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# Modelling the measured local time evolution of strongly nonlinear heat pulses in the Large Helical Device

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## Abstract

In some magnetically confined plasmas, an applied pulse of rapid edge cooling can trigger either a positive or negative excursion in the core electron temperature from its steady state value. We present a new model which captures the time evolution of the transient, non-diffusive local dynamics in the core plasma. We show quantitative agreement between this model and recent spatially localized measurements (Inagaki *et al* 2010 *Plasma Phys. Control. Fusion* **52** 075002) of the local time-evolving temperature pulse in cold pulse propagation experiments in the Large Helical Device.

(Some figures may appear in colour only in the online journal)

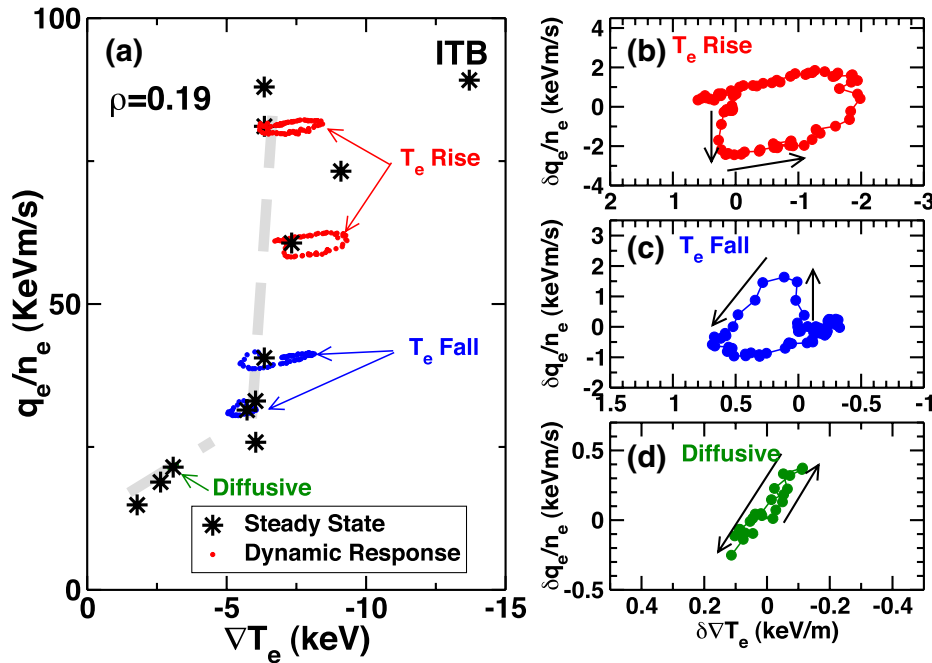
## 1. Introduction

Understanding, prediction and control of energy transport is central to achieving nuclear fusion in magnetically confined plasmas, which are large scale physical systems, nonlinearly coupled across a broad range of spatio-temporal scales and far from equilibrium. They are typically turbulent and can exhibit energy transport phenomenology which is nonlinear and non-diffusive [1–9]. At-a-point measurements of plasma parameters during cold heat pulse experiments in tokamak and stellarator plasmas [10–19] probe the underlying transport processes in a strongly perturbed regime, and are an unresolved challenge to interpretation. We note that the nature and implications of a local measurement of transport may differ significantly between tokamak and stellarator plasmas. For example, in a large aspect ratio tokamak, local magnetic shear is a good proxy for flux-surface-averaged magnetic shear, but this is not the case in a stellarator such as the Large Helical Device (LHD). Insofar as magnetic shear affects transport, this may be important. In these experiments [10–19], the

electron temperature  $T_e$  at the plasma edge is rapidly reduced by a transient local increase in radiation, typically induced by injection of a pellet which produces radiating impurity ions and cold electrons. The magnitude of the local gradient of electron temperature  $\nabla T_e$  at the edge is correspondingly increased. The subsequent measured local behaviour of the plasma, as the resultant cold pulse propagates rapidly inwards, cannot be understood in terms of either diffusive or convective transport. Paradoxically, an applied pulse of rapid edge cooling can trigger either a positive or negative excursion in the core electron temperature from its steady state value, depending on the confinement properties of the plasma [11–13, 19]; see, for example, figure 1. Spatially non-local transport properties have been inferred from cold pulse experiments, and critical temperature gradient scale length models and empirical non-local models have been tested [20–22]. These models, which often incorporate large scale transport codes, contribute to explaining various transient transport phenomena. However successful analytical models and numerical simulations based on the fundamental equations of plasma physics remain elusive. These issues remain topical, and their potential significance is growing. For example, Rice *et al* [23] have recently indicated that cold heat pulse effects observed in Alcator C-Mod may be closely connected to other seemingly



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**Figure 1.** Response of the core plasma to rapid edge cooling as seen in LHD [19]. (a) plots the core plasma conditions in the experiments at steady state. The three distinct transient responses to rapid edge cooling are shown in (b)–(d) and are a sharp temperature rise, a sharp temperature drop, and diffusive transport respectively. The corresponding core plasma conditions for each of these responses are indicated in (a).

unrelated transport effects, including core toroidal rotation reversals, energy confinement saturation and up/down impurity density asymmetries. Mantica *et al* [24] used cold pulses in JET to probe internal transport barriers. In recent reviews, cold pulse experiments are placed in the broader context of perturbative transport phenomena in fusion plasmas in [25], and theoretical approaches to nonlocal transport in tokamaks and stellarators are described and extended in [26].

Here we focus on understanding how the local core plasma responds, over time, to an applied pulse of rapid edge cooling, by exploiting newly available at-a-point measurements in the LHD [19]. In section 2, we propose a model comprising a set of three coupled nonlinear equations that depend on time, with spatial dependence entering implicitly through the local values of transport coefficients, which we infer from experimental measurements. Using experimental parameters as inputs, we show in section 3 that the system dynamics output from the model corresponds quantitatively to the observations. This suggests that we have captured the essential local time-evolving physics of the strongly nonlinear plasma response. The new physically motivated model is the first simple analytical model for local thermal evolution which captures both types of observed dynamics (central temperature rise or fall), which a successful model must predict. This approach may find wider application in understanding the pulsed nonlinear transport dynamics of other non-plasma macroscopic systems that are far from equilibrium.

## 2. Model equations

We propose here a model which we construct in terms of the three key observed thermal properties of the core plasma: the

deviation from steady state of the heat flux, of the electron temperature gradient, and of the electron temperature. These three variables are nonlinearly coupled to each other. In our model, the steady state turbulent plasma transport processes contribute only damping of the strongly nonlinear evolution of the system. This starting point is different from that of transport models constructed in terms of fundamental quantities of plasma physics, such as perturbed probability density functions, and from transport models constructed in terms of corrections to linear transport coefficients. Our model is motivated by recent experiments [17–19] of cold pulse propagation from edge ( $\rho = r/a = 1$ ) to deep core ( $\rho = 0.11$ ) of LHD, where  $a$  denotes the local minor radius (on average  $a = 0.6$  m) and  $r$  denotes distance from the axis of symmetry. Figure 1 encapsulates the results of these experiments, summarising the electron cyclotron emission (ECE) measurements of [19]. These track the simultaneous evolution in time, in response to the initial edge cooling, of two variables observed deep in the core at plasma radius  $\rho = 0.19$ . First, there is the measured excess of the local electron heat flux relative to its steady state value, normalized to local electron number density, represented by  $\delta q_e(\rho, t)/n_e$  defined by equation (1) of [19]. Second, there is the measured excess of the local electron temperature gradient relative to its steady state value, denoted by  $\delta \nabla T_e(\rho, t)$ . The LHD experiments show three distinct types of dynamics in these variables. Below a threshold in  $\nabla T_e$  there is diffusive transport, in which  $\delta q_e/n_e$  and  $\delta \nabla T_e$  rise and fall together. Above this threshold, there is a bifurcation in dynamics; for similar  $\nabla T_e$  the core plasma executes a Lissajous figure in  $\delta q_e/n_e$  and  $\delta \nabla T_e$  which encompasses either a local fall, or rise, in  $T_e$ . This bifurcation is conditioned by the magnitude of  $\delta q_e/n_e$ , and the

phenomenology can also depend on target plasma conditions and on the magnitude of the edge cold pulse [19]. The non-diffusive nature of the energy transport is also indicated by measurements of the time evolution of  $T_e$  at multiple ECE channels across the minor radius [19]. The edge cold pulse is observed to have no apparent effect on the value of  $T_e$  or  $\delta\nabla T_e$  midway across the minor radius, while the edge and core responses are separated by a time interval of a few milliseconds. This dynamical richness suggests non-trivial underlying equations.

Here we will show that the key quantitative aspects of this observed local time-evolving phenomenology in the LHD core plasma can be captured by the following physically motivated mathematical model, embodied in a system of three coupled nonlinear differential equations for the experimentally measured variables  $\delta q_e(\rho, t)/n_e$ ,  $\delta\nabla T_e$ , and  $T_e - T_{e0}$ . We assume that the excess turbulent heat flux  $\delta q_e(\rho, t)/n_e$  acts to reduce the magnitude of the local electron temperature gradient by carrying away thermal energy. Since the sign of the spatial gradient of temperature is negative, this corresponds to reducing the magnitude of the negative excess  $\delta\nabla T_e$ , that is, driving it in the positive direction. In parallel, we assume that the steady state turbulent transport acts to damp any non-zero  $\delta\nabla T_e$ , at a rate  $\gamma_{L1}$ . Hence our first model equation is

$$\frac{\partial}{\partial t}(\delta\nabla T_e) = \kappa_T(T_e, \nabla T_e) \frac{\delta q_e}{\chi_0 n_e} - \gamma_{L1} \delta\nabla T_e. \quad (1)$$

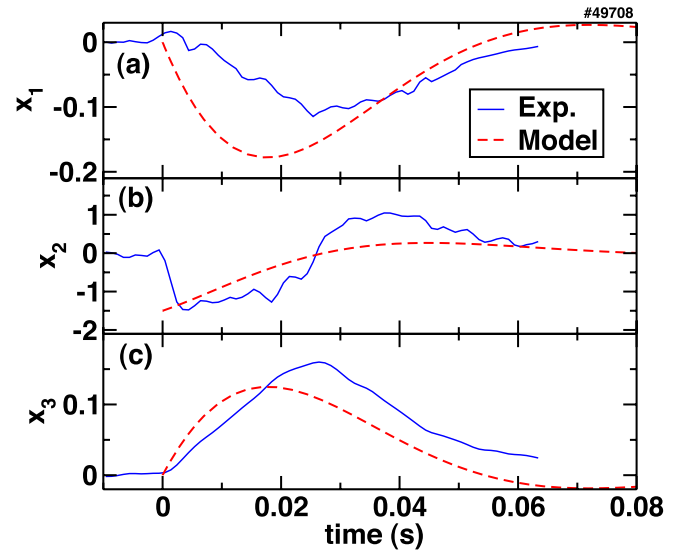
The vector heat flux has only one component, and similarly for the gradient operator. To normalize the dimensionally different variables  $\delta q_e/n_e$  and  $\delta\nabla T_e$ , we use the measured steady state turbulent heat diffusivity  $\chi_0$ , which is estimated by power balance analysis and is basically the same as the slope of figure 1(d) (the metric coefficient of magnetic flux surface is needed). The value of  $\chi_0$  also corresponds approximately to  $\chi_0 = L_c^2/\tau_c$ , where  $L_c$  is the characteristic scale-length of steady state turbulent transport ( $\sim a$ ) and  $\tau_c$  is the associated global energy confinement time. The coefficient  $\kappa_T$ , which has dimension inverse time, depends on both the local electron temperature  $T_e$  and on  $\delta\nabla T_e$ , which we treat as independent variables. The excess heat flux  $\delta q_e$  is a proxy for excess turbulence, and this is driven by excess (negative) temperature gradient and damped by the steady state turbulent transport, so we assume

$$\frac{\partial}{\partial t} \left( \frac{\delta q_e}{\chi_0 n_e} \right) = -\kappa_Q(T_e, \nabla T_e) \delta\nabla T_e - \gamma_{L1} \frac{\delta q_e}{\chi_0 n_e}. \quad (2)$$

We adopt a similar philosophy to [29] in our third model equation, for the local time derivative of the electron temperature difference  $T_e - T_{e0}$ , in assuming that it approximately matches the divergence of the local excess turbulent heat flux, on energy conservation grounds. We again assume that steady state turbulent transport acts to damp the deviation—here the temperature excess:

$$\frac{\partial}{\partial t}(T_e - T_{e0}) = -\eta \nabla \cdot \left( \frac{\delta q_e}{\chi_0 n_e} \right) - \gamma_{L2}(T_e - T_{e0}), \quad (3)$$

where  $\eta$  is the transient heat diffusivity whose value is taken to be identical to  $2\chi_0/3$ , thus nonlinearity in heat diffusivity is not



**Figure 2.** Time evolution of normalized (a)  $\delta\nabla T_e$ , (b)  $\delta q_e$  and (c)  $\delta T_e$  for the case where LHD core  $T_e$  rises, figure 1(b) of [19]. Blue solid lines indicate experimental data and red dash lines are calculated using equations (5) to (7). For normalization of experimental data, measured parameters are  $\chi_0 = 3.2 \text{ m}^2 \text{ s}^{-1}$ ,  $T_{e0} = 3.5 \text{ keV}$  and  $L_c = 1.1 \text{ m}$ . Model coefficients  $\kappa_{T0} = 15$ ,  $\partial\kappa_T/\partial x_1 = \partial\kappa_T/\partial x_3 = 1.5$ ,  $\kappa_{Q0} = 225$ ,  $\partial\kappa_Q/\partial x_1 = \partial\kappa_Q/\partial x_3 = 22.5$ ,  $\gamma_{L1} = \gamma_{L2} = 35$  and  $\eta/\tau_c\chi_0 = 10.5$  are used.

introduced in our model. In the divergence, we will replace  $\nabla$  by  $1/L_c$ . The coupling factor  $\kappa_T(T_e, \nabla T_e)$  can be Taylor expanded (we will see that this approximation is supported by the experimental observations) about its steady state turbulence value  $\kappa_{T0} = \kappa_T(T_e = T_{e0}, \delta\nabla T_e = 0)$ , giving to first order

$$\kappa_T(T_e, \delta\nabla T_e) = \kappa_{T0} + (T_e - T_{e0}) \frac{\partial\kappa_T}{\partial T_e} + \delta\nabla T_e \frac{\partial\kappa_T}{\partial \nabla T_e}. \quad (4)$$

In the same way,  $\kappa_Q(T_e, \nabla T_e)$  can be expanded about  $\kappa_{Q0} = \kappa_Q(T_e = T_{e0}, \delta\nabla T_e = 0)$ . Using these expressions in equations (1) and (2), and defining dimensionless variables  $x_1 = L_c \delta\nabla T_e/T_0$ ,  $x_2 = L_c \delta q_e/\chi_0 n_e T_0$  and  $x_3 = (T_e - T_{e0})/T_0$ , our system of equations becomes

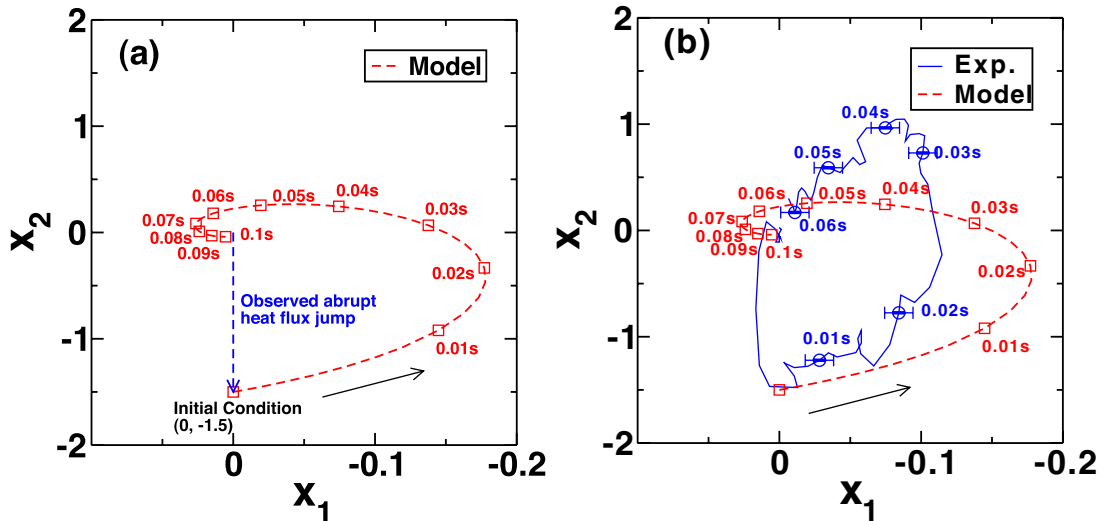
$$\frac{dx_1}{dt} = \kappa_{T0} x_2 + x_1 x_2 \frac{\partial\kappa_T}{\partial x_1} + x_2 x_3 \frac{\partial\kappa_T}{\partial x_3} - \gamma_{L1} x_1, \quad (5)$$

$$\frac{dx_2}{dt} = -\kappa_{Q0} x_1 - x_1^2 \frac{\partial\kappa_Q}{\partial x_1} - x_1 x_3 \frac{\partial\kappa_Q}{\partial x_3} - \gamma_{L1} x_2, \quad (6)$$

$$\frac{dx_3}{dt} = -\frac{1}{\tau_c} \frac{\eta}{\chi_0} x_2 - \gamma_{L2} x_3. \quad (7)$$

We note the strongly nonlinear character of this coupled system of equations, for which we know of no analytical solution. For these two reasons, the time evolution and final state of the system cannot be inferred from the initial conditions, other than by numerically solving the model as in the next section. In this respect our model differs fundamentally from approaches based on, for example, linear diffusion.

To summarize briefly, the LHD experiments outlined in Section 1 find that if the initial heat flux jump on arrival at  $\rho = 0.19$  is negative, the electron temperature rises, and



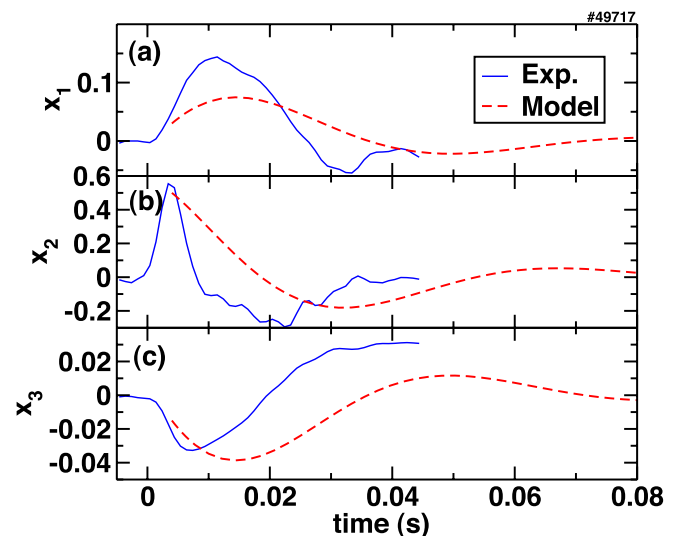
**Figure 3.** Normalized flux-gradient diagram obtained from the experimental and model results plotted in figure 2, where core  $T_e$  rises. The arrow denotes the direction of time evolution, and circles and squares are time-markers. (a) Model alone; (b) model and experiment overlaid.

vice versa. A challenge to theory is to find a model which reproduces this together with the time evolution of the three key experimental observables which are our model parameters, given the local initial conditions and the measured local plasma parameter values. In the next section, we show that our model in equations (5) to (7) achieves this.

### 3. Comparison of model outputs with LHD results

In our approach to modelling local plasma evolution in time but not space, the arrival of the pulse at a particular radial location is treated as an impulsive change in the local heat flux, local electron temperature gradient, and local electron temperature, all defined relative to their steady state values. This determines the initial conditions for our implementation of equations (5) to (7). We now solve numerically the system equations (5) to (7), using values for coefficients that are inferred from the experimental measurements [19] on LHD plasmas.

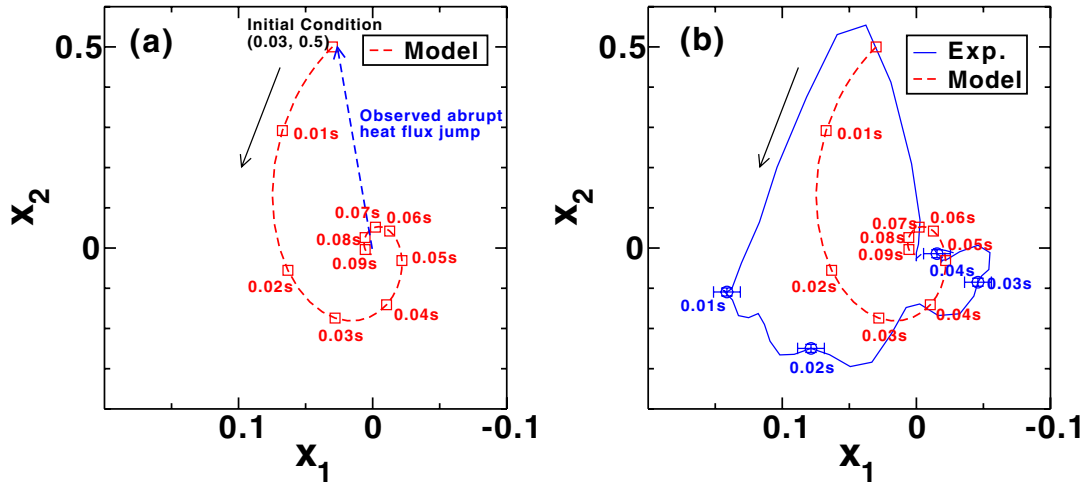
Figure 2 compares our model results to the corresponding experimental results in figure 1(b) of [19], where the temperature rises and then declines to the steady state value. The correspondence between the model output and experimental time series is good given that these are not fitted curves: both the model parameters, and the initial conditions, are determined independently from the plasma conditions in LHD. Measured values of  $\chi_0$ ,  $L_c$  and  $T_{e0}$  are employed for normalization of the time traces. The interaction between core heat flux and edge temperature gradient discussed in [19], which results in a local heat flux jump without change of local temperature gradient, provides the initial values of  $(x_1, x_2, x_3) = (0, -1.5, 0)$ . Coefficients in the model are estimated from direct experimental measurements, together with other physical considerations, as follows. Coefficients  $\kappa_{T0}$  and  $\kappa_{Q0}$  are the primary determinants of the characteristic time scale of variation of the measured variables, for which the observed value is  $\sim 60$  ms, and  $\sqrt{\kappa_{T0}\kappa_{Q0}} \sim 100$  s $^{-1}$ . Gyrokinetic-like dependence of thermal diffusivity on  $T_e$  and



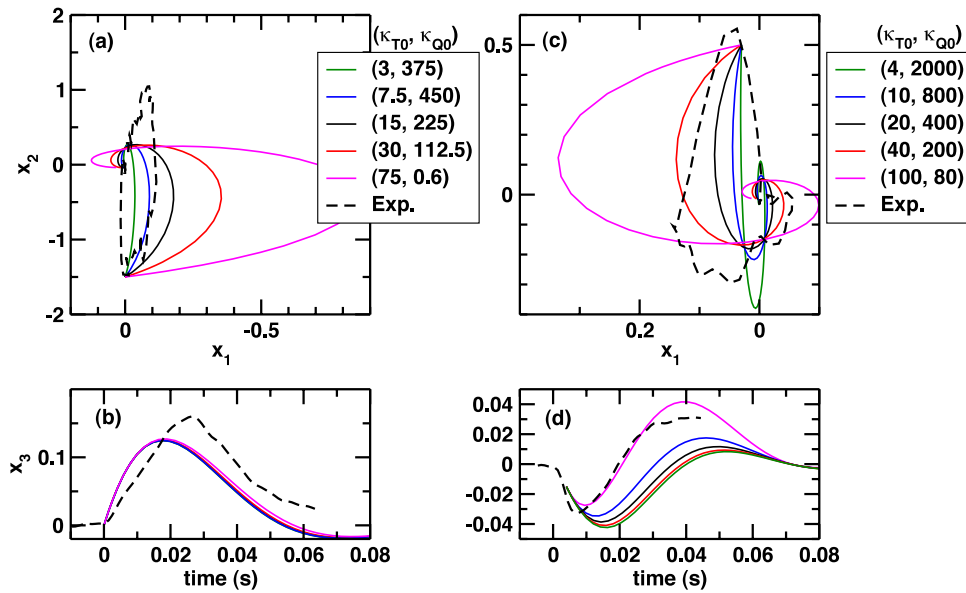
**Figure 4.** Time evolution of normalized (a)  $\delta \nabla T_e$ , (b)  $\delta q_e$  and (c)  $\delta T_e$  in the case where LHD core  $T_e$  falls, figure 1(c) of [19]. Blue solid lines indicate experimental data and red dashed lines are calculated using equations (5) to (7). For normalization of experimental data, measured parameters are  $\chi_0 = 2.4$  m $^2$ s $^{-1}$ ,  $T_{e0} = 2.9$  keV and  $L_c = 1.1$  m. Model coefficients of  $\kappa_{T0} = 20$ ,  $\partial \kappa_T / \partial x_1 = \partial \kappa_T / \partial x_3 = 2.0$ ,  $\kappa_{Q0} = 400$ ,  $\partial \kappa_Q / \partial x_1 = \partial \kappa_Q / \partial x_3 = 40$ ,  $\gamma_{L1} = \gamma_{L2} = 35$  and  $\eta / \tau_c \chi_0 = 10.5$  are used. The initial values of  $(x_1, x_2, x_3)$  are  $(0.03, 0.5, -0.015)$ .

$\nabla T_e$  is indicated by transient transport experiments in LHD, and  $\kappa_T$  and  $\kappa_Q$  are assumed to depend similarly on  $T_e$  and  $\nabla T_e$  [27, 28]. Hence we take  $\partial \kappa_T / \partial x_1 = \partial \kappa_T / \partial x_3 = 0.1 \kappa_{T0}$ ,  $\partial \kappa_Q / \partial x_1 = \partial \kappa_Q / \partial x_3 = 0.1 \kappa_{Q0}$ . There is thus empirical support for the truncation, to first order, of the Taylor expansion in equation (4) and its counterpart for  $\kappa_Q$ . Damping rates  $\gamma_{L1}$  and  $\gamma_{L2}$  are similar to the inverse of the global confinement time  $\tau_c \sim 80$  ms, and  $\eta / \tau_c \chi_0$  is of the order of  $\gamma_{L1}$ .

The correspondence between model and observations is shown in the phase plane portrait, figure 3, which plots the excursions in heat flux and temperature gradient, with time as a



**Figure 5.** Normalized flux-gradient plot obtained from the experimental and model results plotted in figure 4, where core  $T_e$  falls. The arrow denotes the direction of time evolution, and circles and squares are time-markers. (a) Model alone; (b) model and experiment overlaid.

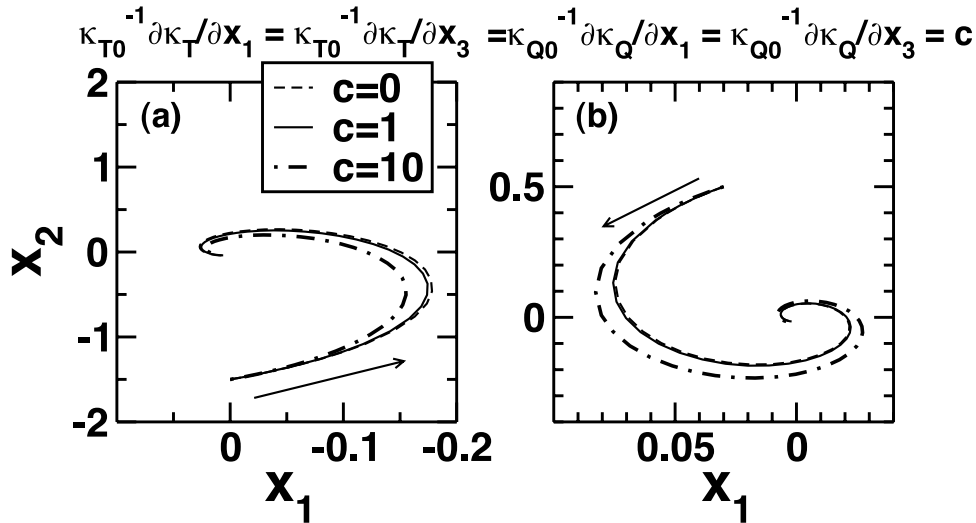


**Figure 6.** Dependence of model outputs on the numerical values of coupling parameters  $\kappa_{T0}$  and  $\kappa_{Q0}$ , with experimental comparisons. Upper panels show the normalized flux-gradient diagrams obtained from the experimental and model results, using different sets of values for  $\kappa_{T0}$  and  $\kappa_{Q0}$ , for the cases where LHD core  $T_e$  rises (a) and drops (c). Lower panels show the corresponding time evolution of the normalized temperature excursion  $\delta T_e(x_3)$  for the cases where  $T_e$  rises (b) and drops (d). Other model parameters are identical to those in figures 3 and 5.

parametric coordinate, as in [19]. Figure 3(a) shows the model evolution following the initial local negative perturbation in heat flux which is anticlockwise. This is overlaid with the experimental data in figure 3(b), which shows that both the direction of rotation and the approximate timing are consistent between model and experiment.

Figure 1 further shows that in the non-diffusive transport regime associated with larger heat fluxes, there is a second type of core temperature response with respect to the edge perturbation of LHD, in which the core temperature initially falls rather than rises. An important test of our model is that, with its coefficient values changed only in the way determined by the changed experimental conditions, it should reconstruct the time evolution of heat flux and  $T_e$  gradient in this case also. Encouragingly, the correspondence between model and observations is equally close in both cases. The results are

displayed in figures 4 and 5, which show the overlaid model and experiment timeseries and phase portrait in the same format as figures 2 and 3. Again, these are not fitted curves. In figures 4 and 5 the initial conditions differ substantially from figures 2 and 3 in that the initial heat flux jump is positive ( $x_2 = 0.5$ ). Slightly different coefficients  $\kappa_{T0} = 20$  and  $\kappa_{Q0} = 400$ , which reflect the differences in  $T_{e0}$  and  $\nabla T_{e0}$ , are used, but the same  $T_e$  and  $\nabla T_e$  dependences of  $\kappa_T$  ( $\kappa_Q$ ) as above are assumed:  $\partial\kappa_T/\partial x_1 = \partial\kappa_T/\partial x_3 = 0.1\kappa_{T0}$ ,  $\partial\kappa_Q/\partial x_1 = \partial\kappa_Q/\partial x_3 = 0.1\kappa_{Q0}$ . Damping rates  $\gamma_{L1}$ ,  $\gamma_{L2}$  and  $\eta/\tau_c\chi_0$  identical to those in figure 2 are employed. Both forms of strongly nonlinear response of the experimental system are thus captured by our model, by using as initial condition the locally observed impulsive change in heat flux, together with values for model coefficients that are inferred from the experimental measurements [19] on LHD.



**Figure 7.** Insensitivity of model outputs to the values of the coefficients in the Taylor expansion of the coupling parameters  $\kappa_{T0}$  and  $\kappa_{Q0}$ , as in equation (4). The four expansion parameters are set equal to each other, and take the values 0, 1 and 10 to generate the three traces shown in this normalized flux-gradient diagram obtained from the model for the case where LHD core  $T_e$  (a) rises and (b) falls. Other model parameters are identical to those in figures 3 and 5 respectively.

#### 4. Discussion

In our model, non-diffusive nonlinear coupling between heat flux and temperature gradient is essential. This coupling is embodied in the coupling parameters,  $\kappa_T$  and  $\kappa_Q$ . Whereas values for the model parameters associated with quasi-equilibrium transport properties, such as  $\chi_0$  and  $\gamma_{L1}$ , can be evaluated directly from experimental measurements, this is more difficult for the newly introduced coupling parameters. We have calculated the values of the coupling parameters as follows. First, we note that if the coupling parameters were independent of  $T_e$  and  $\nabla T_e$ , a damped oscillatory solution of equations (1) and (2) would exist, proportional to  $\exp(-t/\tau) \sin(\omega t)$ , where  $\omega^2 = \kappa_{T0}\kappa_{Q0}$  and  $1/\tau = \gamma_{L1}$ . From the experimental measurements of the oscillation period and duration of the pulses in  $\delta q_e$  and  $\delta \nabla T_e$ , we can therefore estimate the possible range of values of  $\kappa_{T0}\kappa_{Q0}$  and  $\gamma_{L1}$  in this simplified limit. Figure 6 demonstrates that the output of our model depends strongly on the values of  $\kappa_{T0}$  and  $\kappa_{Q0}$ . We can minimize the difference between experimental and model results by choosing optimal values for  $\kappa_{T0}$  and  $\kappa_{Q0}$  from within this range. These values for  $\kappa_{T0}$  and  $\kappa_{Q0}$  are found to lie between  $\sim 1/\tau_c$  and  $\sim 10/\tau_c$ .

In addition, we expect the dependence of coupling parameters on local thermodynamic variables to play a role. Taking the gyro-Bohm dependence of thermal diffusivity as a conceptual starting point, we assume that the coupling parameters  $\kappa_T$  and  $\kappa_Q$  depend on the local temperature and its spatial gradient. An example of the relative insensitivity of our model output to the  $T_e$  and  $\nabla T_e$  dependence of the coupling parameters is shown in figure 7. This plots the normalized flux-gradient diagram inferred from the model, using different  $T_e$  and  $\nabla T_e$  dependence for the coupling parameters. Importantly, we find that even if there is strong  $T_e$  and  $\nabla T_e$  dependence, the output of the model is qualitatively similar to the case where there is no dependence. We note that dependence of the

coupling parameters on the remaining thermodynamic variable in the present context, namely the heat flux, would imply significantly different physics, in particular a requirement for non-local dependence, as indicated in [17].

#### 5. Conclusions

The physical model represented by equations (5) to (7) is mathematically simple in its structure, and is constructed in terms of variables that are directly observed and inferred experimentally. It is motivated by the strongly nonlinear plasma response to perturbations acting on an already turbulent system seen, in particular, in LHD. There is quantitative agreement between our new analytical model and local measurements of time-evolving heat fluxes, temperature gradients, and temperature excursions. So far as we are aware, this is a novel result. Our model may have interpretive and predictive potential for fusion plasmas beyond LHD, insofar as the recent LHD results [17–19] represent state-of-art measurements of heat pulse phenomenology that may share features in common with nonlinear heat pulse measurements on other experiments [10–15].

Modelling the response to a nonlinear heat pulse is important for the development of fundamental understanding of the equilibrium and non-equilibrium transport processes which govern energy confinement in magnetically confined fusion plasmas. These transport processes arise from phenomenology that is also found beyond the plasma state: multi-scale coupled physics, incorporating turbulence and coherent nonlinear structures such as zonal flows, in a spatially inhomogeneous macroscopic driven-dissipative system that has many degrees of freedom. The approach taken here to modelling strongly nonlinear perturbed transport phenomenology in LHD may therefore be of wider physical interest, in at least two respects. First, our model embodies a separation of timescales between the slow pulse evolution



and the fast initial change in local temperature gradient. This separation of timescales is characteristic of anomalous or bursty transport. Second, we model the dynamics in terms of deviations from steady state, not necessarily from equilibrium. This may be helpful in modelling the dynamics of other systems that are far from equilibrium.

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