

Original citation:

Hildebrandt, Torsten and Branke, Juergen (2014) On using surrogates with genetic programming. Working Paper. Coventry, UK: University of Warwick, WBS.

Permanent WRAP url:

<http://wrap.warwick.ac.uk/60025>

Copyright and reuse:

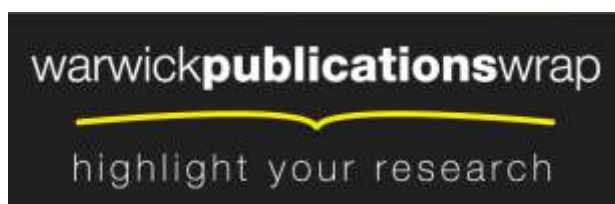
The Warwick Research Archive Portal (WRAP) makes this work by researchers of the University of Warwick available open access under the following conditions. Copyright © and all moral rights to the version of the paper presented here belong to the individual author(s) and/or other copyright owners. To the extent reasonable and practicable the material made available in WRAP has been checked for eligibility before being made available.

Copies of full items can be used for personal research or study, educational, or not-for-profit purposes without prior permission or charge. Provided that the authors, title and full bibliographic details are credited, a hyperlink and/or URL is given for the original metadata page and the content is not changed in any way.

A note on versions:

The version presented here is a working paper or pre-print that may be later published elsewhere. If a published version is known of, the above WRAP url will contain details on finding it.

For more information, please contact the WRAP Team at: publications@warwick.ac.uk



<http://wrap.warwick.ac.uk>

On Using Surrogates with Genetic Programming

Torsten Hildebrandt

hil@biba.uni-bremen.de

Bremer Institut für Produktion und Logistik - BIBA an der Universität Bremen,
Bremen, Germany

Jürgen Branke

Juergen.Branke@wbs.ac.uk

Warwick Business School, University of Warwick, CV4 7AL Coventry, UK

Abstract

One way to accelerate evolutionary algorithms with expensive fitness evaluations is to combine them with surrogate models. Surrogate models are efficiently computable approximations of the fitness function, derived by means of statistical or machine learning techniques from samples of fully evaluated solutions. But these models usually require a numerical representation, and therefore can not be used with the tree representation of Genetic Programming (GP). In this paper, we present a new way to use surrogate models with GP. Rather than using the genotype directly as input to the surrogate model, we propose using a phenotypic characterization. This phenotypic characterization can be computed efficiently and allows us to define approximate measures of equivalence and similarity. Using a stochastic, dynamic job shop scenario as an example of simulation-based GP with an expensive fitness evaluation, we show how these ideas can be used to construct surrogate models and improve the convergence speed and solution quality of GP.

Keywords

Genetic Programming, surrogates, phenotypic characterization.

1 Introduction

For many practical applications, the most time consuming part of Evolutionary Algorithms (EAs) is the fitness evaluation. For example in engineering design, evaluating a single solution may take several hours. In order to speed up the execution of EAs with expensive fitness evaluations, integrating surrogate functions attracted much research (Jin, 2005, 2011). The basic idea here is to minimize the number of expensive fitness evaluations by replacing them with a computationally cheaper function as far as possible. To learn such surrogate functions¹ from a sample of fully evaluated solutions, various statistical or machine learning techniques can be used. These models usually assume a numerical representation of the solutions, as they require a measure of "distance" or "similarity" between solutions. Because the genotype in GP is a tree structure, it is not straightforward to use surrogate models with GP.

¹Sometimes surrogate functions are also called meta-models or response surface models

In this paper, we present an approach that allows surrogate models to be used with GP. Rather than trying to learn an approximate function that maps the genotype (i.e., a GP tree) into the fitness, we introduce the concept of a phenotypic characterization of a solution. This phenotypic characterization tries to capture the *behavior* of the phenotype encoded in the GP tree, and represents it as a vector of numerical values, which then allows calculating distances among individuals as required by the surrogate models. We show how this idea can be used to remove duplicates and reduce the number of necessary expensive fitness evaluations, thus generating better results more quickly. Our approach thus makes GP more efficient when applied to problems with expensive fitness evaluation, and opens up the possibility of using GP also on problems which previously have been computationally too demanding.

The exact phenotypic characterization is problem specific. However, the general idea is generic and should be applicable across application domains. To demonstrate the usefulness of our proposal, we use the task of evolving dispatching rules for shop scheduling as an example of GP with expensive fitness evaluation.

This paper is structured as follows. After reviewing related work in Section 2 we describe our application area in Section 3. In Section 4, we introduce the concept of a phenotypic characterization, present such a characterization for dispatching rules, and describe its use to establish (approximate) phenotypic equivalence and similarity between GP trees encoding dispatching rules. Section 5 presents our experimental setup. The results presented in Section 6 demonstrate the usefulness of the introduced concepts to improve the convergence of GP by

1. detecting and suppressing phenotypic duplicates
2. supplementing GP with a surrogate function that uses approximate phenotypic similarity between individuals.

We analyze what data to base the phenotypic characterization on, and compare the performance of a *genotypic* similarity measure for GP trees with the *phenotypic* similarity introduced in this paper. We conclude with a summary and outlook towards future work.

2 Related Work

The use of approximate but cheap to evaluate learned surrogate models to speed up evolutionary algorithms on problems with expensive fitness functions has been proposed many years ago (e.g., Rattle (1998)) and meanwhile is an established research area. In the following, we briefly discuss some of the most relevant papers. For a more comprehensive review, the interested reader is referred to, e.g., Jin (2005, 2011); Shi and Rasheed (2010); Jin and Branke (2005).

The surrogate model is usually learned from samples of expensive evaluations. Popular choices for surrogate models include Neural Networks (Hong et al., 2003), regression techniques (linear or polynomial) (Oduguwa and Roy, 2002; Branke and Schmidt, 2003), nearest neighbor interpolation (Runarsson, 2004) or Gaussian Processes (El-Beltagy et al., 1999). Recently, also approaches were proposed that combine different models (possibly using different techniques) or select the most promising model(s) depending on the current situation (see, e.g., Goel et al. (2007); Lim et al. (2007)). The

data used to learn the surrogate model can come from an experimental design conducted before the EA, but usually is learned and adopted online during the run (Jin, 2005, 2011; Jin and Branke, 2005).

Surrogate models can be used to support EAs in several ways. Most often, all individuals are evaluated with the surrogate model, and this information is used to pre-select the most promising individuals that are then evaluated with the expensive fitness function (Jin et al., 2002). That way, individuals classified as poor by the surrogate model can be quickly discarded, while the better individuals are fully evaluated to allow an accurate ranking. Furthermore, the full evaluation of these individuals are used to further refine the surrogate model particularly in the most promising areas. Others have proposed to alternate between generations that are evaluated with the surrogate model and generations that are evaluated using the expensive fitness function (Rattle, 1998; Jin et al., 2002), to use surrogate models for supporting local search (Lim et al., 2010), or for pre-selection amongst individuals generated by a genetic operator (Emmerich et al., 2002).

However, so far, successful use of surrogates to speed up EAs has been restricted to fixed-length representations for which it was easy to define a distance metric (e.g., bit-strings or vector of real values). GP, on the other hand, usually uses a tree representation of variable length. Machine learning or statistical techniques can not be used directly to work with such genotypes or phenotypes, which probably is the reason why, to the best of our knowledge, no other work using surrogate functions with GP is reported in the literature. In this paper we overcome these difficulties by using an (approximate) phenotypic characterization of the individual. As it is a vector consisting of integer values, we can then apply standard techniques from the surrogate literature to estimate the fitness value of a GP individual without performing an expensive fitness evaluation.

A few papers in the GP area area related to our idea of phenotypic representation in the sense that they propose considering the behavior of solutions in GP rather than just the genotype. So far, however, this idea has not been used to construct surrogate models.

Gustafson (2004) indicates that there is a positive correlation between diversity and performance achieved by GP for many problems, and consequently high diversity is considered beneficial. A typical approach to maintaining diversity is fitness sharing. It forces similar individuals to share their fitness values, and thereby discourages the formation of clusters of very similar individuals. This requires a similarity metric. While similarity between GP trees is usually calculated using syntactic similarity (Ekárt and Németh, 2000), recent research by Nguyen et al. (2012) aims at incorporating "Sampling Semantics" to form clusters sharing their fitnesses. This "Sampling Semantics" is in some respects similar to our phenotypic characterization. Jackson (2011) modified GP eliminating candidate solutions with duplicate objective function values in the initial population as well as during the GP run and reported improved performance. Detecting such duplicates by comparing objective values is quite costly in a simulation-optimization context as ours, as full simulation runs are required to obtain objective function values. The amount of duplicates can be reduced to a large extent without additional simulations, however. Branke et al. (2013) used a simplified version of the phenotypic characterization to cheaply compute approximate phenotypic equivalence between trees and could demonstrate its usefulness to improve convergence speed and

solution quality of standard GP. Here we further analyze this approach and extend it to create surrogate functions to improve the convergence of GP. As an extreme option to diversity preservation, Lehman and Stanley (2010) propose focusing on novelty instead of the objective function value when selecting individuals, and again use the phenotypic behavior to determine novelty.

In Uy et al. (2011) the authors use the above mentioned Sampling Semantic Distance in order to define tree similarity and use it in an improved crossover operator to enforce crossover between subtrees in a certain similarity range. They report improved results on a number of symbolic regression problems.

Finally, Ashlock and Lee (2013) recently proposed the concept of "agent-case embedding" that is closely related to our concept of phenotypic characterization and is used for analyzing evolved systems.

3 Evolving Dispatching Rules

The application we consider in this paper as an example is the problem of evolving dispatching rules for dynamic job shop scheduling problems. A dispatching rule is a simple heuristic that computes a priority value for a job from its attributes (Haupt, 1989; Blackstone et al., 1982; Holthaus and Rajendran, 1997; Rajendran and Holthaus, 1999). Whenever a machine becomes idle and has waiting operations in its queue, the job with the highest priority value is chosen to be processed next. Benefits of dispatching rules include their simple and intuitive nature, their ease of implementation within practical settings, and their flexibility to incorporate domain knowledge and expertise. They are very well suited for online scheduling, as they automatically take into account the latest information available. All these factors have led to their frequent use in various industries including semiconductor manufacturing (Pfund et al., 2006).

Usually, dispatching rules are designed by experts in a tedious trial-and-error process, with candidate rules being tested in a simulation environment, modified and re-tested until they fulfill the requirements for actual implementation in practice (Geiger et al., 2006). In recent years, several authors have suggested to automatically design suitable dispatching rules by means of EAs, see for example Geiger et al. (2006); Dimopoulos and Zalzala (2001); Pickardt et al. (2013, 2010); Nguyen et al. (2013b,a). Most of these approaches use Genetic Programming (Koza, 1992; Poli et al., 2008) and can be classified as applications of hyper-heuristic search (Burke et al., 2009, 2010). As such their search space is the space of heuristics instead of a concrete solution of a problem instance.

In terms of the set of terminals and non-terminals, finding a dispatching rule is similar to symbolic regression, a standard GP benchmark problem. A GP individual encodes an arithmetic expression, a function of several variables. In case of a dispatching rule, the GP individual encodes a function $p : \mathbb{R}^a \rightarrow \mathbb{R}$ mapping a vector of a attributes describing a job, machine, or the whole system to a priority value. Fitness evaluation is far more complex, however, and usually involves running multiple replications of a stochastic, dynamic shop floor simulation. The time required for just a single fitness evaluation therefore by far exceeds the computational time required by the core GP algorithm.

In recent years, GP was used to successfully develop improved dispatching rules

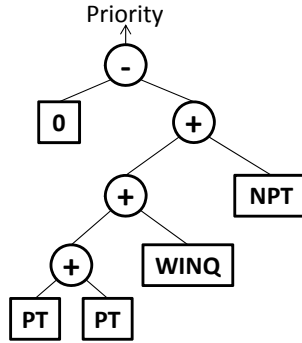


Figure 1: GP tree representation of the Holthaus rule $-(2PT + WINQ + NPT)$ (Holthaus and Rajendran, 2000), where PT, WINQ and NPT denote processing time, work in next queue, and processing time at the next machine, respectively.

for various scheduling problems ranging from single machine problems (e.g., Geiger et al. (2006)), classic static job shop scheduling problems (Nguyen et al., 2013b), to dynamic job shop scheduling problems (e.g., Hildebrandt et al. (2010)). Recently also dispatching rules for a complex dynamic scenario from semiconductor manufacturing were evolved using GP (Pickardt et al. (2013, 2010)). This scenario consists of 36 machines, sequence dependent setup times, parallel machines, batch machines and reentrant process flows with jobs consisting of up to 92 operations. Rules developed by GP for this scenario clearly outperformed standard dispatching rules from the literature. To use GP in such a setting is computationally very demanding. The method presented in this paper is one step towards an increased scalability of GP to even larger practical scenarios requiring even longer simulation times.

In terms of the scheduling scenario considered we take one step back in this paper by considering a dynamic job shop scenario with 10 machines proposed by Rajendran and Holthaus (1999) and described in more detail in Section 5.1. Using this scenario (taking about 0.6s per fitness evaluation) seems complex enough to justify the use of a surrogate model, but still keeps computational times low enough to be able to investigate a variety of different parameter settings and perform each experiment a number of times to obtain statistically valid results on mean performance, etc.

A good benchmark rule for minimizing flow time in this scenario is the rule manually developed by Holthaus and Rajendran (2000) in a follow-up paper to Rajendran and Holthaus (1999). In this rule, the priority of a job is calculated as $-(2PT + WINQ + NPT)$, and is thus a linear combination of the current processing time (PT), work content in next queue (WINQ), and the processing time of a job's next operation (NPT—Next Processing Time). In the following, we call this rule the *Holthaus rule* and use it as reference rule throughout the paper. An example of a GP expression tree for the Holthaus rule is depicted in Figure 1.

4 Approach

4.1 Overview

Before presenting in detail how to compute the phenotypic characterization and how to use it to define (approximate) equivalence and similarity, we show in this section how they are embedded in the overall solution procedure. Figure 2 depicts the general outline of an optimization run. The general procedure is based on a generational reproduction scheme, as used for instance in conventional GP. In Figure 2 standard steps are shown as white boxes, additional steps related to the use of surrogates and detection/removal of phenotypic duplicates are shown as grey boxes. Each iteration of the main loop (steps 3 to 9) constitutes one generation.

We start with a population P of rules/individuals (step 1). These initial rules are usually randomly generated using some initialization procedure. In step 2 we remove duplicate rules using the procedure described in Section 4.3 and replace them with additional random rules until our population consists of the required number of different rules.

All candidate rules in P are subsequently fully evaluated in a simulation in step 3. As already mentioned, this is by far the most time-consuming step in the overall procedure. Once real fitness values are known, we check whether the optimization run should be terminated or continue with another iteration. If we decide to terminate, the best rule found so far is reported as the result of the optimization run. Otherwise, we update our surrogate model to incorporate the new fitness values of all individuals in P (step 4).

In the next step (step 5), conventional GP operators (see Koza (1992); Poli et al. (2008)) for selection, mutation, and crossover are used to produce a new, intermediate population P_{imd} taking into account all individuals in P and their fitness values. Tree mutation works by replacing a node of the tree by a new, randomly created subtree. Tree crossover takes two parent trees and produces two offspring trees by exchanging a randomly selected sub-tree between the two parents.

Duplicates in P_{imd} are subsequently removed in step 6 and replaced with additional individuals generated from P in the same way as in step 5. At this stage we have a set of individuals which produce with a very high probability distinct (as will be examined in Figure 4a) fitness values.

In conventional GP, both P and P_{imd} contain the same number of individuals. As we want to use the surrogate model to select the most promising individuals later on, we have to create more rules in this step, i.e., $|P_{\text{imd}}| = n|P|$ with $n > 1$. In the experimental section of this paper, we investigate different values of n . Setting n too low will result in only minor improvements over standard GP, setting it too large may have negative consequences on convergence, because inaccuracies of the surrogate function may have a lot of impact and misguide the GP.

In the next step (step 7), we determine the phenotypic characterization for all rules in P_{imd} following the procedure explained in the next section. This is used to approximate the fitness values for all individuals using the surrogate model in step 8. Computing the phenotypic characterization of a rule and evaluating the surrogate for it once is computationally far less demanding than a full fitness evaluation.

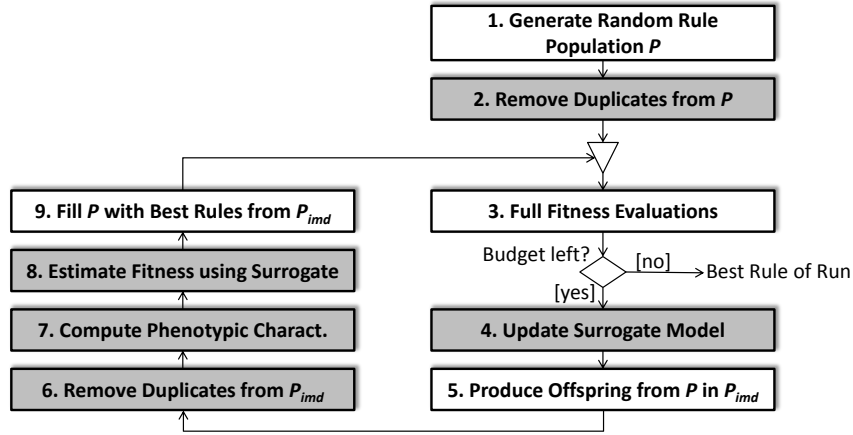


Figure 2: General solution approach. Components of standard GP are shown as white boxes. Additional steps related to the use of surrogates and detection/removal of phenotypic duplicates are shown as grey boxes.

decision situation	attribute set s			ranking by reference rule	ranking by other rule	decision vector d
	s_1	s_2	s_3			
1	3	4	8	1	2	
1	7	6	15	2	1	2
2	23	17	1	2	2	
2	8	9	3	3	1	3
2	6	4	6	1	3	
⋮	⋮	⋮	⋮	⋮	⋮	⋮
k	7	3	9	2	2	
k	4	8	6	1	1	1

(a)

	d_1	d_2	...	d_k	fitness
rule ₁ :	2	3	...	1	1456
rule ₂ :	1	2	...	2	1123
⋮	⋮	⋮	⋮	⋮	⋮
rule _m :	1	3	...	1	1293

(b)

Figure 3: Phenotypic characterization of dispatching rules. (a) creation of a decision vector for a certain rule given a set of k decision situations. (b) database of m rules, their decision vectors and fitness values.

As a next step (step 9), estimated fitnesses are used to select the most promising candidates to form a new population P for the next iteration. Step 3 starts a new iteration of the main optimization loop again fully evaluating each individual in P using the expensive fitness function.

4.2 Phenotypic Characterization of Dispatching Rules

The key to using a surrogate model with GP is to come up with a meaningful distance metric. Because this is difficult on the genotype level (trees), in the following we propose a phenotypic characterization. The phenotypic characterization looks at the *behavior* of the evolved rules, rather than their syntactic description. This is naturally problem-dependent. In the following, we develop a phenotypic characterization for evolving dispatching rules in job shop scheduling. However, similar phenotypic characterizations can also be developed for other problem domains, and Ashlock and Lee (2013) may serve as additional inspiration.

Dispatching rules define an ordering relation among jobs. Each time a machine

is free and there are jobs waiting, the rule is used to sequence all jobs by their priority, and the job with highest priority is processed next. The key characteristic of dispatching rules is not the functional values they compute, but only to which of a set of jobs they assign the highest priority.

Consequently, the phenotypic characterization for dispatching rules we propose here is a decision vector, a record of all the decisions a dispatching rule takes in a comparably small number of k decision situations, as outlined in Figure 3. These decision situations could be sampled from an actual simulation run, or simply be created randomly. This later aspect is analyzed in more depth in Section 6.2.

The rule to be characterized is used to rank all jobs in each decision situation to find out which job is given the highest priority in each situation (rank 1). A certain fixed reference rule is also used to rank jobs in each decision situation. The decision vector d to characterize a rule R consists of, for each decision situation, the rank the reference rule assigned to the job receiving top priority by rule R . Consider the example in Figure 3(a). In the first decision situation, there are two jobs to choose from. Rule R gave the highest priority (rank 1) to the second job. This job was ranked second by the reference rule, so $d_1 = 2$. Similarly, in the second decision situation, rule R gives the first rank to the second of three jobs, which has been ranked third by the reference rule, thus $d_2 = 3$. For decision situation k , rule R prioritizes the second job, which is in concordance with the reference rule, and thus $d_k = 1$. In summary, d consists of k integer values expressing the similarity of R to the reference rule. A rule leading to the same decisions as the reference rule has all elements of the vector set to 1. A rule which always selects the job that has the lowest priority according to the reference rule has all elements set to the highest possible values, i.e., the number of jobs in the corresponding decision situation (note that this means the maximal error a rule can make depends on the number of jobs in a particular decision situation, and may be different for different situations).

This definition completely abstracts from the actual priority values produced by a rule. Therefore also syntactically quite distinct rules (such as "1/PT" vs. "-PT" as two possibilities to express the well-known rule "shortest processing time first") would be recognized as being equivalent.

Obviously, the computational effort to compute the phenotypic characterization is much less than running a full, expensive fitness-evaluation, which would involve tens of thousands of such decisions.

4.3 Approximate Phenotypic Equivalence and Similarity

We use the phenotypic characterization to build a surrogate function that can help us estimate the fitness value of new individuals at much lower computational cost than the full evaluation via simulation. The surrogate function takes the phenotypic characterization (i.e., the decision vector d in our case) as input, and provides the estimated fitness as output. Constructing the surrogate function from a given set of input-output pairs (see Figure 3b) is a typical machine learning or regression task, and standard techniques such as Neural Networks, Gaussian Processes or Regression Trees could be used.

In this paper, we use the simplest possible regression model, the nearest neighbor regression. To predict the fitness of a new individual, simply the distances to all

individuals in the database are computed using the Euclidean distance between phenotypic characterizations. The fitness of the most similar individual is returned as the fitness estimate for the new individual.

To detect and remove phenotypically identical rules we could use identical decision vectors as a criterion. For this task an even simpler criterion turned out to be sufficient, however: We only consider a single decision situation consisting of 100 jobs. Values of the attribute set are created randomly within typical value ranges but not taking into account any dependencies or correlations between the attributes. Two rules are considered identical, if they produce the same rank vector for these 100 jobs.

5 Experimental Setup

5.1 Shop Floor Scenario

Our computational experiments use the dynamic job shop-scenarios from Rajendran and Holthaus (1999) and try to find good dispatching rules for these scenarios automatically. In total there are 10 machines on the shop floor, each job entering the system is assigned a random routing, i.e., machine visitation order is random with no machine being revisited. Processing times are drawn from a uniform discrete distribution ranging from 1 to 49 minutes. Job arrival is a Poisson process, i.e., inter-arrival times are exponentially distributed. The mean of this distribution is chosen to reach a desired utilization level on all machines. All experiments in this paper use a (mean) utilization of 95%. These scenarios were also used to evolve dispatching rules in Branke et al. (2013) and Hildebrandt et al. (2010).

Following the procedure from Rajendran and Holthaus (1999), we start with an empty shop and simulate the system until the first 2500 jobs have been completed. Data on the first 500 jobs is discarded to focus on the shop's steady state-behavior. The objective function is to minimize the mean flowtime, i.e., the arithmetic mean of the flowtimes of jobs 501 to 2500: $FT = \frac{1}{2000} \sum_{j=501}^{2500} (C_j - r_j)$, where C_j is the completion time of a job j and r_j is its arrival time.

Because the simulation is stochastic, also the calculated flowtime is a stochastic variable. To reduce the impact of stochasticity, we replicate each simulation 10 times for each fitness evaluation and use the average performance for optimization. Furthermore, we use the same 10 random number seeds to evaluate all solutions during optimization (common random numbers, (Law, 2007)). All results reported in this paper are based on evaluating the resulting rules on a *different* set of 100 independent test runs. The simulation has been implemented in Java, and is publicly available (Hildebrandt, 2012).

Most of the experiments described below use as reference dispatching rule the manually developed *Holthaus rule* (Holthaus and Rajendran, 2000) described in Section 3. This rule has been shown to perform very well for the objective of minimizing mean flow time.

Table 1: GP parameters used

Name	Value
Computational Budget	30,000 simulations (60 generations)
Population Size	500
Crossover Proportion	90 %
Mutation Proportion	10 %
Elitism	10
Selection Method	Tournament Selection (size 7)
Creation Type	Ramped Half-and-Half (Min. Depth 2, Max. Depth 6)
Max. Depth for Crossover Operators	17 +, -, *, /, max, if-then-else
Terminals	0, 1, 7 attributes (see Table 2)

Table 2: Information available to be used in dispatching rules (terminal set).

Attribute	Norm. Range	Explanation
PT	[1, 47]	Processing Time of Current Operation
NPT	[0, 47]	Next Processing Time, i.e., Processing Time of Next Operation
WINQ	[0, 410]	Work In Next Queue, i.e., Sum of Processing Times of All Jobs at the Next Machine
RemProcTime	[1, 264]	Remaining Processing Time, i.e., Sum of Processing Times of All Unfinished Operations
OpsLeft	[1, 10]	Operations Left, i.e., Number of all Unfinished Operations
TimeInQueue	[0, 1500]	Time Since Arrival in Current Queue
TimeInSystem	[0, 2770]	Time Since Arrival in System

5.2 Genetic Programming

For our experiments we used the Genetic Programming implementation of the Evolutionary Computation in Java (ECJ)-framework². Details of the parameters used are shown in Tables 1 and 2. This choice of parameters and terminal set resembles the best settings identified for the tree representation in Branke et al. (2013), where we could also identify normalization of input attributes in a common value range of [0, 2] to improve GP performance. We therefore also use these settings for the experiments reported in this paper. Unless mentioned otherwise, convergence curves in this paper are based on 100 independent runs.

²version 20, available from <http://cs.gmu.edu/~eclab/projects/ecj/>, last accessed 2013-01-29

5.3 Surrogate Function

We use a Nearest Neighbor Learner as a modeling technique. The Nearest Neighbor surrogate model uses the full fitness evaluations of the last two generations, i.e., 1000 fully evaluated individuals are used to predict the fitness of new individuals. To predict the fitness of a new individual, the distances to all the 1000 individuals in the database are computed using the genotypic (syntactic) or phenotypic distance measures as described below. The fitness of the most similar individual is returned as the fitness estimate for the new individual.

As mentioned in the previous sections, it is very difficult to use surrogate functions for GP’s tree representation, as popular surrogate modeling techniques such as Neural Networks or Polynomial Regression can only learn functional relationships between real- or integer-valued vectors and a fitness value. In order to use a Nearest Neighbor learner, however, we only have to specify a distance measure between solutions. We can therefore use this learning method to compare surrogates based not only on the phenotypic characterization proposed above in Section 4.2, but also based on a genotypic distance metric from the literature.

More formally, for our phenotypic characterization, the distance D between two decision vectors \tilde{d} and \hat{d} with n dimensions is computed as

$$D(\tilde{d}, \hat{d}) = \sqrt{\sum_{i=1}^n (\tilde{d}_i - \hat{d}_i)^2}.$$

Genotypic similarity between expression trees is computed using the Structural Hamming Distance (SHD), which was presented in Moraglio and Poli (2005) to create an improved crossover operator.

$$\text{SHD}(T_1, T_2) = \begin{cases} 1 & \text{if } \text{arity}(p) \neq \text{arity}(q) \\ hd(p, q) & \text{if } \text{arity}(p) = \text{arity}(q) = 0 \\ \frac{1}{m+1} (hd(p, q) + \sum_{i=1}^m \text{SHD}(s_i, t_i)) & \text{if } \text{arity}(p) = \text{arity}(q) = m \end{cases}$$

It defines a syntactic distance measure between trees ranging from 0 (trees are equal) to a maximum distance of 1. In this formula T_1 and T_2 are trees, p and q are their root nodes and s_i as well as t_i denote the i th subtree of p and q respectively. The utility function $\text{arity}(p)$ computes the number of a node’s subtrees. $hd(p, q)$ computes the Hamming distance between p and q , which is 0 if $p = q$, i.e., p and q represent the same type of terminal or non-terminal node, or 1 otherwise.

6 Results

6.1 Duplicate Detection and Removal

First, we look at the benefit of duplicate avoidance based on phenotypic characterization. As explained in Section 4.3, this is using the simplified phenotypic characterization based on the ranking of 100 artificial “jobs”. Based on this approximate equiva-

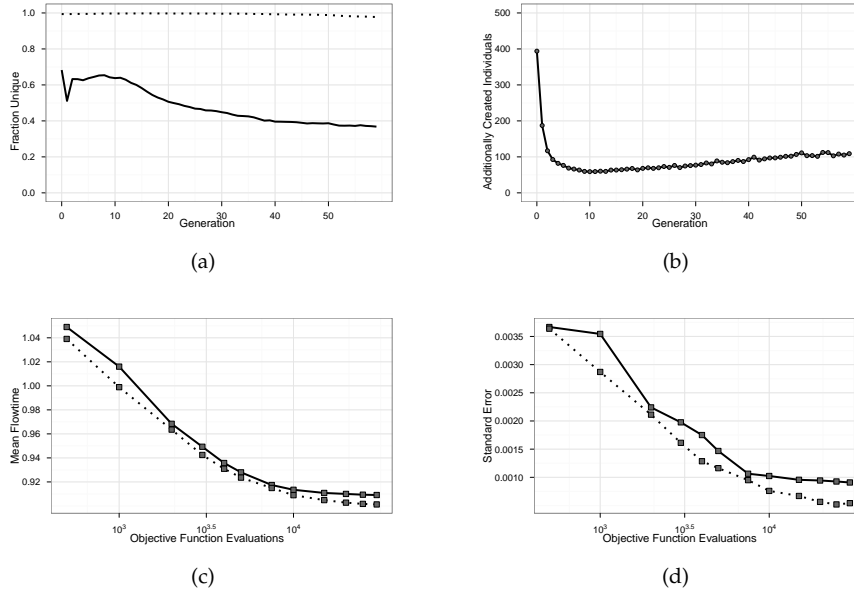


Figure 4: Figure 4a shows the fraction of individuals with unique fitness values for Standard GP (solid line) and when using (approximate) duplicate detection (dotted line). The number of additional individuals required to increase diversity is shown in Figure 4b (population size is 500). Mean performance (4c) and standard error (4d) of GP runs with (dotted lines) and without (solid lines) suppression of duplicates based on (approximate) phenotypic equivalence. Performances are relative to the mean flowtime achieved by the Holthaus rule and averaged over 100 runs.

lence we eliminate all duplicate rules in a population before running any simulations to assess rule performances. These rules are replaced with new rules either created randomly (initial population), or, later on in a GP run, by using the mutation/crossover operators.

As shown by the dotted line in Figure 4a, this duplicate avoidance scheme is quite successful at maintaining a high level of diversity (measured in the number of individuals with distinct fitness values). Standard GP (solid line) starts with a considerably lower diversity, and depicts a further decreasing diversity after generation 13. The number of individuals created additionally to replace duplicates is shown in Figure 4b. Interestingly, especially for the initial population and the first few generations, the number of additionally created individuals is rather high, before dropping to a level of around 60 additional individuals per generation. From around generation 10 this number is increasing again with a linear trend. This is consistent with the behavior of standard GP: from about generation 10-13 it seems to become increasingly difficult for GP to find new, fitness-distinct individuals, therefore more individuals have to be created to compensate.

An increase in fitness diversity alone does not necessarily lead to good performance. Genotypically different individuals with the same fitness might represent different ways to express a certain dispatching rule, and preserving this information might

be beneficial for the evolutionary process. However, a look at the convergence lines in Figure 4c shows a clear advantage of removing fitness duplicates: Both, convergence speed and final solution quality, improve. Also the standard error and therefore standard deviation of run performance decreases (see Figure 4d), leading to more reliable optimization results. We can therefore conclude that at least in the considered application, removing phenotypically equivalent rules allows finding better solutions more quickly.

Summarizing, without using any additional expensive simulation runs, and with very low additional computational cost, we can almost entirely remove fitness duplicates, allowing a faster convergence to a better performance level.

6.2 Choosing a Set of Decision Situations

The phenotypic characterization of a dispatching rule (Section 4.2) depends on the rule's behaviour on a set of decision situations. Obviously, the set of decision situations selected has an impact on the quality of the resulting surrogate model, and the question arises how to create this set. For example, it could be created randomly, or by sampling real situations encountered in a simulation. To examine the influence of different ways to choose the set of decision situations, we analyze the ranking performance of the resulting surrogate models, based on the individuals of 30 GP runs (with suppression of duplicates but not using a surrogate function). Data of all individuals created is recorded and used to learn surrogate models from three different sets of decision situations; in all cases a set consists of 100 situations:

- *Random*: Decision situations are created randomly containing between 2 and 20 "jobs". Similar to the technique to detect duplicates for each of these "jobs" random values are created for each of the attributes within the ranges listed in Table 2 using a uniform continuous distribution. This approach assumes all attributes to be independent. It is pretty simple as it only depends on knowing typical value ranges of the attributes, no additional simulation runs are required.
- *Reference rule*: Decision situations are sampled from preliminary simulation runs using the Holthaus rule. From all real decision situations encountered in such a simulation, a sub-set of 100 situations is sampled.
- *Optimized rule*: As optimization progresses and decisions of optimized rules get increasingly different, situation characteristics might change. Thus, it might be advantageous to change decision situations during an optimization run. To quantify this effect we used the best rules from 30 GP runs to sample decision situations, anticipating the situations encountered by rules at the end of an optimization run. Obviously, this would not be feasible in practice, but may serve as an indication for the performance when the set of decision situations is adapted dynamically to always reflect the best solution found so far.

We created 30 different random sets of decision situations and also sampled 30 different sets using the Holthaus rule. To assess the influence of optimized rules we used the best rule from each of the 30 recorded runs and sample a single set of decision situations with each one of them. Thus, for each setting we tested 30 different sets of decision situations to base the decision vector on. Using the Nearest Neighbor learner

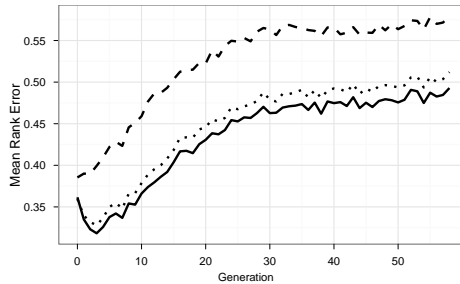


Figure 5: Choice of decision situations for phenotypic characterization: dashed line: random decision situations; dotted line: decision situations sampled with reference rule; solid line: decision situations sampled with optimized rules. All lines show the mean rank error, normalized to the expected error of random selection.

with Euclidean distance as a similarity measure, we created surrogate models using the phenotypic characterization based on each set of decision situations.

The quality of a surrogate model is judged as its ability to produce the same ranking that would result from the expensive fitness evaluations, which seemed the most relevant aspect given that we are using a rank-based selection scheme. We measure this by looking at the mean rank error of the predictions, normalized to the expected rank error of a random ordering of the individuals. The best possible error of 0 would mean the surrogate can produce a perfect ranking. In this case, the computationally expensive simulation runs could be replaced with the surrogate without any impact on GP performance. In the other extreme, a model with quality 1 is not better than using a random permutation of individuals. For a more detailed discussion of appropriate measures of surrogate quality see Jin et al. (2003).

Results in Figure 5 show the surrogate’s quality when using the individuals (and their fitness) from a certain generation as training data to predict the performance of the individuals of the next generation. For each graph in Figure 5, we tested each of the 30 different sets of decision situations with each of the 30 recorded runs.

The curves in Figure 5 show surrogate evaluation to be most accurate in the first few generations, probably because there is a high diversity in early generations, which makes it easier to distinguish between good and bad solutions. Surrogate quality decreases afterwards until generation 30, and then mostly stagnates. Comparing the three different settings to create decision situations, we achieve the best results using real decision situations from simulation runs (solid and dotted lines). Surrogates based on decision situations generated with optimized rules (solid) seem slightly better than if the reference rule is used (dotted). But the difference is small compared to using decision situations that have been randomly generated, which performs much worse (dash-dotted line). In the remainder of this paper, we therefore use situations sampled with the reference rule. Changing the set of decision situations dynamically during an optimization run can probably be used to further improve surrogate quality slightly, but is left for future work.

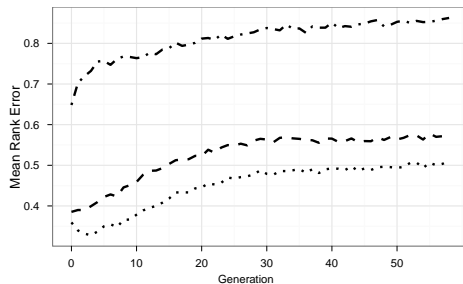


Figure 6: Genotypic vs. phenotypic surrogate. The lines show the (normalized) mean rank error using SHD as a genotypic similarity measure (dash-dot line) vs. approximate phenotypic similarity (dashed line: random decision situations; dotted line: decision situations sampled with reference rule).

6.3 Phenotypic vs. Genotypic Surrogate

The Nearest Neighbor surrogate model used in this paper only requires a distance metric to be applied. In order to demonstrate that the proposed phenotypic characterization allows for much more meaningful distance metric than genotypic distances, in this section we compare the surrogate quality based on our phenotypic characterization with a surrogate model using the genotypic SHD distance measure (Moraglio and Poli, 2005), following the same experimental setup as described in the previous section.

Results are shown in Figure 6 comparing surrogate quality using phenotypic similarity from the previous section (based on random decision situations—dashed line; based on reference rule—dotted line) with genotypic similarity (dash-dot line). Results clearly show a much better performance of the surrogate model based on our phenotypic characterization. Even using random decision situations leads to much better results than the surrogate based on SHD distances. Especially in later generations, the ranking produced by the surrogate model based on SHD distances is only slightly better than simply creating a random permutation of individuals.

6.4 Phenotypic Surrogate for GP

In the previous two sections, surrogates were used to predict performance of GP individuals from recorded GP runs. We now report results from using surrogates dynamically in an actual GP run. Based on the results from the previous sections, we use decision situations sampled from simulations with the reference rule as the basis of the phenotypic characterization and predict rule performance using the Nearest Neighbor learner using Euclidean distance. As mentioned before, we use a pre-selection scheme to improve GP convergence by creating an intermediate population which contains a multiple n of the population size of new individuals. Using the surrogate model based on the phenotypic characterization, the most promising fraction $1/n$ of individuals is selected to form the new population. This new population is fully evaluated using the simulation model. We investigate three different settings for the size of the intermediate population $n = 2, 5, 10$; the setting $n = 1$ does not use the surrogate model but only removal of duplicates.

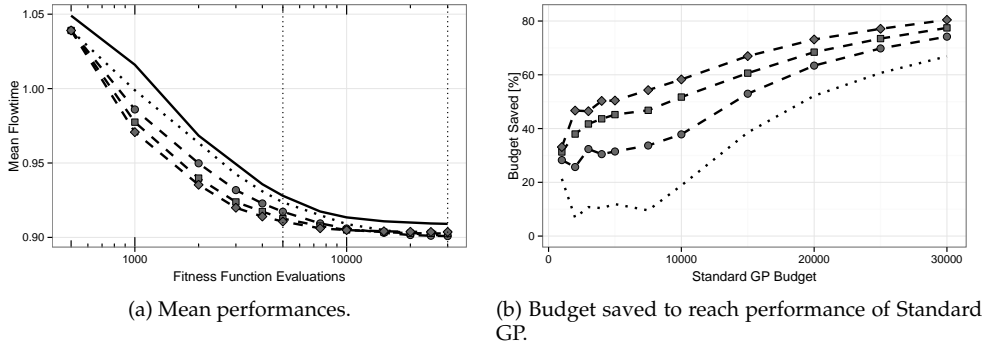
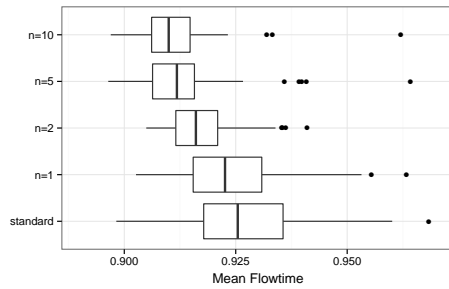


Figure 7: Comparison of Standard GP (solid line), GP with duplicate suppression (i.e., $n=1$; dotted line), and surrogate-supported GP runs (dashed lines). Indicated by the shapes of the dashed lines we investigated three different settings for the number of preselection individuals ($n=2$: circles; $n=5$: squares; $n=10$: diamonds).

Results are given in Figure 7a. The solid and dotted lines show the results of Standard GP and when using duplicate removal (as already presented in Figure 4c). Dashed lines show the convergence lines with surrogates. Different settings of n are indicated by different shapes to mark data points (circle, square, diamond: $n = 2, 5, 10$). As can be seen, using the surrogate model results in faster convergence. Concerning the right size of the intermediate population there is a benefit of using larger values of n . Increasing n shows decreasing returns, however. The value of the surrogate model therefore seems limited, and for larger n the computational effort to create and evaluate (using the surrogate) additional individuals would only lead to marginally faster convergence.

These result are presented in a slightly different form in Figure 7b graphically showing the percentage of fitness evaluations saved while still achieving the performance of standard GP. Data for this graph was obtained by moving a horizontal line in Figure 7a along the solid line, i.e., the convergence curve of standard GP. As an example, after 5,000 fitness evaluations (dotted vertical line next to the center of Figure 7a) standard GP achieves a performance of about 0.93. The same performance levels are achieved by the other variants considerably earlier, resulting in the saved budget values for a standard GP budget of 5,000 as shown in Figure 7b. The final performance level of standard GP after 30,000 fitness evaluations is reached by the surrogate-assisted variants much earlier, resulting in savings of up to 80% of the fitness evaluations. Already GP with removal of duplicates reaches a very good performance level much more quickly. However, there is a clear additional benefit of using the surrogate model.

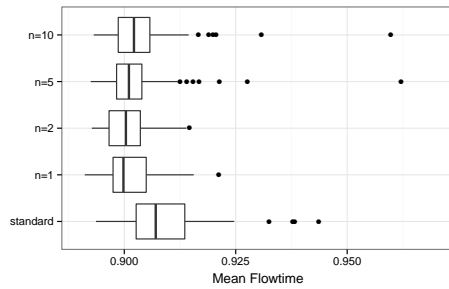
The convergence curves in Figure 7a also show another effect of increasing n : for large computational budgets, solutions without using the surrogate seem to converge to slightly better solutions in the end. To investigate this effect, we further analyzed the situation for a budget of 30,000 fitness evaluations, i.e., at the rightmost data point in Figure 7a. Figure 8c shows a boxplot of run performances for this budget and a detailed comparison of performance differences. The absolute performance differences in Figure 8d show mean performance differences (mean flowtime is measured in minutes) between the settings indicated by the methods in the corresponding row and column.



(a) Run performances after 5,000 fitness evaluations.

	n=1	n=2	n=5	n=10
standard	5.7 (+)	14.0 (++)	20.0 (++)	22.6 (++)
n=1		8.3 (++)	14.3 (++)	16.9 (++)
n=2			6.0 (++)	8.6 (++)
n=5				2.6 (o)

(b) Performance differences after 5,000 fitness evaluations.



(c) Run performances after 30,000 fitness evaluations.

	n=1	n=2	n=5	n=10
standard	10.2 (++)	10.7 (++)	8.5 (++)	7.1 (++)
n=1		0.5 (o)	-1.7 (o)	-3.1 (+)
n=2			-2.2 (o)	-3.6 (++)
n=5				-1.4 (o)

(d) Performance differences after 30,000 fitness evaluations.

Figure 8: Detailed performances after 5,000 and 30,000 fitness evaluations (100 runs each). Figures (a) and (c) show boxplots of run results. Figures (b) and (d) show (absolute) performance differences in minutes and an indication of the statistical significance of these differences (highly significant (99%): "++", significant (95%): "+", not significant: "o"). Significant differences are highlighted in bold. Positive numbers mean that the method listed in the row is worse than the method listed in the column.

For example, a difference of 10.2 between “standard” and “ $n=1$ ” means a worse performance of Standard GP in comparison with the setting of $n=1$ by 10.2 minutes of flow time on average. Indications of statistical significance of these differences are shown in brackets. They are based on a non-parametric, paired Wilcoxon signed-rank test.

As can be seen in Figure 8d, all settings for n dominate the performance of Standard GP. Comparing $n = 1$ with $n = 2$, i.e., using removal of duplicates and duplicate removal with pre-selection with $n = 2$, both lead to about the same performance level (slightly better result of $n = 2$ is not significant). Given the faster convergence, $n = 2$ is a much better choice. Increasing n further accelerates convergence, but performance for large budgets stagnates, performance of $n = 10$ is significantly worse than that of $n = 1$ or $n = 2$. At an intermediate budget of 5,000 fitness evaluations (shown in Figures 8a and 8b) a high setting of n is still beneficial, however increasing n from 5 to 10 results only in a non-significant improvement of performance.

We explain this by the search bias introduced with the surrogate model. As long as there only is a modest influence of the model, convergence is not affected. If the model’s influence is high due to a large n , errors introduced by the model can lead to premature convergence in sub-optimal parts of the search space. Furthermore, given the results of Section 6.3, it seems to be more easy to differentiate between good and bad rules in the first few generations when individuals in the population are very dissimilar with a large variance of fitness values.

When optimizing with expensive fitness functions, detailed convergence lines as shown in Figure 7 will generally not be known in advance. Therefore, given a certain computational budget, a robust setting is required, which combines fast convergence with a good convergence level and low computational overhead. Given these requirements, using the phenotypic surrogate with a moderate setting of $n = 2 \dots 3$ seems to be a good compromise to achieve faster convergence without sacrificing the final convergence level achievable.

6.5 Runtime Considerations

Using Surrogate-Assisted GP as presented in this paper requires additional computational time compared to Standard GP. For each generation, i.e., iteration of the main loop of Figure 2, this overhead consists of:

1. the time to detect duplicates and replace them with additional rules;
2. the time to build or update the surrogate model (in our case only an update of the database);
3. additional time to compute the phenotypic characterization, i.e., in our experiments the decision vector as described in Section 4.2;
4. time to estimate each rule’s fitness by querying the surrogate model using the rule’s phenotypic characterization;
5. time to sort all rules by estimated fitness and copy rules with best estimated fitness to the new population.

Looking at the runtime requirements of Standard GP and Surrogate-Assisted GP (with $n = 2$) in our experiments, both running for 60 generations using 30,000 full fit-

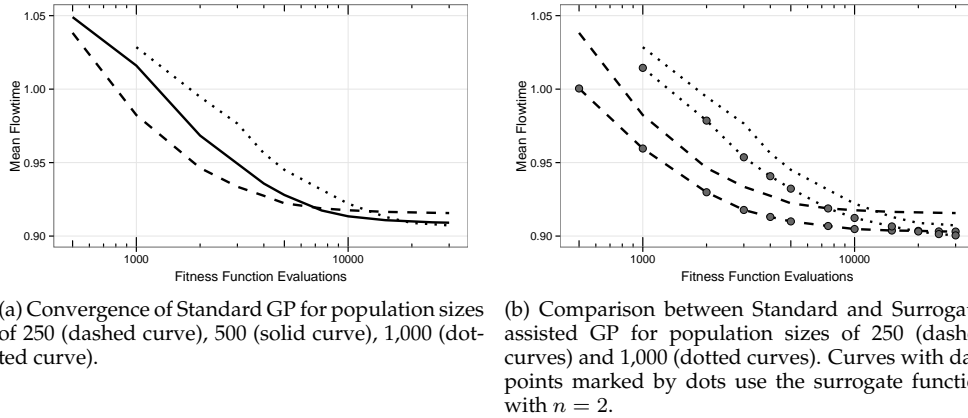


Figure 9: Influence of population size.

ness evaluations, we measured an increase of computational time of 295s (± 18 s based on a 95% confidence interval). This is an increase of less than 1.7% in total CPU time used. In our experiments, a single fitness evaluation takes about 0.6s on average. Our measured runtime difference is therefore equivalent to about 492 (± 30) fitness evaluations in total or 8.2 fitness evaluations per generation. Contrasting this with the corresponding curves in Figure 7 (dashed curve with circles) shows a clear benefit of using the surrogate for the dynamic job shop scheduling scenario used in this paper.

Even more important, this additional runtime requirement for using the surrogate does not depend on the runtime of a single simulation. When using our approach with more complex and realistic simulations taking much longer, the overhead of Surrogate-Assisted GP would soon become negligible and benefits like faster convergence to better performance levels even more important.

6.6 Influence of population size

This paper aims at demonstrating the benefit of integrating into GP a surrogate model based on phenotypic characterization. The relative performance of a GP with and without surrogate model should be mostly independent of the GP parameter settings, as long as they are reasonable. The GP with surrogate model however uses an intermediate population of larger size, so it seems sensible to investigate the influence of the population size.

We therefore report in Figure 9 results of using different population sizes in addition to the standard setting of 500 we used so far in our experiments: a smaller population size of 250 and a larger setting of 1,000. Convergence curves using these three settings for Standard GP are shown in Figure 9a. As can be seen, using a population size of 250 leads to faster convergence for small computational budgets at the expense of worse mean performance for budgets larger than 7,000–8,000. A population size of 1,000 might only be beneficial for very large budgets above 20,000. Even for a budget of 30,000, however, performance differences to a setting of 500 are not statistically significant. Therefore, a population size of 500, as used for the experiments in this paper,

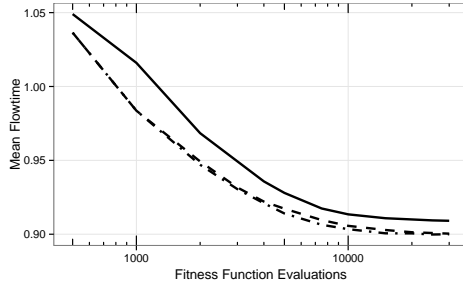


Figure 10: Convergence of Standard GP (solid curve), Surrogate-Assisted GP with $n = 2$ (dashed curve), and Surrogate-Assisted GP using a hypothetical perfect surrogate (dash-dot curve; also using $n = 2$).

seems to be a good compromise for the maximum budget of 30,000 fitness evaluations used.

More important for the findings of this paper is the comparison between Standard GP and Surrogate-assisted GP for population sizes of 250 and 1,000 as shown in Figure 9b. For both settings there is a clear benefit of using the surrogate, resulting in faster convergence as well as convergence to better performance levels. The benefits of using the surrogate model for a population size of 500 were already analyzed in more detail in the previous sections and shown graphically in Figure 7b. In summary, using the surrogate model appears to be beneficial independent of the population size used.

6.7 Perfect Surrogate

So far, we could demonstrate a clear benefit of Surrogate-Assisted GP in terms of convergence speed and convergence level as compared to Standard GP. Now we would like to understand how much better we might be able to do by further improving the surrogate model. To answer this question we performed additional experiments for Surrogate-Assisted GP with $n = 2$. In these experiments, we replaced the calculation of the phenotypic characterization and surrogate evaluation with a full fitness evaluation. Of course this takes much more time, as we are performing 60,000 instead of just 30,000 fitness evaluations, but offers a lower bound, and allows us to assess the performance if we had a perfect surrogate model.

Results of these runs are shown in Figure 10. Solid and dashed curves show the performance of Standard GP and Surrogate-Assisted GP as already shown above. Results for the hypothetical perfect surrogate are shown by the dash-dot curve. The two curves are very close which means that the surrogate model based on a rule’s phenotypic characterization, as used in this paper, is quite effective and, at least for the parameters investigated, allows to gain a large portion of the improvement potential over Standard GP.

7 Conclusion

In this paper, we presented a novel approach to improve the convergence speed of Genetic Programming with expensive fitness evaluations. Introducing the concept of

a phenotypic characterization, we enable the use of surrogate models in combination with GP. The idea is to record the outcome of the rule encoded in a GP individual in a specified set of decision situations, and work in the space of phenotypic characterizations rather than genotypes to construct and evaluate the surrogate model.

We have demonstrated the usefulness of our approach at the example of evolving dispatching rules for dynamic job shop scheduling. We present a phenotypic characterization for this problem, and show how it can be used to detect (and remove) phenotypically equivalent individuals, leading to a faster evolution of better solutions. We also show how the phenotypic characterizations can be used to successfully learn surrogate models that can be used to replace expensive fitness evaluations, further speeding up evolution. Together, our proposed approach saved up to 80% of the fitness evaluations compared to the standard GP model. The paper is thus an important advancement, allowing GP to be used for problems with computationally expensive fitness evaluations. A comparison with an alternative approach that uses a genotypic distance measure on the GP trees shows that the surrogate models built on phenotypic characterizations are much more accurate than those based on genotypic distances.

There are several ways to extend our work in the future. First, different modeling techniques can be investigated such as Neural Networks, Support Vector regression, or Gaussian Process regression. We expect such techniques to lead to even better surrogate quality. Second, there are several ways to improve the model management and integration of the surrogate in the GP run. What training data to use and what individuals to evaluate with the expensive fitness functions are currently handled in an effective, yet simple way, certainly allowing for further refinements and improvements in future work. Third, it would be interesting to further investigate the choice of decision situations that form the basis for the phenotypic characterization, and perhaps adapt these situations online during the run. Fourth, the idea should also be tested in other application domains, which would require to develop corresponding phenotypic characterizations. Last but not least it would be interesting to combine the work presented in this paper with efforts to create improved GP operators incorporating semantic information, such as proposed by Uy et al. (2011), and fitness sharing incorporating semantic information (Nguyen et al., 2012). Both areas seem to be complementary to our work and can probably be combined to further improve the performance of GP in application areas with expensive fitness evaluations.

Acknowledgment

The authors would like to thank Alberto Moraglio for the source code to compute the Structural Hamming Distance (SHD) as a syntactic/genotypic similarity measure between trees.

This work was partially supported by the German Research Foundation (DFG) under grant SCHO 540/17-2.

References

- Ashlock, D., Lee, C., 2013. Agent-case embeddings for the analysis of evolved systems. *IEEE Transactions on Evolutionary Computation* 17 (2), 227–240.
- Blackstone, J. H., Phillips, D. T., Hogg, G. L., 1982. A state-of-the-art survey of dispatch-

ing rules for manufacturing job shop operations. *International Journal of Production Research* 20 (1), 27–45.

Branke, J., Hildebrandt, T., Scholz-Reiter, B., 2013. Evolving dispatching rules—a comparison of rule representations. *Evolutionary Computation Journal* Submitted for publication.

Branke, J., Schmidt, C., 2003. Fast convergence by means of fitness estimation. *Soft Computing Journal* 9, 13–20.

Burke, E. K., Hyde, M., Kendall, G., Ochoa, G., Özcan, E., Woodward, J. R., 2010. A classification of hyper-heuristic approaches. In: Gendreau, M., Potvin, J.-Y. (Eds.), *Handbook of Metaheuristics*, 2nd Edition. Vol. 146 of *International Series in Operations Research and Management Science*. Springer, New York, pp. 449–468.

Burke, E. K., Hyde, M. R., Kendall, G., Ochoa, G., Özcan, E., Woodward, J. R., 2009. Exploring hyper-heuristic methodologies with genetic programming. In: Kacprzyk, J., Jain, L. C., Mumford, C. L., Jain, L. C. (Eds.), *Computational Intelligence*. Vol. 1 of *Intelligent Systems Reference Library*. Springer Berlin Heidelberg, pp. 177–201.

Dimopoulos, C., Zalzala, A. M. S., 2001. Investigating the use of genetic programming for a classic one-machine scheduling problem. *Advances in Engineering Software* 32 (6), 489–498.

Ekárt, A., Németh, S. Z., 2000. A metric for genetic programs and fitness sharing. In: *Proceedings of the European Conference on Genetic Programming*. Springer-Verlag, London, UK, UK, pp. 259–270.

El-Beltagy, M. A., Keane, A. J., Nair, P. B., 1999. Metamodeling techniques for evolutionary optimization of computationally expensive problems: Promises and limitations. In: *Genetic and Evolutionary Computation Conference*. Morgan Kaufmann, pp. 196–203.

Emmerich, M., Giotis, A., Özdemir, M., Bäck, T., Giannakoglou, K., 2002. Metamodel-assisted evolution strategies. In: *Proceedings of the 7th International Conference on Parallel Problem Solving from Nature. PPSN VII*. Springer-Verlag, London, UK, UK, pp. 361–370.

Geiger, C. D., Uzsoy, R., Aytug, H., 2006. Rapid modeling and discovery of priority dispatching rules: an autonomous learning approach. *Journal of Scheduling* 9 (1), 7–34.

Goel, T., Haftka, R. T., Shyy, W., Queipo, N. V., 2007. Ensemble of surrogates. *Structural and Multidisciplinary Optimization* 33 (3), 199–216.

Gustafson, S., Feb. 2004. An analysis of diversity in genetic programming. Ph.D. thesis, School of Computer Science and Information Technology, University of Nottingham, Nottingham, England.

Haupt, R., 1989. A survey of priority rule-based scheduling. *OR Spektrum* 11 (1), 3–16.

Hildebrandt, T., 2012. Jasima - an efficient Java Simulator for Manufacturing and Logistics. Last accessed 16th September 2013.
URL <http://code.google.com/p/jasima/>

- Hildebrandt, T., Heger, J., Scholz-Reiter, B., 2010. Towards improved dispatching rules for complex shop floor scenarios: a genetic programming approach. In: GECCO '10: Proceedings of the 12th annual conference on Genetic and evolutionary computation. ACM, New York, NY, USA, pp. 257–264.
- Holthaus, O., Rajendran, C., 1997. Efficient dispatching rules for scheduling in a job shop. *International Journal of Production Economics* 48 (1), 87–105.
- Holthaus, O., Rajendran, C., 2000. Efficient jobshop dispatching rules: further developments. *Production Planning & Control* 11 (2), 171–178.
- Hong, Y.-S., H.Lee, Tahk, M.-J., 2003. Acceleration of the convergence speed of evolutionary algorithms using multi-layer neural networks. *Engineering Optimization* 35 (1), 91–102.
- Jackson, D., 2011. Promoting phenotypic diversity in genetic programming. In: Schaefer, R., Cotta, C., Kolodziej, J., Rudolph, G. (Eds.), *Parallel Problem Solving from Nature – PPSN XI*. Vol. 6239 of *Lecture Notes in Computer Science*. Springer Berlin / Heidelberg, pp. 472–481.
- Jin, Y., 2005. A comprehensive survey of fitness approximation in evolutionary computation. *Soft Computing - A Fusion of Foundations, Methodologies and Applications* 9, 3–12.
- Jin, Y., 2011. Surrogate-assisted evolutionary computation: Recent advances and future challenges. *Swarm and Evolutionary Computation* 1 (2), 61–70.
- Jin, Y., Branke, J., 2005. Evolutionary optimization in uncertain environments—a survey. *Evolutionary Computation, IEEE Transactions on* 9 (3), 303–317.
- Jin, Y., Huesken, M., Sendhoff, B., 2003. Quality measures for approximate models in evolutionary computation. In: *Proceedings of GECCO Workshops: Workshop on Adaptation, Learning and Approximation in Evolutionary Computation*. AAAI, pp. 170–173.
- Jin, Y., Olhofer, M., Sendhoff, B., oct 2002. A framework for evolutionary optimization with approximate fitness functions. *Evolutionary Computation, IEEE Transactions on* 6 (5), 481–494.
- Koza, J. R., 1992. *Genetic Programming: On the Programming of Computers by Means of Natural Selection*. MIT Press, Cambridge, MA, USA.
- Law, A. M., 2007. *Simulation Modeling and Analysis*, 4th Edition. McGraw-Hill, New York, USA.
- Lehman, J., Stanley, K. O., 2010. Efficiently evolving programs through the search for novelty. In: *Genetic and Evolutionary Computation Conference*. ACM, pp. 837–844.
- Lim, D., Jin, Y., Ong, Y.-S., Sendhoff, B., june 2010. Generalizing surrogate-assisted evolutionary computation. *Evolutionary Computation, IEEE Transactions on* 14 (3), 329–355.
- Lim, D., Ong, Y.-S., Jin, Y., Sendhoff, B., 2007. A study on metamodeling techniques, ensembles, and multi-surrogates in evolutionary computation. In: *Genetic and Evolutionary Computation Conference*. ACM, pp. 1288–1295.

- Moraglio, A., Poli, R., sept. 2005. Geometric landscape of homologous crossover for syntactic trees. In: *Evolutionary Computation, 2005. The 2005 IEEE Congress on*. Vol. 1. pp. 427–434.
- Nguyen, Q., Nguyen, X., O’Neill, M., Agapitos, A., 2012. An investigation of fitness sharing with semantic and syntactic distance metrics. In: Moraglio, A., Silva, S., Krawiec, K., Machado, P., Cotta, C. (Eds.), *Genetic Programming*. Vol. 7244 of *Lecture Notes in Computer Science*. Springer Berlin / Heidelberg, pp. 109–120.
- Nguyen, S., Zhang, M., Johnston, M., Tan, K.-C., 2013a. Automatic design of scheduling policies for dynamic multi-objective job shop scheduling via cooperative coevolution genetic programming. *IEEE Transactions on Evolutionary Computation*.
URL DOI:10.1109/TEVC.2013.2248159
- Nguyen, S., Zhang, M., Johnston, M., Tan, K.-C., 2013b. A computational study of representations in genetic programming to evolve dispatching rules for the job shop scheduling problem. *IEEE Transactions on Evolutionary Computation* 17 (5), 621–639.
- Oduguwa, V., Roy, R., 2002. Multiobjective optimization of rolling rod product design using meta-modeling approach. In: *Genetic and Evolutionary Computation Conference*. Morgan Kaufmann, New York, pp. 1164–1171.
- Pfund, M. E., Mason, S. J., Fowler, J. W., 2006. Semiconductor manufacturing scheduling and dispatching. In: Herrmann, J. W. (Ed.), *Handbook of Production Scheduling*. Vol. 89 of *International Series in Operations Research & Management Science*. Springer, New York, pp. 213–241.
- Pickardt, C., Branke, J., Hildebrandt, T., Heger, J., Scholz-Reiter, B., 2010. Generating dispatching rules for semiconductor manufacturing to minimize weighted tardiness. In: Johansson, B., Jain, S., Montoya-Torres, J., Hukan, J., Yücesan, E. (Eds.), *Proceedings of the 2010 Winter Simulation Conference*. IEEE, New York, USA, pp. 2504–2515.
- Pickardt, C., Hildebrandt, T., Branke, J., Heger, J., Scholz-Reiter, B., 2013. Evolutionary generation of dispatching rule sets for complex dynamic scheduling problems. *International Journal of Production Economics*.
- Poli, R., Langdon, W. B., Mcphee, N. F., March 2008. *A field guide to genetic programming*.
- Rajendran, C., Holthaus, O., 1999. A comparative study of dispatching rules in dynamic flowshops and jobshops. *European Journal of Operational Research* 116 (1), 156–170.
- Rattle, A., 1998. Accelerating the convergence of evolutionary algorithms by fitness landscape approximation. In: *Parallel Problem Solving from Nature*. Springer, pp. 87–96.
- Runarsson, T. P., 2004. Constrained evolutionary optimization by approximate ranking and surrogate models. In: *Parallel Problem Solving from Nature*. No. 3242 in *LNCS*. Springer, pp. 401–410.
- Shi, L., Rasheed, K., 2010. A survey of fitness approximation methods applied in evolutionary algorithms. In: Tenne, Y., Goh, C.-K. (Eds.), *Computational Intelligence in Expensive Optimization Problems*. Vol. 2 of *Adaptation, Learning, and Optimization*. Springer Berlin Heidelberg, pp. 3–28.

Uy, N., Hoai, N., O'Neill, M., McKay, R., Galván-López, E., 2011. Semantically-based crossover in genetic programming: application to real-valued symbolic regression. *Genetic Programming and Evolvable Machines* 12, 91–119.