appendix A.

According to Proposition 1, P_{1a} can be reformulated as

$$\begin{aligned} \mathbf{P}_{2\mathbf{a}} &: \max_{\mathcal{V}_2} \quad \sum_{k=1}^{K} w_k \left(R_k^{\text{off}} + \frac{f_k T}{C_{\text{cpu},k}} \right) \\ \text{s.t. } & \text{C1} - 1 : R_k^{\text{off}} + \frac{f_k T}{C_{\text{cpu},k}} \ge L_{\min,k}, \forall k, \\ & \text{C2} - 1 : \varepsilon_k (f_k)^3 T + P_{\mathbf{c},k} \left(\sum_{n=1}^N t_{n,k}^{\mathbf{b}} \right) + p_k t_k^{\mathbf{a}} + p_{\mathbf{c},k} t_k^{\mathbf{a}} \\ & \le E_{\text{tot}}^k, \forall k, \\ & \text{C3}, \text{C4}, \text{C6}, \text{C7}, \end{aligned}$$

where $\mathcal{V}_2 = \{\beta, \{t_{n,k}^{\mathrm{b}}\}, \{t_k^{\mathrm{a}}\}, \{p_k\}, \{f_k\}, \{\alpha_{n,k}\}\}.$ It can be seen that $\mathbf{P}_{2\mathrm{a}}$ is still a non-convex problem

and challenge to solve. This is because the coupled relationship between p_k and $t_k^{\rm a}$ or between $\alpha_{n,k}$ and $t_{n,k}^{\rm b}$ leads to the non-convexities of the objective function, C1 - 1 and C2 - 1. To address this problem, several auxiliary variables are introduced into \mathbf{P}_{2a} . Specifically, let $P_k = p_k t_k^a$ and $x_{n,k} = \alpha_{n,k} t_{n,k}^{\mathrm{b}}, \forall n, \forall k \text{ replace } p_k \text{ and } \alpha_{n,k}, \text{ respectively.}$ Then \mathbf{P}_{2a} can be transformed into

$$\begin{split} \mathbf{P}_{3\mathbf{a}} : \max_{\mathcal{V}_{3}} & \sum_{k=1}^{K} w_{k} \bigg(\sum_{n=1}^{N} t_{n,k}^{\mathbf{b}} B \log_{2} \left(1 + \frac{\xi x_{n,k} P_{\mathbf{u}} g_{n,k} h_{k}}{t_{n,k}^{\mathbf{b}} B \sigma^{2}} \right) \\ & + t_{k}^{\mathbf{a}} B \log_{2} \left(1 + \frac{P_{k} h_{k}}{t_{k}^{\mathbf{b}} B \sigma^{2}} \right) + \frac{f_{k} T}{C_{\mathrm{cpu},k}} \bigg) \\ \mathrm{s.t.} & \operatorname{C1} - 2 : \sum_{n=1}^{N} t_{n,k}^{\mathbf{b}} B \log_{2} \left(1 + \frac{\xi x_{n,k} P_{\mathbf{u}} g_{n,k} h_{k}}{t_{n,k}^{\mathbf{b}} B \sigma^{2}} \right) \\ & + t_{k}^{\mathbf{a}} B \log_{2} \left(1 + \frac{P_{k} h_{k}}{t_{k}^{\mathbf{a}} B \sigma^{2}} \right) + \frac{f_{k} T}{C_{\mathrm{cpu},k}} \ge L_{\mathrm{min},k}, \forall k, \\ \mathrm{C2} - 2 : \varepsilon_{k} (f_{k})^{3} T + P_{\mathrm{c},k} \left(\sum_{n=1}^{N} t_{n,k}^{\mathbf{b}} \right) + P_{k} + p_{\mathrm{c},k} t_{k}^{\mathbf{a}} \\ & \leq \sum_{n=1}^{N} \left(\frac{\beta T}{N} P_{\mathbf{u}} g_{n,k} \eta - x_{n,k} P_{\mathbf{u}} g_{n,k} \eta \right), \forall k, \\ \mathrm{C3}, \mathrm{C4}, \mathrm{C6} - 1 : 0 \le x_{n,k} \le t_{n,k}^{\mathbf{b}}, \forall k, \forall n, \\ \mathrm{C7} - 1 : t_{n,k}^{\mathbf{b}} \ge 0, \forall n, \forall k, t_{k}^{\mathbf{a}} \ge 0, P_{k} \ge 0, \forall k, \end{split}$$

where $\mathcal{V}_3 = \{\beta, \{t_{n,k}^{\mathrm{b}}\}, \{t_k^{\mathrm{a}}\}, \{P_k\}, \{f_k\}, \{x_{n,k}\}\}.$ **Proposition 2:** $\mathbf{P}_{3\mathrm{a}}$ is convex and can be solved by means

of several convex tools, i.e., the Lagrange duality method. *Proof.* Please see Appendix B.

In Theorem 1, the Lagrange duality method is employed to achieve the optimal solutions to several optimization variables under a given trajectory, as an effort to gain more insights.

Theorem 1: Under a given trajectory \mathbf{q}_{ij} , the optimal power reflection coefficient in the *n*-th time slot $\alpha_{n,k}^*$, transmit power p_k^* and local computing frequency f_k^* of the k-th IoT node are determined by

$$\alpha_{n,k}^{*} = \left[\frac{\left(w_{k} + \theta_{k}\right)B}{\left(\overline{\omega}_{k}P_{\mathrm{u}}g_{n,k}\eta + \varphi_{n,k}\right)\ln 2} - \frac{B\sigma^{2}}{\xi P_{\mathrm{u}}g_{n,k}h_{k}}\right]^{+}, \forall n, \forall k,$$
(12)

$$p_k^* = \left[\frac{\left(w_k + \theta_k\right)B}{\varpi_k \ln 2} - \frac{B\sigma^2}{h_k}\right]^+, \forall k,$$
(13)

$$f_k^* = \sqrt{\frac{(w_k + \theta_k)}{3\varpi_k \varepsilon_k C_{\text{cpu},k}} - \frac{\phi_k}{3\varpi_k \varepsilon_k T}}, \forall k,$$
(14)

where $\boldsymbol{\theta} = (\theta_1, \theta_2, \dots, \theta_K), \boldsymbol{\varpi} = (\varpi_0, \varpi_1, \varpi_2, \dots, \varpi_K), \boldsymbol{\phi} =$ $(\phi_1, \phi_2, \dots, \phi_K), \mu = (\mu_0, \mu_1, \dots, \mu_N), \text{ and } \varphi =$ $\begin{pmatrix} \varphi_{1,1} & \cdots & \varphi_{1,K} \\ \vdots & \ddots & \vdots \\ \varphi_{N,1} & \cdots & \varphi_{N,K} \end{pmatrix}$ are the non-negative Lagrange

multipliers with respect to all the constraints for P_{3a} , namely C1 - 2, C2 - 2, C3, C4 and C6 - 1.

Proof. Please see Appendix C.

Based on Theorem 1, we have the following findings. Firstly, the maximum WSCB of all IoT nodes are achieved when each IoT node uses up all its harvested energy. Secondly, the task offloading is chosen by the k-th IoT node only when the channel gain from the k-th IoT node to the MEC server is strong enough, i.e., $h_k > \frac{\sigma^2 \varpi_k \ln 2}{w_k + \theta_k}$. Moreover, as for the k-th IoT node, when its weight is large, it prefers to perform task offloading. Thirdly, the k-th IoT node performs local computation only when $\frac{(w_k+\theta_k)}{C_{max}} > \frac{\phi_k}{T}$ holds and a larger weight of the k-th IoT node brings a larger computation frequency at the k-th IoT node. The reasons are as follows. From (12), (13) and (14), it can be observed that $\varpi_k > 0$ must hold for achieving the maximum WSCB of all IoT nodes. Then using the Karush-Kuhn-Tucker (KKT) conditions, the equation $\varpi_k \left(\sum_{n=1}^N \left(\frac{\beta T}{N} P_{\mathbf{u}} g_{n,k} \eta - x_{n,k} P_{\mathbf{u}} g_{n,k} \eta \right) - \varepsilon_k (f_k)^3 T - P_k - \sum_{n=1}^N \left(\frac{\beta T}{N} P_{\mathbf{u}} g_{n,k} \eta - x_{n,k} P_{\mathbf{u}} g_{n,k} \eta \right) - \varepsilon_k (f_k)^3 T - P_k - \sum_{n=1}^N \left(\frac{\beta T}{N} P_{\mathbf{u}} g_{n,k} \eta - x_{n,k} P_{\mathbf{u}} g_{n,k} \eta \right) - \varepsilon_k (f_k)^3 T - P_k - \sum_{n=1}^N \left(\frac{\beta T}{N} P_{\mathbf{u}} g_{n,k} \eta - x_{n,k} P_{\mathbf{u}} g_{n,k} \eta \right) - \varepsilon_k (f_k)^3 T - P_k - \sum_{n=1}^N \left(\frac{\beta T}{N} P_{\mathbf{u}} g_{n,k} \eta - x_{n,k} P_{\mathbf{u}} g_{n,k} \eta \right) - \varepsilon_k (f_k)^3 T - P_k - \sum_{n=1}^N \left(\frac{\beta T}{N} P_{\mathbf{u}} g_{n,k} \eta - x_{n,k} P_{\mathbf{u}} g_{n,k} \eta \right) - \varepsilon_k (f_k)^3 T - P_k - \sum_{n=1}^N \left(\frac{\beta T}{N} P_{\mathbf{u}} g_{n,k} \eta - x_{n,k} P_{\mathbf{u}} g_{n,k} \eta \right) - \varepsilon_k (f_k)^3 T - P_k - \sum_{n=1}^N \left(\frac{\beta T}{N} P_{\mathbf{u}} g_{n,k} \eta - x_{n,k} P_{\mathbf{u}} g_{n,k} \eta \right) - \varepsilon_k (f_k)^3 T - P_k - \sum_{n=1}^N \left(\frac{\beta T}{N} P_{\mathbf{u}} g_{n,k} \eta - x_{n,k} P_{\mathbf{u}} g_{n,k} \eta \right) - \varepsilon_k (f_k)^3 T - P_k - \sum_{n=1}^N \left(\frac{\beta T}{N} P_{\mathbf{u}} g_{n,k} \eta - x_{n,k} P_{\mathbf{u}} g_{n,k} \eta \right) - \varepsilon_k (f_k)^3 T - P_k - \sum_{n=1}^N \left(\frac{\beta T}{N} P_{\mathbf{u}} g_{n,k} \eta - x_{n,k} P_{\mathbf{u}} g_{n,k} \eta \right) - \varepsilon_k (f_k)^3 T - P_k - \sum_{n=1}^N \left(\frac{\beta T}{N} P_{\mathbf{u}} g_{n,k} \eta - x_{n,k} P_{\mathbf{u}} g_{n,k} \eta \right) - \varepsilon_k (f_k)^3 T - P_k - \sum_{n=1}^N \left(\frac{\beta T}{N} P_{\mathbf{u}} g_{n,k} \eta \right) - \varepsilon_k (f_k)^3 T - \sum_{n=1}^N \left(\frac{\beta T}{N} P_{\mathbf{u}} g_{n,k} \eta \right) - \varepsilon_k (f_k)^3 T - \sum_{n=1}^N \left(\frac{\beta T}{N} P_{\mathbf{u}} g_{n,k} \eta \right) - \varepsilon_k (f_k)^3 T - \sum_{n=1}^N \left(\frac{\beta T}{N} P_{\mathbf{u}} g_{n,k} \eta \right) - \varepsilon_k (f_k)^3 T - \sum_{n=1}^N \left(\frac{\beta T}{N} P_{\mathbf{u}} g_{n,k} \eta \right) - \varepsilon_k (f_k)^3 T - \sum_{n=1}^N \left(\frac{\beta T}{N} P_{\mathbf{u}} g_{n,k} \eta \right) - \varepsilon_k (f_k)^3 T - \sum_{n=1}^N \left(\frac{\beta T}{N} P_{\mathbf{u}} g_{n,k} \eta \right) - \varepsilon_k (f_k)^3 T - \sum_{n=1}^N \left(\frac{\beta T}{N} P_{\mathbf{u}} g_{n,k} \eta \right) - \varepsilon_k (f_k)^3 T - \sum_{n=1}^N \left(\frac{\beta T}{N} P_{\mathbf{u}} g_{n,k} \eta \right) - \varepsilon_k (f_k)^3 T - \sum_{n=1}^N \left(\frac{\beta T}{N} P_{\mathbf{u}} g_{n,k} \eta \right) - \varepsilon_k (f_k)^3 T - \sum_{n=1}^N \left(\frac{\beta T}{N} P_{\mathbf{u}} g_{n,k} \eta \right) - \varepsilon_k (f_k)^3 T - \sum_{n=1}^N \left(\frac{\beta T}{N} P_{\mathbf{u}} g_{n,k} \eta \right) - \varepsilon_k (f_k)^3 T - \sum_{n=1}^N \left(\frac{\beta T}{N} P_{\mathbf{u}} g_{n,k} \eta \right) - \varepsilon_k (f_k)^3 T - \sum_{n=1}^N \left(\frac{\beta T}{N} P_{\mathbf{u}} g_{n,k} \eta$ $\begin{array}{l} \sum_{k=1}^{N} t_{n,k}^{\mathrm{b}} &- p_{\mathrm{c},k} t_{k}^{\mathrm{a}} \\ \text{hold. Combining with } \varpi_{k} &> 0, \text{ we can obtain} \\ \sum_{n=1}^{N} \left(\frac{\beta T}{N} P_{\mathrm{u}} g_{n,k} \eta - x_{n,k} P_{\mathrm{u}} g_{n,k} \eta \right) - P_{\mathrm{c},k} \left(\sum_{n=1}^{N} t_{n,k}^{\mathrm{b}} \right) - \end{array}$ $\varepsilon_k (f_k)^3 T - P_k - p_{c,k} t_k^a = 0$, which indicates that the

harvested energy per IoT node will be used up. Thus, the first finding is obtained. Based on (13), we can see that $h_k > \frac{\sigma^2 \varpi_k \ln 2}{w_k + \theta_k}$ should be satisfied to guarantee a nonzero p_k^* and the larger the k-th IoT node's weight is, the higher the probability with $h_k > \frac{\sigma^2 \varpi_k \ln 2}{w_k + \theta_k}$ holds, resulting in the fact that the k-th IoT node prefers to perform task offloading. Then the second finding is achieved. Based on (14), in order to obtain a nonzero f_k^* , $\frac{(w_k + \theta_k)}{C_{\text{cpu},k}} > \frac{\phi_k}{T}$ must be satisfied and f_k^* will increase with the increasing of w_k . Therefore, the third finding is obtained.

When the communication resource allocation scheme is

given, the trajectory optimization problem is given by

$$\begin{aligned} \mathbf{P_{1b}:} & \max_{\mathbf{q}_{u}[n]} \sum_{k=1}^{K} w_{k} \left(\sum_{n=1}^{N} t_{n,k}^{b} B \log_{2} \left(1 + \frac{\xi \alpha_{n,k} P_{u} h_{k} \beta_{0}}{B \sigma^{2} (H^{2} + \|\mathbf{q}_{u}[n] - \mathbf{q}_{k}\|^{2})} + R_{k}^{a} + R_{k}^{\text{Loc}} \right) \\ & + R_{k}^{a} + R_{k}^{\text{Loc}} \right) \\ \text{s.t. } & \text{C1}: \sum_{n=1}^{N} t_{n,k}^{b} B \log_{2} \left(1 + \frac{\xi \alpha_{n,k} P_{u} h_{k} \beta_{0}}{B \sigma^{2} (H^{2} + \|\mathbf{q}_{u}[n] - \mathbf{q}_{k}\|^{2})} \right) \\ & + R_{k}^{a} + R_{k}^{\text{Loc}} \ge L_{\min,k}, \forall k, \\ & \text{C2}: E_{k}^{\text{Loc}} + P_{c,k} \left(\sum_{n=1}^{N} t_{n,k}^{b} \right) + p_{k} t_{k}^{a} + p_{c,k} t_{k}^{a} \\ & \leq \sum_{n=1}^{N} \frac{\beta_{0} \left(\frac{\beta T}{N} P_{u} \eta - t_{n,k}^{b} \alpha_{n,k} P_{u} \eta \right)}{H^{2} + \|\mathbf{q}_{u}[n] - \mathbf{q}_{k}\|^{2}}, \forall k, \\ & \text{C8}, \text{C9}. \end{aligned}$$

Clearly, the objective function, C1 and C2 are non-convex with respect to $\mathbf{q}_{u}[n]$, leading to the non-convex problem \mathbf{P}_{1b} . To address it, the successive convex approximation (SCA) method is applied, where its main idea is to successively maximize a lower bound of \mathbf{P}_{1b} via optimizing the incremental of the UAV's trajectory at each iteration. Specifically, let $\mathbf{q}_{u,j}[n], \forall n$, denote the local trajectory of the UAV at the *j*-th iteration. Then at the (j + 1)-th iteration, we have the following inequalities, given by,

$$\begin{aligned}
 R_{k,j+1}^{\mathrm{b}} &= \sum_{n=1}^{N} t_{n,k}^{\mathrm{b}} B \log_2 \left(1 + \frac{\xi \alpha_{n,k} P_{\mathrm{u}} h_k \beta_0}{B \sigma^2 \left(H^2 + \| \mathbf{q}_{\mathrm{u},j+1}[n] - \mathbf{q}_k \|^2 \right)} \right) \\
 \geq R_{k,j+1}^{\mathrm{b},\mathrm{low}} &= \sum_{n=1}^{N} t_{n,k}^{\mathrm{b}} B \log_2 \left(1 + \frac{A_{n,k}}{H^2 + \| \mathbf{q}_{\mathrm{u},j}[n] - \mathbf{q}_k \|^2} \right) \\
 - \sum_{n=1}^{N} \frac{t_{n,k}^{\mathrm{b}} B A_{n,k}}{\left(H^2 + \| \mathbf{q}_{\mathrm{u},j}[n] - \mathbf{q}_k \|^2 \right) \left(H^2 + \| \mathbf{q}_{\mathrm{u},j}[n] - \mathbf{q}_k \|^2 + A_{n,k} \right)} \\
 \times \frac{\left(\| \mathbf{q}_{\mathrm{u},j+1}[n] - \mathbf{q}_k \|^2 - \| \mathbf{q}_{\mathrm{u},j}[n] - \mathbf{q}_k \|^2 \right)}{\ln 2}, \forall k, \qquad (15)$$

$$E_{\text{tot}}^{k,j+1} = \sum_{n=1}^{N} \frac{\beta_0 \left(\frac{\beta T}{N} P_{\mathbf{u}} \eta - t_{n,k}^{\mathbf{b}} \alpha_{n,k} P_{\mathbf{u}} \eta\right)}{H^2 + \|\mathbf{q}_{\mathbf{u},j+1}[n] - \mathbf{q}_k\|^2} \ge E_{\text{tot,low}}^{k,j+1}$$
$$= \sum_{n=1}^{N} \frac{B_{n,k}}{H^2 + \|\mathbf{q}_{\mathbf{u},j}[n] - \mathbf{q}_k\|^2} - \sum_{n=1}^{N} \frac{B_{n,k}}{\left(H^2 + \|\mathbf{q}_{\mathbf{u},j}[n] - \mathbf{q}_k\|^2\right)}$$
$$\times \left(\|\mathbf{q}_{\mathbf{u},j+1}[n] - \mathbf{q}_k\|^2 - \|\mathbf{q}_{\mathbf{u},j}[n] - \mathbf{q}_k\|^2\right), \forall k, (16)$$

where $R_{k,j+1}^{\rm b}$ and $E_{\rm tot}^{k,j+1}$ denote the total computation bits and harvested energy at the k-th IoT node during the BackCom phase in the (j + 1)-th iteration, $\mathbf{q}_{{\rm u},j+1}[n], \forall n$, is the UAV's trajectory in the (j + 1)-th iteration, $R_{k,j+1}^{\rm b,low}$ and $E_{\rm tot,low}^{k,j+1}$ are the low bounds of $R_{k,j+1}^{\rm b}$ and $E_{\rm tot}^{k,j+1}$, respectively, $A_{n,k} = \frac{\xi \alpha_{n,k} P_{\rm u} h_k \beta_0}{B\sigma^2}$, and $B_{n,k} = \beta_0 \left(\frac{\beta T}{N} P_{\rm u} \eta - t_{n,k}^{\rm b} \alpha_{n,k} P_{\rm u} \eta\right)$.

Based on (15) and (16), we optimize the trajectory of the UAV in the (j + 1)-th iteration by replacing $R_{k,j+1}^{b}$ and $E_{tot}^{k,j+1}$ with their low bounds, namely $R_{k,j+1}^{b,low}$ and $E_{tot,low}^{k,j+1}$.

Accordingly, $\mathbf{P_{1b}}$ of the (j+1)-th iteration is transformed into

$$\begin{aligned} \mathbf{P}_{2\mathrm{b}} &: \max_{\mathbf{q}_{\mathrm{u},j+1}[n]} \sum_{k=1}^{K} w_k (R_{k,j+1}^{\mathrm{b,low}} + R_k^{\mathrm{a}} + R_k^{\mathrm{Loc}}) \\ \text{s.t. } & \mathrm{C1} - 3 : R_{k,j+1}^{\mathrm{b,low}} + R_k^{\mathrm{a}} + R_k^{\mathrm{Loc}} \ge L_{\min,k}, \forall k, \\ & \mathrm{C2} - 3 : E_k^{\mathrm{Loc}} + P_{\mathrm{c},k} \left(\sum_{n=1}^{N} t_{n,k}^{\mathrm{b}} \right) + p_k t_k^{\mathrm{a}} + p_{\mathrm{c},k} t_k^{\mathrm{a}} \\ & \le E_{\mathrm{tot,low}}^{k,j+1}, \forall k, \\ & \mathrm{C8} - 1 : \| \mathbf{q}_{\mathrm{u},j+1} [n+1] - \mathbf{q}_{\mathrm{u},j+1} [n] \| \le V_{\max} \frac{\beta T}{N}, \forall n, \\ & \mathrm{C9} - 1 : \mathbf{q}_{\mathrm{u},j+1} [1] = \mathbf{q}_{\mathrm{I}}, \mathbf{q}_{\mathrm{u},j+1} [N+1] = \mathbf{q}_{\mathrm{F}}. \end{aligned}$$

Since both $R_{k,j+1}^{b,low}$ and $E_{tot,low}^{k,j+1}$ are concave functions regarding to $\mathbf{q}_{u,j+1}[n]$, \mathbf{P}_{2b} is convex and can be solved by means of several convex tools, i.e., the interior point method. On this basis, we propose a successive trajectory optimization algorithm, as shown in Algorithm 1, to achieve the UAV's trajectory with fixed communication resource allocation. Specifically, \mathbf{P}_{2b} should be optimally solved by means of the convex tools, i.e., CVX [34], in each iteration and the above step continues until the stopping condition is satisfied.

Algorithm 1 Successive Trajectory Optimization with Fixed Communication Resource Allocation

- 1: Initialize the UAV's trajectory as $\mathbf{q}_{u,0}[n], \forall n$, and set j = 0;
- 2: Set the maximum allowed number of iterations as I_{max} and Flag = 0;
- 3: repeat
- 4: Solve \mathbf{P}_{2b} and obtain the optimal trajectory as $\mathbf{q}_{u,j+1}[n], \forall n;$
- 5: **if** $\mathbf{q}_{u,j+1}[n]$ is converge to $\mathbf{q}_{u,j}[n], \forall n$ then

6: Set
$$\mathbf{q}_{\mathbf{u}}^*[n] = \mathbf{q}_{\mathbf{u},j+1}[n], \forall n \text{ and set } \text{Flag} = 1;$$

- 7: else
- 8: Set j = j + 1 and Flag = 0;
- 9: end if
- 10: **until** $j = I_{\text{max}}$ or Flag = 1.

C. Design of Two-stage Alternating Iterative Algorithm

Here we propose a two-stage alternating iterative algorithm to solve \mathbf{P}_1 and the detailed process is shown in Algorithm 2. Specifically, we take turns to solve \mathbf{P}_{3a} and \mathbf{P}_{1b} and obtain their optimal solutions in each iteration. Note that \mathbf{P}_{3a} is _optimally solved by means of CVX, while \mathbf{P}_{1b} is solved by ²using Algorithm 1. The above steps will continue until the stopping condition is satisfied.

The complexity of the proposed two-stage alternating iterative algorithm in Algorithm 2 is provided as follows. Assume that the interior point method is applied to obtain the optimal solutions to \mathbf{P}_{3a} and \mathbf{P}_{2b} . According to [34], the complexities for solving \mathbf{P}_{3a} and \mathbf{P}_{2b} are computed as $O(\sqrt{5K + 2KN + 3}\log(5K + 2KN + 3))$ and $O(\sqrt{2K + N}\log(2K + N))$, where $O(\cdot)$ is the big-O notation. Let N_1 and N_2 denote the number of iterations of Algorithm 1 and Algorithm 2, then The complexity of the proposed two-stage alternating iterative algorithm is given by $N_2(O(\sqrt{5K + 2KN + 3}\log(5K + 2KN + 3)) + N_1O(\sqrt{2K + N}\log(2K + N)))$. Algorithm 2 Two-stage Alternating Iterative Algorithm

- 1: Initialize the trajectory of the UAV and the maximum tolerance error δ_t ;
- 2: repeat
- 3: Solve P_{3a} with the fixed UAV's trajectory via CVX and obtain the optimal communication resource allocation;
- Compute the WSCB of all IoT nodes as R_{sum}^1 ; 4:
- Solve P_{1b} with the fixed communication resource allo-5: cation obtained in the above step by using Algorithm 1 and obtain the UAV's trajectory;
- Compute the WSCB of all IoT nodes as R_{sum}^2 ; 6.
- 7: **until** $|R_{sum}^2 R_{sum}^1| \le \delta_t$; 8: Output the obtained communication resource allocation and trajectory.

IV. BINARY OFFLOADING BASED WSCB MAXIMIZATION

In this section, considering the binary offloading mode at each IoT node, the WSCB maximization is studied for the UAV-enabled WP-MEC network with hybrid passive and active communications. Specifically, by formulating the WSCB maximization problem for the considered network, the local computation frequencies and time, the reflection coefficients, the transmit powers, the BackCom time and the AT time of IoT nodes, the trajectory of the UAV, as well as the mode selection of each IoT node for choosing either task offloading or local computation are jointly optimized. The formulated problem not only involves the optimization of the UAV's trajectory, but also includes the optimization of the mode selection, leading to a mixed integer non-convex optimization problem. To address this problem, a three-stage alternating iterative algorithm is devised.

A. Problem Formulation

Based on (9) and (11), the WSCB maximization problem under the binary offloading mode is formulated as

$$\begin{aligned} \mathbf{P}_{4} &: \max_{\mathcal{V}_{4}} \sum_{i \in \mathcal{K}_{\mathrm{L}}} w_{i} R_{i}^{\mathrm{L},\mathrm{B}} + \sum_{l \in \mathcal{K}_{\mathrm{O}}} w_{l} R_{l}^{\mathrm{O},\mathrm{B}} \\ \text{s.t. } \mathrm{F1} &: R_{i}^{\mathrm{L},\mathrm{B}} \geq L_{\min,i}, i \in \mathcal{K}_{\mathrm{L}}, R_{l}^{\mathrm{O},\mathrm{B}} \geq L_{\min,l}, l \in \mathcal{K}_{\mathrm{O}}, \\ \mathrm{F2} &: E_{i}^{\mathrm{Loc}} \leq E_{i}^{\mathrm{L},\mathrm{B}}, i \in \mathcal{K}_{\mathrm{L}}, P_{\mathrm{c},l} \left(\sum_{n=1}^{N} t_{n,l}^{\mathrm{b}}\right) + p_{l} t_{l}^{\mathrm{a}} + p_{\mathrm{c},l} t_{l}^{\mathrm{a}} \\ &\leq E_{l}^{\mathrm{O},\mathrm{B}}, l \in \mathcal{K}_{\mathrm{O}}, \\ \mathrm{F3} &: 0 \leq f_{i} \leq f_{i}^{\max}, i \in \mathcal{K}_{\mathrm{L}}, \\ \mathrm{F4} &: 0 < \beta < 1, \sum_{l \in \mathcal{K}_{\mathrm{O}}} t_{n,l}^{\mathrm{b}} \leq \frac{\beta T}{N}, \forall n, \sum_{l \in \mathcal{K}_{\mathrm{O}}} t_{l}^{\mathrm{a}} \leq (1 - \beta) \mathcal{I}, \\ \mathrm{F5} &: 0 \leq \tau_{i} \leq \mathcal{I}, i \in \mathcal{K}_{\mathrm{L}}, \\ \mathrm{F6} &: 0 \leq \alpha_{n,l} \leq 1, l \in \mathcal{K}_{\mathrm{O}}, \forall n, \\ \mathrm{F7} &: t_{n,l}^{\mathrm{b}} \geq 0, \forall n, t_{l}^{\mathrm{a}} \geq 0, p_{l} \geq 0, l \in \mathcal{K}_{\mathrm{O}}, \\ \mathrm{F8} &: \mathcal{K}_{\mathrm{L}} \cup \mathcal{K}_{\mathrm{O}} = \mathcal{K}, \mathcal{K}_{\mathrm{L}} \cap \mathcal{K}_{\mathrm{O}} = \emptyset, \\ \mathrm{F9} &: \|\mathbf{q}_{\mathrm{u}}[n + 1] - \mathbf{q}_{\mathrm{u}}[n]\| \leq V_{\max} \frac{\beta T}{N}, \forall n, \\ \mathrm{F10} &: \mathbf{q}_{\mathrm{u}}[1] = \mathbf{q}_{\mathrm{I}}, \mathbf{q}_{\mathrm{u}}[N + 1] = \mathbf{q}_{\mathrm{F}}, \end{aligned}$$

 $\{\mathbf{q}_{n}\}\}$.

In P₄, F1 and F2 are the minimum tasks requirement and the energy causal constraints per IoT node, respectively. F3

constrains the maximum allowed computation frequency at the IoT node who performs fully local computation. Both F4 and F5 are time allocation constrains which ensure that the total consumed time for task execution is not larger than T. F6 indicates the range of the power reflection coefficient of the IoT node who chooses to offload tasks. F8 is the user operation selection constraint, where each IoT node either computes its tasks locally or performs task offloading. F9 is the speed constraint and F10 constrains the UAV's initial and final horizontal location.

 \mathbf{P}_4 is a mixed integer non-convex problem due to the following reasons. Firstly, P_4 involves the optimization of the user mode selection. Secondly, the optimization of the trajectory of the UAV exists in P_4 , bringing coupled relationships between the trajectory and communication/computation resources. Thirdly, the coupled relationships among different optimization variables of communication/computation resources further increase the difficulty of solving \mathbf{P}_4 .

B. Solution

Similar to \mathbf{P}_1 , here \mathbf{P}_4 is decoupled into two sub-problems, where one sub-problem is P_4 with a fixed trajectory, denoted by P_{4a} , and the other is P_4 with fixed communication resources, namely $\mathbf{P}_{4b},$ respectively. Accordingly, \mathbf{P}_{4a} can be formulated as

$$\mathbf{P}_{4a} : \max_{\mathcal{V}_5} \sum_{i \in \mathcal{K}_L} w_i R_i^{L,B} + \sum_{l \in \mathcal{K}_O} w_l R_l^{O,B}$$

s.t. F1 - F8,

where $\mathcal{V}_5 = \{\beta, \{t_{n,l}^{\mathrm{b}}\}, \{t_l^{\mathrm{a}}\}, \{p_l\}, \{f_i\}, \{\tau_i\}, \{\alpha_{n,l}\}, \mathcal{K}_{\mathrm{L}}, \mathcal{K}_{\mathrm{O}}\}.$ It is obvious that $\mathbf{P}_{4\mathrm{a}}$ is still a non-convex problem. To

address this problem, we first introduce the following proposition to clarify the optimal computing time of the IoT node that performs local computation and decouples the coupled relationship between the computing frequency and time of the IoT node.

Proposition 3: The WSCB of all the IoT nodes for the considered network under the binary offloading mode are maximized when the IoT node that performs local computation executes its tasks during the whole transmission block, i.e., $\tau_i = T, i \in \mathcal{K}_{\mathrm{L}}.$

Proof. This proposition can be proved by means of contradictions and the process of the proof is similar to Appendix A. Therefore, the detailed process is omitted.

According to Proposition 3, P_{4a} can be transformed as

$$\begin{split} \mathbf{P}_{5a} : \max_{\mathcal{V}_{6}} & \sum_{i \in \mathcal{K}_{L}} \frac{w_{i}l_{i}I}{C_{cpu,i}} + \sum_{l \in \mathcal{K}_{O}} w_{l}R_{l}^{O,B} \\ \text{s.t. } \mathrm{F1} - 1 : & \frac{f_{i}T}{C_{cpu,i}} \ge L_{\min,i}, i \in \mathcal{K}_{L}, R_{l}^{O,B} \ge L_{\min,l}, l \in \mathcal{K}_{O}, \\ \mathrm{F2} - 1 : & \varepsilon_{i}(f_{i})^{3}T \le E_{i}^{\mathrm{L},B}, i \in \mathcal{K}_{\mathrm{L}}, \\ & P_{\mathrm{c},l}\left(\sum_{n=1}^{N} t_{n,l}^{\mathrm{b}}\right) + p_{l}t_{l}^{\mathrm{a}} + p_{\mathrm{c},l}t_{l}^{\mathrm{a}} \le E_{l}^{\mathrm{O,B}}, l \in \mathcal{K}_{O}, \\ \mathrm{F3}, \mathrm{F4}, \mathrm{F6} - \mathrm{F8}, \end{split}$$

where $\mathcal{V}_4 = \left\{\beta, \left\{t_{n,l}^{\mathrm{b}}\right\}, \left\{t_{l}^{\mathrm{a}}\right\}, \left\{p_{l}\right\}, \left\{f_{i}\right\}, \left\{\tau_{i}\right\}, \left\{\alpha_{n,l}\right\}, \mathcal{K}_{\mathrm{L}}, \mathcal{K}_{\mathrm{O}}\right\}$, where $\mathcal{V}_6 = \left\{\beta, \left\{t_{n,l}^{\mathrm{b}}\right\}, \left\{t_{l}^{\mathrm{a}}\right\}, \left\{p_{l}\right\}, \left\{f_{i}\right\}, \left\{\alpha_{n,l}\right\}, \mathcal{K}_{\mathrm{L}}, \mathcal{K}_{\mathrm{O}}\right\}$. In order to efficiently deal with the optimization of the user

mode selection, we introduce a binary variable, denoted by $\lambda_k \ (\lambda_k \in \{0,1\}, \forall k)$, into \mathbf{P}_{5a} , where $\lambda_k = 1$ indicates that the k-th IoT node performs task offloading and $\lambda_k = 0$ means that the k-th IoT node chooses to compute its tasks locally. Substituting λ_k into \mathbf{P}_{5a} , we have

$$\begin{split} \mathbf{P}_{6a} &: \max_{\mathcal{V}_{7}} \sum_{k=1}^{K} w_{k} \left(\lambda_{k} \left(\sum_{n=1}^{N} t_{n,k}^{b} B \log_{2} \left(1 + \frac{\xi \alpha_{n,k} P_{u}g_{n,k}h_{k}}{B\sigma^{2}} \right) \right) \\ &+ t_{k}^{a} B \log_{2} \left(1 + \frac{p_{k}h_{k}}{B\sigma^{2}} \right) \right) + (1 - \lambda_{k}) \frac{f_{k}T}{C_{cpu,k}} \right) \\ \text{s.t. F1} &- 2 : \lambda_{k} \left(\sum_{n=1}^{N} t_{n,k}^{b} B \log_{2} \left(1 + \frac{\xi \alpha_{n,k} P_{u}g_{n,k}h_{k}}{B\sigma^{2}} \right) \right) \\ &+ t_{k}^{a} B \log_{2} \left(1 + \frac{p_{k}h_{k}}{B\sigma^{2}} \right) \right) + \frac{(1 - \lambda_{k})f_{k}T}{C_{cpu,k}} \geq L_{\min,k}, \forall k, \\ \text{F2} &- 2 : (1 - \lambda_{k}) \varepsilon_{k} (f_{k})^{3}T \\ &+ \lambda_{k} \left(P_{c,k} \left(\sum_{n=1}^{N} t_{n,k}^{b} \right) + p_{k} t_{k}^{a} + p_{c,k} t_{k}^{a} \right) \\ &\leq \sum_{n=1}^{N} \left(\frac{\beta T}{N} P_{u}g_{n,k}\eta - \lambda_{k} t_{n,k}^{b} \alpha_{n,k} P_{u}g_{n,k}\eta \right), \forall k, \\ \text{F3} &- 1 : 0 \leq (1 - \lambda_{k}) f_{k} \leq f_{k}^{\max}, \forall k, \\ \text{F4} &- 1 : 0 < \beta < 1, \sum_{k=1}^{K} \lambda_{k} t_{n,k}^{b} \leq \frac{\beta T}{N}, \forall n, \\ &\sum_{k=1}^{K} \lambda_{k} t_{k}^{a} \leq (1 - \beta) T, \\ \text{F6} &- 1 : 0 \leq \lambda_{k} \alpha_{n,k} \leq 1, \forall k, \forall n \\ \text{F7} &- 1 : t_{n,k}^{b} \geq 0, \forall n, t_{k}^{a} \geq 0, p_{k} \geq 0, \forall k, \\ \text{F8} &- 1 : \lambda_{k} \in \{0, 1\}, \forall k, \end{split}$$

where $\mathcal{V}_7 = \left\{ \beta, \left\{ t_{n,k}^{\mathrm{b}} \right\}, \left\{ t_k^{\mathrm{a}} \right\}, \left\{ p_k \right\}, \left\{ f_k \right\}, \left\{ \alpha_{n,k} \right\}, \lambda_k \right\}.$

 \mathbf{P}_{6a} is a mixed integer non-convex problem. To address the issue arisen from the integer optimization, we relax the integer variable λ_k as a continuous real variable that varies from 0 to 1 by following [35]. Note that such a relaxation removes the integer optimization, bringing a more tractable problem. Thus, \mathbf{P}_{6a} can be relaxed as

$$\begin{aligned} \mathbf{P}_{7a} : & \max_{\mathcal{V}_{7}} \sum_{k=1}^{K} w_{k} \bigg(\lambda_{k} \bigg(\sum_{n=1}^{N} t_{n,k}^{b} B \log_{2} \bigg(1 + \frac{\xi \alpha_{n,k} P_{u} g_{n,k} h_{k}}{B \sigma^{2}} \bigg) \\ & + t_{k}^{a} B \log_{2} \bigg(1 + \frac{p_{k} h_{k}}{B \sigma^{2}} \bigg) \bigg) + (1 - \lambda_{k}) \frac{f_{k} T}{C_{cpu,k}} \bigg) \\ \text{s.t. F1} - 2, F2 - 2, F3 - 1, F4 - 1, F6 - 1, F7 - 1, \\ F8 - 2 : \lambda_{k} \in [0, 1], \forall k. \end{aligned}$$

However, \mathbf{P}_{7a} is still non-convex since the optimization of λ_k is highly coupled with the optimization of other communication resources. To tackle this issue, we also apply the BCD technique to handle \mathbf{P}_{7a} . Specifically, \mathbf{P}_{7a} can be decoupled into two sub-problems: \mathbf{P}_{7a} with fixed λ_k and \mathbf{P}_{7a} with other communication resources fixed. When λ_k is fixed, \mathbf{P}_{7a} is reduced to

$$\begin{aligned} \mathbf{P}_{8a} : \max_{\mathcal{V}_8} \sum_{k=1}^{K} w_k \bigg(\lambda_k \bigg(\sum_{n=1}^{N} t_{n,k}^{b} B \log_2 \bigg(1 + \frac{\xi \alpha_{n,k} P_u g_{n,k} h_k}{B \sigma^2} \bigg) \\ &+ t_k^{a} B \log_2 \bigg(1 + \frac{p_k h_k}{B \sigma^2} \bigg) \bigg) + (1 - \lambda_k) \frac{f_k T}{C_{cpu,k}} \bigg) \\ \text{s.t. F1} - 2, \text{F2} - 2, \text{F3} - 1, \text{F4} - 1, \text{F6} - 1, \text{F7} - 1, \end{aligned}$$

where $\mathcal{V}_8 = \{\beta, \{t_{n,k}^{\mathrm{b}}\}, \{t_k^{\mathrm{a}}\}, \{p_k\}, \{f_k\}, \{\alpha_{n,k}\}\}$. To deal with the coupled relationships among different optimization variables in \mathbf{P}_{8a} , the following variables are introduced:

 $x_{n,k} = t_{n,k}^{\rm b} \alpha_{n,k}, \forall n, \forall k$, and $P_k = p_k t_k^{\rm a}, \forall k$, and then \mathbf{P}_{8a} can be rewritten as

$$\begin{split} \mathbf{P}_{9a} : & \max_{\mathcal{V}_9} \sum_{k=1}^{K} w_k \bigg(\lambda_k \bigg(\sum_{n=1}^{N} t_{n,k}^{b} B \log_2 \left(1 + \frac{\xi x_{n,k} P_u g_{n,k} h_k}{t_{n,k}^{b} B \sigma^2} \right) \\ & + t_k^{a} B \log_2 \left(1 + \frac{P_k h_k}{t_k^{a} B \sigma^2} \right) \bigg) + (1 - \lambda_k) \frac{f_k T}{C_{\text{cpu},k}} \bigg) \\ \text{s.t. F1} - 3 : & \lambda_k \bigg(\sum_{n=1}^{N} t_{n,k}^{b} B \log_2 \left(1 + \frac{\xi x_{n,k} P_u g_{n,k} h_k}{t_{n,k}^{b} B \sigma^2} \right) \bigg) \\ & + t_k^{a} B \log_2 \left(1 + \frac{P_k h_k}{t_k^{a} B \sigma^2} \right) \bigg) + \frac{(1 - \lambda_k) f_k T}{C_{\text{cpu},k}} \\ & \geq L_{\min,k}, \forall k, \\ \text{F2} - 3 : & \lambda_k \bigg(P_{c,k} \bigg(\sum_{n=1}^{N} t_{n,k}^{b} \bigg) + P_k + p_{c,k} t_k^{a} \bigg) \\ & + (1 - \lambda_k) \varepsilon_k (f_k)^3 T \\ & \leq \sum_{n=1}^{N} \bigg(\frac{\beta T}{N} P_u g_{n,k} \eta - \lambda_k x_{n,k} P_u g_{n,k} \eta \bigg), \forall k, \\ \text{F3} - 1, \text{F4} - 1, \text{F6} - 2 : 0 \leq \lambda_k x_{n,k} \leq t_{n,k}^{b}, \forall k, \forall n, \\ \text{F7} - 2 : t_{n,k}^{b} \geq 0, \forall n, t_k^{a} \geq 0, P_k \geq 0, \forall k, \end{split}$$

where $\mathcal{V}_9 = \{\beta, \{t_{n,k}^{\mathrm{b}}\}, \{t_k^{\mathrm{a}}\}, \{P_k\}, \{f_k\}, \{x_{n,k}\}\}$. It is easy to prove that $\mathbf{P}_{9\mathrm{a}}$ is convex and the detailed process of the proof is similar to Appendix B and is omitted here for brevity.

When other communication resources are fixed, \mathbf{P}_{7a} can be transformed as

$$\begin{aligned} \mathbf{P}_{10a}: & \max_{\{\lambda_k\}} \sum_{k=1}^{K} w_k \bigg(\lambda_k \bigg(\sum_{n=1}^{N} t_{n,k}^{\mathrm{b}} B \log_2 \Big(1 + \frac{\xi \alpha_{n,k} P_{\mathrm{u}} g_{n,k} h_k}{B \sigma^2} \Big) \\ & + t_k^{\mathrm{a}} B \log_2 \Big(1 + \frac{p_k h_k}{B \sigma^2} \Big) \bigg) + (1 - \lambda_k) \frac{f_k T}{C_{\mathrm{cpu},k}} \bigg) \\ \text{s.t. F1} - 2, F2 - 2, F3 - 1, F4 - 1, F6 - 1, F8 - 2. \end{aligned}$$

Obviously, \mathbf{P}_{10a} is a linear optimization problem regarding to λ_k , which can be solved by means of several convex tools.

Likewise, \mathbf{P}_{4b} is reformulated as

$$\begin{split} \mathbf{P}_{4\mathbf{b}} &: \max_{\mathbf{q}_{u}[n]_{k=1}^{N}} \sum_{k=1}^{K} w_{k} \bigg(\lambda_{k} \bigg(\sum_{n=1}^{N} t_{n,k}^{\mathbf{b}} B \log_{2} \bigg(1 + \frac{\xi \alpha_{n,k} P_{u} h_{k} \beta_{0}}{B \sigma^{2} (H^{2} + \|\mathbf{q}_{u}[n] - \mathbf{q}_{k}\|^{2})} \bigg) \\ &+ t_{k}^{\mathbf{a}} B \log_{2} \bigg(1 + \frac{p_{k} h_{k}}{B \sigma^{2}} \bigg) \bigg) + (1 - \lambda_{k}) \frac{f_{k} T}{C_{cpu,k}} \bigg) \\ \text{s.t. F1} - 2 : \lambda_{k} \bigg(\sum_{n=1}^{N} t_{n,k}^{\mathbf{b}} B \log_{2} \bigg(1 + \frac{\xi \alpha_{n,k} P_{u} h_{k} \beta_{0}}{B \sigma^{2} (H^{2} + \|\mathbf{q}_{u}[n] - \mathbf{q}_{k}\|^{2})} \bigg) \\ &+ t_{k}^{\mathbf{a}} B \log_{2} \bigg(1 + \frac{p_{k} h_{k}}{B \sigma^{2}} \bigg) \bigg) + \frac{(1 - \lambda_{k}) f_{k} T}{C_{cpu,k}} \\ &\geq L_{\min,k}, \forall k, \\ \text{F2} - 2 : \lambda_{k} \bigg(P_{c,k} \bigg(\sum_{n=1}^{N} t_{n,k}^{\mathbf{b}} \bigg) + p_{k} t_{k}^{\mathbf{a}} + p_{c,k} t_{k}^{\mathbf{a}} \bigg) \\ &+ (1 - \lambda_{k}) \varepsilon_{k} (f_{k})^{3} T \\ &\leq \sum_{n=1}^{N} \frac{\big(\frac{\beta T}{N} P_{u} - \lambda_{k} t_{n,k}^{\mathbf{b}} \alpha_{n,k} P_{u} \big) \beta_{0} \eta}{(H^{2} + \|\mathbf{q}_{u}[n] - \mathbf{q}_{k}\|^{2})}, \forall k, \\ \text{F9, F10.} \end{split}$$

In order to solve P_{4b} , the SCA technique is applied by following P_{1b} . Accordingly, P_{4b} in the (j+1)-th iteration is

Tabel 1: Key Simulation Settings

Parameters	Notation	Value
Number of IoT nodes	K	4
Number of time slots	N	50
Altitude of the UAV	H	10 m
The maximum speed of the UAV	$V_{\rm max}$	$20 \ m/s$
The entire transmission block	T	2 seconds
The system bandwidth	В	100 kHz
The number of CPU cycles for computing 1 bit at the k-th IoT node	$C_{\mathrm{cpu},k}$	1000 cycles/bit
The BackCom's fixed circuit power consumption at the k-th IoT node	$P_{\mathrm{c},k}$	100 µW
The AT's fixed circuit power consumption at the k -th IoT node	$p_{\mathrm{c},k}$	1 mW
The UAV's transmit power	$P_{\rm u}$	1 W
The fixed energy conversion efficiency per IoT node	η	0.7
The performance gap reflecting the real modulation for BackCom	ξ	-15 dB
The noise power spectral density	σ^2	-120 dBm/Hz
Channel gain at reference distance	β_0	-30 dB
The effective capacitance coefficient at the k-th IoT node	ε_k	10^{-26}
The maximum CPU frequency of the k-th IoT node	f_k^{\max}	500 MHz
The minimum required bits computed by the k-th IoT node	$L_{\min,k}$	10 kbits

transformed into

Algorithm 3 Three-stage Alternating Iterative Algorithm

- 1: Initialize the iterative number J = 1;
- 2: Initialize the trajectory of the UAV $\mathbf{q}_{n}^{J}[n], \forall n$, and the maximum tolerance errors δ_1 and δ_2 ;
- 3: repeat
- Initialize the iterative number jj = 1 and λ_k^{jj} , $\forall k$; 4:
- 5: repeat
- $\mathbf{q}_{\mathrm{u}}^{J}[n], \forall n,$ Solve \mathbf{P}_{9a} with given and 6: $\lambda_k^{jj}, \forall k$ via CVX and obtain the optimal communication resource allocation, denoted by $\left\{ \beta^{jj}, \left\{ t_{n,k}^{\text{b},jj} \right\}, \left\{ t_{k}^{\text{a},jj} \right\}, \left\{ P_{k}^{jj} \right\}, \left\{ f_{k}^{jj} \right\}, \left\{ x_{n,k}^{jj} \right\} \right\};$ Compute the WSCB of all IoT nodes as $R_{\text{sum}}^{jj};$
- 7:
- $\begin{array}{l} \text{Solve} \quad \mathbf{P}_{10a} \quad \text{with} \quad \text{gg} \\ \left\{ \beta^{jj}, \left\{ t_{n,k}^{\text{b},jj} \right\}, \left\{ t_{k}^{\text{a},jj} \right\}, \left\{ P_{k}^{jj} \right\}, \left\{ f_{k}^{jj} \right\}, \left\{ x_{n,k}^{jj} \right\} \right\} \\ \text{and} \quad \mathbf{q}_{u}^{J}[n], \forall n, \text{ and obtain } \lambda_{k}^{jj+1}, \forall k; \end{array}$ Solve given 8:
- Compute the WSCB of all IoT nodes as R_{sum}^{jj+1} ; 9: until $|\hat{R}_{\text{sum}}^{jj+1} - R_{\text{sum}}^{jj}| \leq \delta_1;$ 10:
- Output the obtained communication resource allocation 11: under $\mathbf{q}_{n}^{J}[n], \forall n$, and the WSCB of all IoT nodes R_{I}^{s} ;
- Initialize the iterative number j = 1 and the maximum 12: allowed number of iterations I_{max} ;
- Set $\mathbf{q}_{\mathrm{u},j}[n] = \mathbf{q}_{\mathrm{u}}^{J}[n], \forall n;$ 13:
- 14: repeat
- Solve \mathbf{P}_{5b} with given $\left\{\beta^{jj}, \left\{t_{n,k}^{b,jj}\right\}, \left\{t_{k}^{a,jj}\right\}, \left\{P_{k}^{jj}\right\}, \left\{f_{k}^{jj}\right\}, \left\{x_{n,k}^{jj}\right\}, \left\{\lambda_{k}^{jj+1}\right\}\right\}$ 15: and obtain the optimal trajectory as $\mathbf{q}_{\mathbf{u},j+1}[n], \forall n;$ if $\mathbf{q}_{\mathbf{u},j+1}[n]$ is converge to $\mathbf{q}_{\mathbf{u},j}[n], \forall n$ then 16: Set J = J + 1, $\mathbf{q}_{u}^{J}[n] = \mathbf{q}_{u,j+1}[n], \forall n$ and break;
- 17: else 18:
- Set j = j + 1; 19:
- end if 20:
- until $j = I_{\max}$; 21:
- Output the obtained trajectory and the WSCB achieved 22: by all IoT nodes R_{I}^{s} ;

23: **until** $|R_J^s - R_{J-1}^s| \leq \delta_2$;

24: Output the obtained resource allocation and trajectory.

$\mathbf{P}_{5b} : \max_{\mathbf{q}_{u}[n]} \sum_{k=1}^{K} w_{k} \left(\lambda_{k} \left(R_{k,j+1}^{b} + t_{k}^{a} B \log_{2} \left(1 + \frac{p_{k} h_{k}}{B \sigma^{2}} \right) \right) \right)$ $+(1-\lambda_k)\frac{f_kT}{C_{\mathrm{cpu},k}}$ s.t. F1 - 4 : $\lambda_k \left(R_{k,j+1}^{\mathrm{b}} + t_k^{\mathrm{a}} B \log_2 \left(1 + \frac{p_k h_k}{B\sigma^2} \right) \right)$ $+\frac{(\mathbf{i}-\lambda_k)f_kT}{C_{cpu,k}} \ge L_{\min,k}, \forall k,$ F2-4: $(1-\lambda_k) \varepsilon_k (f_k)^3 T$ $+\lambda_k \left(P_{\mathrm{c},k} \left(\sum_{n=1}^N t_{n,k}^{\mathrm{b}} \right) + p_k t_k^{\mathrm{a}} + p_{\mathrm{c},k} t_k^{\mathrm{a}} \right)$ $^{j+1}, \forall$ F9-1: $\|\mathbf{q}_{u,j+1}[n+1] - \mathbf{q}_{u,j+1}[n]\| \le V_{\max} \frac{\beta T}{N}, \forall n,$ $F10 - 1 : \mathbf{q}_{u,i+1}[1] = \mathbf{q}_{I}, \mathbf{q}_{u,i+1}[N+1] = \mathbf{q}_{F},$

where $B_{n,k} = \beta_0 \left(\frac{\beta T}{N} P_{\mathrm{u}} \eta - \lambda_k t_{n,k}^{\mathrm{b}} \alpha_{n,k} P_{\mathrm{u}} \eta \right)$ in $E_{\mathrm{tot}}^{k,j+1}$. Similar to $\mathbf{P}_{2\mathrm{b}}$, $\mathbf{P}_{5\mathrm{b}}$ is also convex, which can be solved by applying convex tools, e.g., CVX.

C. Design of Three-stage Alternating Iterative Algorithm

Here a three-stage alternating iterative algorithm is proposed to solve P_4 and obtain the corresponding resource allocation and trajectory. The steps of this algorithm can be found in Algorithm 3. Specifically, in the outer loop, P_{7a} and P_{4b} should be solved in each iteration, where P_{7a} is solved with fixed trajectory of the UAV and $\mathbf{P}_{4\mathrm{b}}$ is solved under given communication resource allocation. The first inner loop is to solve P_{7a} , where in each iteration, we take turns to optimally solve \mathbf{P}_{9a} and \mathbf{P}_{10a} . The second inner loop is to solve \mathbf{P}_{4b} , where \mathbf{P}_{5b} is optimally solved in each iteration.

As for the proposed three-stage alternating iterative algorithm in Algorithm 3, its complexity is computed as follows. With the interior point method adopted, the complexities for solving P_{9a} , P_{10a} and P_{5b} are given by $O(\sqrt{5K + 2KN + 3}\log(5K + 2KN + 3))$, $O(\sqrt{4K} + KN + 3\log(4K))$ + KN+ 3)) and $O(\sqrt{2K} + N \log(2K + N))$, respectively [34]. Denote L_1, L_2 and L_3 as the number of iterations required for the outer loop, the first inner loop and the second loop. Then the computation complexity of the three-stage alternating iterative algorithm can be calculated as $L_1(L_2(O(\sqrt{5K+2KN+3}\log(5K+2KN+3))+O(\sqrt{4K+KN+3}\log(4K+KN+3))) + L_3O(\sqrt{2K+N}\log(2K+N))).$

V. SIMULATIONS

This section validates the superiority of the proposed schemes by conducting computer simulations. The basic settings of the parameters, unless otherwise specified, are shown in Table I according to [4], [10], [15], [28]. Here the channel gain of the k-th IoT node-the MEC server link is considered as $h_k = h'_k d_k^{-\alpha}$ with the small-scale fading h'_k , distance d_k and path loss exponent α . We set $\alpha = 3$, $d_1 = 12$ m, $d_2 = 10$ m, $d_3 = 15$ m and $d_4 = 13$ m. The locations of IoT nodes are set as $\mathbf{q}_1 = [0,0]$, $\mathbf{q}_2 = [0,10]$, $\mathbf{q}_3 = [10,10]$ and $\mathbf{q}_4 = [10,0]$, respectively. The UAV's initial and final positions are given by $\mathbf{q}_{\mathrm{I}} = [0,0]$ and $\mathbf{q}_{\mathrm{F}} = [10,0]$. The weight vector of all IoT nodes, $[w_1, w_2, w_3, w_4]$, is set as [0.1, 0.4, 0.3, 0.2].

In order to show the advantages of the proposed schemes in terms of the WSCB of all IoT nodes, the performance under the proposed schemes is compared with that under the four baseline schemes, which are called backscatter-assisted UAV-MEC, wireless powered UAV-MEC, the complete offloading scheme and the fully local computing scheme, respectively. For backscatter-assisted UAV-MEC or wireless powered UAV-MEC, each IoT node only chooses BackCom or AT to offload tasks when it performs task offloading. In the complete offloading scheme, all IoT nodes' tasks are offloaded to the MEC server via BackCom, AT or hybrid passive and active communications, while in the fully local computing scheme, all IoT nodes' tasks are executed locally. Note that the above four schemes can also be obtained by using the proposed algorithms after making a few changes. Specifically, the backscatter-assisted UAV-MEC or the wireless powered UAV-MEC is achieved by using the proposed algorithms with $p_k = 0$ and $t_k^{a} = 0, \forall k$ or $t_{n,k}^{b} = 0$ and $\alpha_{n,k} = 0, \forall n, \forall k$, respectively. The complete offloading scheme is obtained by the proposed algorithms with $f_k = 0, \forall k$, while the fully local computing scheme is obtained via the proposed algorithms with $p_k = 0, t_k^{a} = 0, t_{n,k}^{b} = 0$, and $\alpha_{n,k} = 0, \forall n, \forall k$.

Fig. 2 illustrates the convergence analysis of the proposed Algorithm 1, Algorithm 2, and Algorithm 3 under different settings of the UAV's transmit power $P_{\rm u}$ and initial trajectory. Here $P_{\rm u}$ is set as 0.5 W and 1 W, respectively, and two initial trajectories are considered. For the first initial trajectory (denoted as "Initial trajectory 1"), the UAV flies straight with a constant speed from the initial position to the final position. For the second initial trajectory (denoted as "Initial trajectory 2"), the UAV is dispatched from its initial horizontal position [0,0], flies straight to the position [5,10] and then flies to its final horizontal position [10,0] with a constant speed. Specifically, Fig. 2(a) is given to verify the convergence of Algorithm 1, where the communication resource allocation is determined by solving P_{3a} with the given initial trajectory via CVX. Fig. 2(b) shows the convergence of Algorithm 2. In Fig. 2(c), the convergence of Algorithm 3 is demonstrated.

From Fig. 2(a), it can be seen that the proposed successive trajectory optimization algorithm in Algorithm 1 always



Fig. 3. The WSCB of all IoT nodes under the partial offloading mode versus the UAV's transmit power.



Fig. 4. The WSCB of all IoT nodes under the partial offloading mode versus the minimum required bits computed by each IoT node.

converges to the optimal trajectory within 3 iterations, which verifies the effectiveness of Algorithm 1 and illustrates that Algorithm 1 has a fast convergence rate. The proposed twostage alternating iterative algorithm in Algorithm 2 is provided to obtain the proposed scheme under the partial offloading mode. It can be observed from Fig. 2(b) that less than 5 iterations are required for Algorithm 2 to achieve a convergent state. This also indicates the effectiveness and fast convergence of Algorithm 2. Algorithm 3 provides the three-stage alternating iterative algorithm to achieve the proposed scheme under the binary offloading mode. From Fig. 2(c), we can see that the proposed three-stage alternating iterative algorithm only needs several iterations (e.g., 4 iterations) to converge, which illustrates that Algorithm 3 is computationally effective with a fast convergence rate.

Fig. 3 plots the WSCB achieved by all IoT nodes versus $P_{\rm u}$, where $P_{\rm u}$ ranges from 1 W to 3 W and the partial offloading mode is considered for the investigated network. In order to show the advantage of the proposed scheme, the WSCB under the proposed scheme are compared with those obtained by the backscatter-assisted UAV-MEC, the wireless

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Fig. 2. The convergence analysis of the proposed iterative algorithms under different settings of the UAV's transmit power and initial trajectory: (a) the convergence analysis of Algorithm 1; (b) the convergence analysis of Algorithm 2; (c) the convergence analysis for Algorithm 3.

powered UAV-MEC, the complete offloading scheme and the fully local computing scheme. It can be observed from this figure that the WSCB achieved by all IoT nodes under all the schemes will increase when $P_{\rm u}$ increases. The reasons are as follows. When $P_{\rm u}$ is larger, the IoT nodes will offload more tasks to the MEC server via BackCom since the received RF signals are strong, and the total harvested energy per IoT node also increases, resulting in more tasks that can be offloaded by AT or executed locally. Thus, a larger $P_{\rm u}$ brings higher WSCB of all IoT nodes. By comparison, we can also find that the proposed scheme can achieve the best performance in terms of the WSCB of all IoT nodes among the above five schemes since the proposed scheme includes the superiorities of BackCom and AT, and can choose to offload how many task bits more flexibly compared with the complete offloading scheme and the fully local computing scheme. Besides, we can also see that the WSCB in the backscatter-assisted UAV-MEC are higher than those under the wireless powered UAV-MEC since BackCom has a lower energy consumption for offloading task bits. Moreover, when $P_{\rm u}$ is large enough, the WSCB under the complete offloading scheme are higher than those under the fully local computing scheme, even higher than those obtained by the wireless powered UAV-MEC. This is because a larger $P_{\rm u}$ brings a higher harvested energy per IoT node and then each IoT node has enough energy to support task offloading.

Fig. 4 plots the WSCB achieved by all IoT nodes versus the minimum required computation bits per IoT node, where the partial offloading mode is considered. Let $L_{\min,1} = L_{\min,2} = L_{\min,3} = L_{\min,4} = L_{\min}$ and then L_{\min} ranges from 11 kbits to 15 kbits. From this figure, we can see that with the increase of L_{\min} , the WSCB achieved by the proposed scheme, the backscatter-assisted UAV-MEC, the wireless powered UAV-MEC and the fully local computing scheme will decrease, while the WSCB obtained by the complete offloading scheme are always 0. The reasons are listed below. A higher L_{\min} indicates a more strict computation bits requirement for each IoT node. This will lead to a reduction to WSCB since in some cases, the IoT node may not satisfy this requirement. For the complete offloading scheme, P_{u} is not large enough to support



Fig. 5. The WSCB of all IoT nodes under the binary offloading mode versus the UAV's transmit power.

all IoT nodes' task offloading while satisfying the minimum required computation bits. By comparison, it can also be seen that the proposed scheme outperforms the other schemes in terms of the WSCB of all IoT nodes, which also verifies the superiority of combining BackCom and AT.

Fig. 5 plots the WSCB achieved by all IoT nodes under the binary offloading mode versus P_u under different schemes, where $L_{\min} = 5$ kbits. We can observe that the WSCB of all IoT nodes under all the schemes increase with the increasing P_u and the proposed scheme is superior to the other schemes in terms of the WSCB of all IoT nodes since each IoT node can choose to perform either complete task offloading via BackCom, AT or hybrid passive and active communications, or fully local computing flexibly according to its channel gains, bringing an improvement to the computation performance.

Fig. 6 shows the UAV's trajectory under the partial and binary offloading modes. The black line denotes the given initial UAV's trajectory, the blue line with the mark of the blue cross represents the optimized trajectory of the UAV under the partial offloading mode achieved by applying Algorithm 2 while the pink dotted line with the mark of the pink dot expresses the optimized trajectory of the UAV under the binary



Fig. 6. The UAV's trajectory under the partial and binary offloading modes.



Fig. 7. The WSCB of all IoT nodes under the partial and binary offloading modes versus the number of IoT nodes.

offloading mode achieved by using Algorithm 3. The red circles denotes the locations of all IoT nodes. As shown in this figure, the UAV is dispatched from its initial horizontal position [0,0] and then flies to its final horizontal position [10,0] at the end of the BackCom phase. It can be observed that the trajectory under the partial offloading mode is always close to IoT node 2 and IoT node 3 due to the fact that the weights of the two nodes are higher and the UAV needs to fly close to them to provide stronger RF signals for BackCom and more energy so that the WSCB of all IoT nodes can be improved. The trajectory under the binary offloading mode is close to IoT node 2 since its weight is highest. Different from the partial offloading mode, the trajectory under the binary offloading mode is not close to IoT 3 since in this case, only IoT 1 and IoT 2 choose to perform task offloading while the others compute their tasks locally. Therefore, there is no need for the UAV to fly close to IoT 3 to provide stronger RF signals for BackCom. By observations, we also find that the values of the weights can influence the UAV's trajectory and a proper weight can balance the performance of all IoT nodes.

Fig. 7 shows the WSCB of all IoT nodes under the partial and binary offloading modes versus the number of IoT nodes K, where $L_{\min} = 10$ kbits, K ranges from 4 to 8 and the weight of each IoT node is set as 1. It can be observed that the WSCB of all IoT nodes increase with K since with a larger K, more IoT nodes can compute and/or offload their tasks by using their received signals or harvested energy, bringing a higher WSCB. Besides, we also observe that the WSCB under the partial offloading mode is higher than that under the binary offloading mode. This is because the partial offloading mode is more flexible than the binary offloading mode, i.e., IoT nodes under the partial offloading mode can dynamically select the operation mode for achieving a higher WSCB according to the quality of the CSI.

VI. CONCLUSIONS

In this work, the resource allocation schemes for the partial and binary offloading modes were studied in a UAV-enabled WP-MEC network with hybrid passive and active communications. Specifically, two WSCB maximization problems were formulated by optimizing the local computation frequencies and time, the reflection coefficients, and the transmit powers of the IoT nodes, the UAV's trajectory, etc, subject to the QoS, energy causality, speed constraints, etc. Then the optimization problem under the partial offloading mode was solved by the proposed two-stage alternating iterative algorithm, while a three-stage alternating iterative algorithm was proposed to solve the problem under the binary offloading mode. Computer results verified the effectiveness of the proposed algorithms and demonstrated the superiority of the proposed schemes under the partial and binary offloading modes over several baseline schemes in terms of WSCB.

APPENDIX A

In this section, Proposition 1 is proved by means of contradiction. Specifically, when other optimization variables, such as β , $\{t_{n,k}^{\rm b}\}_{k=1}^{K}$, $\{t_{k}^{\rm a}\}_{k=1}^{K}$, $\{p_{k}\}_{k=1}^{K}$, $\alpha_{n,k}$ and $\{f_{i}, \tau_{i}\}_{i=\{1,2,\ldots,K\}\setminus k}$, are given, f_{k} and τ_{k} should be jointly optimized to maximize the WSCB of all IoT nodes for the considered network. Let f_{k}^{*} and τ_{k}^{*} be the optimal computation frequency and time of the k-th IoT node. Suppose that $\tau_{k}^{*} < T$ holds and both f_{k}^{*} and τ_{k}^{*} satisfy all the constraints of \mathbf{P}_{1a} . In this case, the maximum WSCB of all IoT nodes are computed as $R_{\text{total}}^{*} = \sum_{k=1}^{K} w_{k} \left(\sum_{n=1}^{N} t_{n,k}^{\rm b} B \log_{2} \left(1 + \frac{\xi \alpha_{n,k} P_{u} g_{n,k} h_{k}}{B \sigma^{2}} \right) + t_{k}^{*} B \log_{2} \left(1 + \frac{p_{k} h_{k}}{B \sigma^{2}} \right) \right) + \sum_{i=1, i \neq k}^{K} \frac{w_{i} f_{i} \tau_{i}}{C_{\text{cpu},i}} + \frac{w_{k} f_{k}^{*} \tau_{k}^{*}}{C_{\text{cpu},k}}$.

Then we construct another feasible solution, denoted by $\{f_k^+, \tau_k^+\}$, where $\tau_k^+ = T$ and $\tau_k^+ f_k^+ (f_k^+)^2 = \tau_k^* f_k^* (f_k^*)^2$. It can be observed that the constructed solution also satisfies all the constraints of \mathbf{P}_{1a} . Accordingly, the WSCB of all IoT nodes under the constructed solution can be computed as $R_{\text{total}}^+ = \sum_{k=1}^K w_k \left(\sum_{n=1}^N t_{n,k}^{\text{b}} B \log_2 \left(1 + \frac{\xi \alpha_{n,k} P_{\text{u}} g_{n,k} h_k}{B \sigma^2} \right) + t_k^a B \log_2 \left(1 + \frac{p_k h_k}{B \sigma^2} \right) \right) + \sum_{i=1, i \neq k}^K \frac{w_i f_i \tau_i}{C_{\text{cpu},i}} + \frac{w_k f_k^+ \tau_k^+}{C_{\text{cpu},k}}.$ Since $\tau_k^+ = T > \tau^*$ and $\tau_k^+ f_k^+ (f_k^+)^2 = \tau_k^* f_k^* (f_k^*)^2$, we can obtain $f_k^+ < f_k^*$, leading to $\tau_k^+ f_k^+ > \tau_k^* f_k^*$. Then we have $R_{\text{total}}^+ > R_{\text{total}}^*$, which contradicts the above assumption.

$$\mathcal{L} = \sum_{k=1}^{K} w_k \left(\sum_{n=1}^{N} t_{n,k}^{\rm b} B \log_2 \left(1 + \frac{\xi x_{n,k} P_{\rm u} g_{n,k} h_k}{t_{n,k}^{\rm b} B \sigma^2} \right) + t_k^{\rm a} B \log_2 \left(1 + \frac{P_k h_k}{t_k^{\rm a} B \sigma^2} \right) + \frac{f_k T}{C_{\rm cpu,k}} \right) \\
+ \sum_{k=1}^{K} \theta_k \left(\sum_{n=1}^{N} t_{n,k}^{\rm b} B \log_2 \left(1 + \frac{\xi x_{n,k} P_{\rm u} g_{n,k} h_k}{t_{n,k}^{\rm b} B \sigma^2} \right) + t_k^{\rm a} B \log_2 \left(1 + \frac{P_k h_k}{t_k^{\rm a} B \sigma^2} \right) + \frac{f_k T}{C_{\rm cpu,k}} - L_{\min,k} \right) \\
+ \sum_{k=1}^{K} \varpi_k \left(\sum_{n=1}^{N} \left(\frac{\beta T}{N} P_{\rm u} g_{n,k} \eta - x_{n,k} P_{\rm u} g_{n,k} \eta \right) - \varepsilon_k (f_k)^3 T - P_{\rm c,k} \left(\sum_{n=1}^{N} t_{n,k}^{\rm b} \right) - P_k - p_{\rm c,k} t_k^{\rm a} \right) \\
+ \sum_{k=1}^{K} \phi_k \left(f_k^{\max} - f_k \right) + \mu_0 \left(1 - \beta \right) + \sum_{n=1}^{N} \mu_n \left(\frac{\beta T}{N} - \sum_{k=1}^{K} t_{n,k}^{\rm b} \right) + \varpi_0 \left((1 - \beta) T - \sum_{k=1}^{K} t_k^{\rm a} \right) \\
+ \sum_{k=1}^{K} \sum_{n=1}^{N} \varphi_{n,k} \left(t_{n,k}^{\rm b} - x_{n,k} \right).$$
(C.1)

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Therefore, the optimal computation time at the k-th IoT node should be $\tau_k^* = T$.

slot and the optimal transmit power of the k-th IoT node in closed forms, given by,

$$\frac{\partial \mathcal{L}}{\partial x_{n,k}} = \frac{(w_k + \theta_k) \xi P_{\mathbf{u}} g_{n,k} h_k B}{(B\sigma^2 + \alpha_{n,k} \xi P_{\mathbf{u}} g_{n,k} h_k) \ln 2} - \varpi_k P_{\mathbf{u}} g_{n,k} \eta - \varphi_{n,k},$$

$$\partial \mathcal{L} \qquad (w_k + \theta_k) h_k B \tag{C.2}$$

$$\frac{\partial \mathcal{L}}{\partial P_k} = \frac{(\omega_k + v_k) n_k D}{(B\sigma^2 + p_k h_k) \ln 2} - \varpi_k.$$
(C.3)

By letting $\frac{\partial \mathcal{L}}{\partial x_{n,k}} = 0$, the optimal power reflection coefficient at the k-th IoT node in the n-th time slot $\alpha_{n,k}^*$ can be computed as

$$\alpha_{n,k}^* = \left[\frac{(w_k + \theta_k)B}{(\varpi_k P_{\mathrm{u}}g_{n,k}\eta + \varphi_{n,k})\ln 2} - \frac{B\sigma^2}{\xi P_{\mathrm{u}}g_{n,k}h_k}\right]^+, \forall n, \forall k,$$
(C.4)

where $[x]^+ = \max \{x, 0\}$. Similarly, by letting $\frac{\partial \mathcal{L}}{\partial P_k} = 0$, we can obtain the optimal transmit power at the k-th IoT node p_k^* as

$$p_k^* = \left[\frac{\left(w_k + \theta_k\right)B}{\varpi_k \ln 2} - \frac{B\sigma^2}{h_k}\right]^+, \forall k.$$
 (C.5)

In order to achieve the closed-form expression of the optimal local computation frequency at the k-th IoT node, we take the partial derivative of \mathcal{L} regarding to f_k and obtain

$$\frac{\partial \mathcal{L}}{\partial f_k} = \frac{(w_k + \theta_k) T}{C_{\text{cpu},k}} - 3\varpi_k \varepsilon_k T f_k^2 - \phi_k.$$
(C.6)

Letting $\frac{\partial \mathcal{L}}{\partial f_k} = 0$, we can calculate the optimal local computing frequency at the k-th IoT node f_k^* as

$$f_k^* = \sqrt{\frac{(w_k + \theta_k)}{3\varpi_k \varepsilon_k C_{\text{cpu},k}} - \frac{\phi_k}{3\varpi_k \varepsilon_k T}}, \forall k.$$
 (C.7)

Based on (C.4), (C.5) and (C.7), Theorem 1 can be obtained.

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APPENDIX B

As for P_{3a} , C3, C4, C6 – 1 and C7 – 1 are linear constraints and whether P_{3a} is convex or not depends on the convexity-concavity of the objective function and constraints C1-2 and C2-2. That is, when the objective function is concave and both C1-2 and C2-2 are convex, P_{3a} is proved to be convex.

1) The concavity of the objective function: It can be observed that the objective function is concave if and only if function $f(x, y) = x \log_2 \left(1 + \frac{y}{x}\right)$ is concave jointly regarding to x and y. Based on the fact that the perspective function can preserve convexity, it can be found that the convexity of f(x,y) is the same as that of function $\log_2(1+y)$ which is easily proved to be concave. Therefore, f(x, y) is also a concave function, resulting in a concave objective function.

2) The convexities of constraints C1 - 2 and C2 - 2: As for C1 - 2, its left side is a concave function and its right side is a constant. Thus, C1 - 2 is a convex constraint.

As for C2 - 2, its right side is a linear function while the convexity-concavity of its left side depends on that of function $f_1(x) = x^3$ with $x \ge 0$. Since $f_1(x) = x^3$ with $x \ge 0$ can be easily proved to be convex, C2 - 2 is also a convex constraint.

Based on the above analyses, P_{3a} can be proved to be convex.

APPENDIX C

Let $\boldsymbol{\theta} = (\theta_1, \theta_2, \dots, \theta_K), \boldsymbol{\varpi} = (\varpi_0, \varpi_1, \varpi_2, \dots, \varpi_K), \boldsymbol{\phi} = (\phi_1, \phi_2, \dots, \phi_K), \boldsymbol{\mu} = (\mu_0, \mu_1, \dots, \mu_N), \text{ and } \boldsymbol{\varphi} =$ $\varphi_{1,1} \cdots \varphi_{1,K}$ $\vdots \cdots \vdots$ $\varphi_{N,1} \cdots \varphi_{N,K}$ express the non-negative Lagrange

multipliers regarding to all the constraints for P_{3a} . Then the Lagrangian function of P_{3a} can be written as (C.1), as shown at the top of this page.

On this basis, we can take the partial derivatives of \mathcal{L} with respect to $x_{n,k}$ and P_k , as an effort to achieve the expressions for the optimal power reflection coefficient in the n-th time

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